MgB$_2$ hot-electron bolometer mixers for sub-mm wave astronomy

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Cover:
Left: HPCVD system deposition chamber. Center upper left: SEM image of spiral antenna coupled MgB$_2$ HEB. Center upper right: TEM image of 5 nm thick HPCVD grown MgB$_2$ film on SiC substrate. Center: Cold plate of LHe cryostat. Center lower left: SEM image of HPCVD grown MgB$_2$ film on Al$_2$O$_3$ substrate. Center lower right: 3D CAD image of MgB$_2$ HEB. Upper right: Chamber view during MgB$_2$ film deposition. Lower right: mixer block with Si lens. Designed by Niia Silaeva.

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Per aspera ad astra
Abstract

Spectroscopy and photometry in the terahertz (THz) range of remote space objects allows for a study of their chemical composition, because this range covers rotational lines from simple molecules and electron transition lines from atoms and ions. Due to high spectral resolution, THz heterodyne receivers allow for studying dynamical properties of space objects manifested in doppler-shifted emission lines. Niobium nitride (NbN) hot-electron bolometer (HEB) mixers currently used at frequencies >1 THz, provide a typical gain bandwidth (GBW) of 3 GHz, and consequently, a noise bandwidth (NBW) of 4 GHz. This property severely limits the functionality of astronomical instruments. Moreover, the low critical temperature ($T_c = 8–11$ K) of NbN ultrathin films necessitates usage of liquid helium (LHe) for device cooling, which reduces lifetime of spaceborne missions.

In this thesis, a study of HEB mixers dedicated for sub-mm wave astronomy applications made from magnesium diboride ($\text{MgB}_2$) ultrathin films is presented. It is shown that $\text{MgB}_2$ HEB mixers reach a unique combination of low noise, wide noise bandwidth, and high operation temperature when 8 nm thick $\text{MgB}_2$ films ($T_c = 30$ K) are used. The hybrid physical chemical vapour deposition (HPCVD) technique allows for reproducible deposition of such thin films. The high $T_c$ of $\text{MgB}_2$ (39 K), and consequently, short (3 ps) electron-phonon interaction time result in a GBW of up to 10 GHz and possibility of operation at temperatures $>20$ K, where compact cryocoolers are available. The GBW was observed to be almost independent on both bias voltage and bath temperature. A NBW of 11 GHz with a minimum double sideband (DSB) receiver noise temperature of 930 K is achieved at a 1.63 THz local oscillator (LO) and a 5 K bath temperature. At 15 K and 20 K, noise temperatures are 1100 K and 1600 K, respectively. From 0.69 THz to 1.63 THz noise increases by only 12%, and hence, low noise performance is expected even at higher frequencies. The minimum receiver noise temperature is achieved in a quite large range of both bias voltages (5–10 mV) and LO power. Compared to initial results, higher sensitivity and larger NBW are due to a larger HEB width (lower contact resistance), applied in-situ contact cleaning, and a smaller film thickness. The increase of noise temperature when operation temperature rises from 5 K to 20 K is due to a reduction of conversion gain by 2–4 dB caused by the reduced LO power absorbed in the HEB. The output noise of the HEB remains the same (120–220 K depending on the bias point).

Keywords: conversion gain, electron-phonon interaction, gain bandwidth, hot-electron bolometer, magnesium diboride, mixer, noise bandwidth, noise temperature, superconductor, thin film, THz detector.
List of Publications

Appended papers

This thesis is based on the following papers:


[F] E. Novoselov and S. Cherednichenko, “Broadband MgB$_2$ hot-electron bolometer THz mixers operating up to 20 K,” in *IEEE Transactions on Applied Superconductivity*, vol. 27, no. 4, June 2017, Art. no. 2300504.


Other papers and publications

The following papers and publications are not appended to the thesis, either due to contents overlapping of that of appended papers, or due to contents not related to the thesis.


### Notations and Abbreviations

#### Notations

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<th>Description</th>
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<tbody>
<tr>
<td>$2\Delta$</td>
<td>Superconducting energy gap</td>
</tr>
<tr>
<td>$2\Delta_{dirty}$</td>
<td>Dirty limit superconducting energy gap</td>
</tr>
<tr>
<td>$2\Delta_\pi$</td>
<td>Superconducting energy $\pi$-gap</td>
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<td>$2\Delta_\sigma$</td>
<td>Superconducting energy $\sigma$-gap</td>
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<td>$\hbar$</td>
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<td>$\alpha$</td>
<td>Thermometer local sensitivity</td>
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<td>$\beta$</td>
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<td>$\gamma$</td>
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<td>$\Delta U_0$</td>
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<td>$P$</td>
<td>Power</td>
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<td>$P_{hot}$</td>
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<td>Temperature</td>
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<td>$t$</td>
<td>Time</td>
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<td>Debye temperature</td>
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<td>$T_{FL}$</td>
<td>Thermal fluctuation noise</td>
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<td>Definition</td>
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<td>$T_J$</td>
<td>Johnson noise</td>
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<td>IF chain noise temperature</td>
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<td>$T_{opt}$</td>
<td>Equivalent noise temperature of optical components</td>
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<td>Mixer output noise temperature</td>
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<td>Phonon temperature</td>
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<td>$T_{rec}$</td>
<td>Receiver noise temperature</td>
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<td>$T_{REF}$</td>
<td>Equivalent noise temperature at the reference state</td>
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<td>$u$</td>
<td>Speed of sound</td>
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<td>$U$</td>
<td>Voltage</td>
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<tr>
<td>$U_0$</td>
<td>Bias voltage</td>
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<td>$U_{LO}$</td>
<td>Voltage amplitude of the local oscillator</td>
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<tr>
<td>$U_s$</td>
<td>Voltage amplitude of the signal</td>
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<tr>
<td>$W$</td>
<td>Bolometer width</td>
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<td>$Z$</td>
<td>Bolometer impedance</td>
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### Abbreviations

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<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tr>
<td>2-T</td>
<td>Two-temperature</td>
</tr>
<tr>
<td>3D</td>
<td>Three-dimensional</td>
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<tr>
<td>AFM</td>
<td>Atomic force microscope</td>
</tr>
<tr>
<td>Al₂O₃</td>
<td>Sapphire</td>
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<tr>
<td>Ar</td>
<td>Argon</td>
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<tr>
<td>Au</td>
<td>Gold</td>
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<tr>
<td>B</td>
<td>Boron</td>
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<td>B₂H₆</td>
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<tr>
<td>BCS</td>
<td>Bardeen-Cooper-Schrieffer</td>
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<td>BH₃</td>
<td>Borane</td>
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<td>BWO</td>
<td>Backward-wave oscillator</td>
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<td>CAD</td>
<td>Computer-aided design</td>
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<td>CH₂F₂</td>
<td>Difluoromethane</td>
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<td>Formic acid</td>
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<td>Direct current</td>
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<td>Double sideband</td>
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<td>Far Infrared</td>
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<td>GBW</td>
<td>Gain bandwidth</td>
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<td>GHz</td>
<td>10⁹ Hz</td>
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<td>H₂</td>
<td>Hydrogen</td>
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<td>HCl</td>
<td>Hydrogen chloride</td>
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<tr>
<td>HDPE</td>
<td>High-density polyethylene</td>
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<td>HEB</td>
<td>Hot electron bolometer</td>
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<tr>
<td>HEMT</td>
<td>High-electron-mobility transistor</td>
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<td>HPCVD</td>
<td>Hybrid physical chemical vapour deposition</td>
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<td>IF</td>
<td>Intermediate frequency</td>
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<tr>
<td>IR</td>
<td>Infrared</td>
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<tr>
<td>InP</td>
<td>Indium phosphide</td>
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<tr>
<td>InSb</td>
<td>Indium antimonide</td>
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<td>I-V</td>
<td>Current versus voltage</td>
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<tr>
<td>LHe</td>
<td>Liquid helium</td>
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<tr>
<td>LO</td>
<td>Local oscillator</td>
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<tr>
<td>LSB</td>
<td>Lower sideband</td>
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<tr>
<td>MBE</td>
<td>Molecular beam epitaxy</td>
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<tr>
<td>Mg</td>
<td>Magnesium</td>
</tr>
<tr>
<td>MgO</td>
<td>Magnesium oxide</td>
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<tr>
<td>MgB₂</td>
<td>Magnesium diboride</td>
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<tr>
<td>N₂</td>
<td>Nitrogen</td>
</tr>
<tr>
<td>NbN</td>
<td>Niobium nitride</td>
</tr>
<tr>
<td>NbTiN</td>
<td>Niobium titanium nitride</td>
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<tr>
<td>NBW</td>
<td>Noise bandwidth</td>
</tr>
<tr>
<td>O₂</td>
<td>Oxygen</td>
</tr>
<tr>
<td>PLD</td>
<td>Pulsed laser deposition</td>
</tr>
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<td>RF</td>
<td>Radio frequency</td>
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<td>R-T</td>
<td>Resistance versus temperature</td>
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<td>SEM</td>
<td>Scanning electron microscope</td>
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<tr>
<td>Abbreviation</td>
<td>Description</td>
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<td>--------------</td>
<td>-------------</td>
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<tr>
<td>SD</td>
<td>Schottky diode</td>
</tr>
<tr>
<td>Si</td>
<td>Silicon</td>
</tr>
<tr>
<td>SiC</td>
<td>Silicon carbide</td>
</tr>
<tr>
<td>SiN$_x$</td>
<td>Silicon nitride</td>
</tr>
<tr>
<td>SiO$_2$</td>
<td>Silicon dioxide</td>
</tr>
<tr>
<td>SIS</td>
<td>Superconductor-insulator-superconductor tunnel junction</td>
</tr>
<tr>
<td>SSPD</td>
<td>Superconducting single-photon detector</td>
</tr>
<tr>
<td>SQUID</td>
<td>Superconducting quantum interference device</td>
</tr>
<tr>
<td>TEM</td>
<td>Transmission electron microscope</td>
</tr>
<tr>
<td>THz</td>
<td>$10^{12}$ Hz</td>
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<tr>
<td>Ti</td>
<td>Titanium</td>
</tr>
<tr>
<td>USB</td>
<td>Upper sideband</td>
</tr>
<tr>
<td>UV</td>
<td>Ultraviolet</td>
</tr>
<tr>
<td>XRD</td>
<td>X-ray diffractometer</td>
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<td>YIG</td>
<td>Yttrium iron garnet</td>
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Acknowledgments

Bibliography

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Chapter 1

Introduction

The 0.1–10 THz part of electromagnetic spectrum between the microwave and infrared (IR) bands is referred to as terahertz (THz) range [1, 2]. Despite technological difficulties (the THz gap), this region has proven to be of great interest for medical [3] and security [4] sensing, communication [5], and Earth and Space science [6]. The THz range covers rotational lines from simple molecules and the ground state fine-structure emission lines from atoms and ions [7]. This is of great interest for astronomy [8], because of the possibility to study physics, dynamics, and chemistry of galaxies, star-formation regions, the interstellar medium, comets, asteroids, outer planet atmospheres, etc.

In order to resolve fine structure of molecular emission lines, heterodyne receivers with a high spectral resolution ($\lambda/\Delta\lambda \approx 10^6–10^7$) are required [9, 10]. For such applications several types of devices have been used as a mixer element for a heterodyne receiver, e.g. Schottky diodes (SD) [11], superconductor-insulator-superconductor tunnel junctions (SIS) [12], hot-electron bolometers (HEB) [13]. At frequencies above 1 THz HEBs are devices of choice (see Figure 1.1). Superconducting HEB mixers were introduced in Ref. [14] after the discovery of the electron-heating effect in superconducting films [15]. Until recently, the state-of-the-art phonon-cooled HEBs were fabricated using niobium nitride (NbN) and niobium titanium nitride (NbTiN) ultrathin films. HEB mixers are highly sensitive THz detectors providing a low receiver noise temperature from 300 K at 1.3 THz local oscillator (LO) [16] to 1150 K at 5.25 THz LO [17]. They were employed in many receivers for astronomical and atmospheric science observation programs launched in recent years, e.g. RLT [18], APEX [19, 20], the Herschel Space Observatory [21, 22], TELIS [23, 24], STO/STO-2 [25–29], and SOFIA [30–32]. They were also chosen for a number of current programs and programs under development, such as ASTE [33,34], DATE5 [16,35], SMILES-2 [36,37], GUSSTO [38], Millimetron [39,40], FIRSPEX [41], and OST [42].

NbN HEB mixers typically have a gain bandwidth (GBW) of $\approx 3$ GHz (NbTiN HEB mixers have even smaller GBW of $\approx 2$ GHz). As a result, the receiver noise temperature increases towards higher intermediate frequencies (IF) and doubles already at an IF of $\approx 4$ GHz. Therefore, the number of scientific tasks in sub-mm wave astronomy which can be performed with HEB mixers is limited [43].
Chapter 1. Introduction

Fig. 1.1: State-of-the-art noise temperature versus LO frequency for different THz mixer technologies: SD [44–69]; SIS [70–90]; NbN, NbTiN HEB [16,17,19,31–35,91–121]; and MgB$_2$ HEB [122–126].

Figure 1.2(a) demonstrates a mapping of Galaxy M82 by the HIFI instrument of the Hershel Space Observatory [43]. The high spectral resolution and sensitivity of the HIFI instrument allowed for observation of very weak (<5 K) frequency-shifted emissions from the two arms of the galaxy. Measured spectra at 0.57 THz (CO line) and 1.9 THz (CII line) are shown in Figure 1.2(b). One arm of the galaxy is moving towards us and the other from us, which results in the existence of two main velocity components: the blue-shifted and the red-shifted emission lobes, which are clearly seen on the left spectrum in Figure 1.2(b). The large difference between relative to the Earth velocities of the Galaxy M82 arms of 400 km/s resulted in the rather broad 1.9 THz CII spectral line (2.5 GHz). The nominal IF bandwidth of the used receivers (2.4 GHz) was just enough to fit this spectral line, but it did not allow to get the baseline of the signal properly. At the same time, the observation at higher frequencies might be interesting due to the smaller beam size. For example, the beam at 1.9 THz was almost four times smaller than at 0.57 THz (red bars on Figure 1.2(a)). Moreover, emission lines for some molecules exist only at higher frequencies. At 4.7 THz such velocity difference will result in ≈6 GHz broad lines, which is well above a typical NbN HEB mixer bandwidth. On the other hand, a superconducting critical temperature (T$_c$) of 8–11 K limits NbN HEB mixer operation to liquid helium (LHe) temperatures (<6 K). The lack of 4K cryocoolers qualified for space application necessitates of LHe utilization that leads to very limited spaceborne mission lifetimes. In order to improve the functionality of HEB mixers, other superconducting materials must be used, e.g. magnesium diboride (MgB$_2$).

The discovery of superconductivity in MgB$_2$ [127] with the highest T$_c$ among intermetallic compounds (bulk T$_c$ = 39 K) and fast progress in thin film deposition techniques [128–130] opened new opportunities in HEB development. For the first time heterodyne mixing using a MgB$_2$ HEB with a T$_c$ of 22 K made from a molecular beam epitaxy (MBE) grown [130] 20 nm thick
film on a silicon (Si) substrate was reported in 2007 [122]. The device had a rather high receiver noise temperature of 11 000 K at 1.6 THz but the GBW was already 2.3 GHz at 0.6 THz despite such a thick film.

In subsequent works by Bevilacqua et al. [123,124,131] the GBW of MgB$_2$ HEB mixers made from MBE grown films on c-cut sapphire (Al$_2$O$_3$) substrates was studied the most. The large dimensions of initial HEBs (100–500 µm$^2$) and consequently high LO power requirements forced the utilization of low frequency (0.35–0.6 THz) sources providing more output power for device characterisation. Therefore, a large superconducting energy gap necessitated the use of high bath temperatures of up to few degrees below the $T_c$ in order to make the gap smaller than the energy of photons. The maximum GBW of 3.4 GHz was achieved with a 10 nm thick device with a $T_c$ of 14 K [124]. And the possibility to increase the GBW up to 8–10 GHz using 3–5 nm thick MgB$_2$ HEB mixers with a $T_c$ >30 K was suggested [123]. Fabrication of smaller devices (3–42 µm$^2$) that requires less LO power allowed for the study of MgB$_2$ HEB mixers sensitivity in a wide range of bath temperatures [123, 124]. The minimum noise temperature of 800 K at 0.6 THz was demonstrated with a device with a $T_c$ of 8.5 K [123]. A HEB mixer with a $T_c$ of 15 K had a higher noise temperature of 1500 K, but it was also shown that the noise temperature remains constant at bath temperatures ranging from 4.2 K up to 10.5 K [124]. The need for fabrication of submicron size MgB$_2$ HEB mixers for operation at higher LO frequencies was highlighted [124].

In parallel work on MgB$_2$ HEB mixers by Cunnane et al. [125,126,132] devices made from hybrid physical-chemical vapour deposition (HPCVD) grown [133] films on silicon carbide (SiC) substrates were studied. A GBW greater than 8 GHz was demonstrated with a 15 nm thick HEB mixer with a $T_c$ of 33 K. The best noise performance achieved for HEB mixers made from HPCVD grown films was 2000 K at 0.6 THz [126]. This device had a noise bandwidth (NBW) of 6.5 GHz and the noise temperature had a minimal dependance on a bath temperature up to 20 K. At 1.9 THz, the noise temperature of such device increased to 3600 K.
The research presented in this thesis addresses the problem of limited bandwidth and low operation temperature of THz HEB mixers. The increase of bandwidth and operation temperature is required without sacrificing the low noise performance. The low noise temperature and the large bandwidth were shown for MgB$_2$ HEB mixers separately, but devices simultaneously demonstrating both of these features were not achieved. **The achievement of sensitivity and bandwidth superior to NbN HEB mixers and operation at bath temperatures above the LHe temperature by fabrication of submicron size MgB$_2$ HEB mixers was the main goal of this work.**

- The performance of HEB mixer is mainly affected by the quality of superconducting thin film used for device fabrication. **The primary goal** was to develop the process for growth of MgB$_2$ ultrathin (5-10 nm thick) films with a $T_c$ above 30 K, low roughness, high homogeneity, and applicable for fabrication of submicron size structures.

- **The second goal** was the development of HEB fabrication process capable for submicron size device fabrication, preserving superconducting film quality, and providing a high yield and a high robustness.

- **Third,** the fabricated HEB mixers should be tested at THz frequencies. The dependance of their intrinsic parameters on LO frequency and power, a $T_c$, and a bath temperature should be studied in order to find the way for further MgB$_2$ HEB mixers improvement and their optimization for specific tasks.

The thesis is structured in 6 chapters. **Chapter 2** contains an overview of: bolometer detection principles, heterodyne mixing, HEB modeling, and design of heterodyne receivers utilizing HEB mixers. **Chapter 3** describes the HPCVD technique used for MgB$_2$ ultrathin film deposition and the study of achieved films. The electron beam (e-beam) and ultraviolet (UV) lithography HEB fabrication processes are presented in **Chapter 4.** **Chapter 5** provides the detailed description of the measurement setup and techniques used for device characterization at THz frequencies. The summary of THz characterization results is given in **Chapter 6.** Finally, **Chapter 7** summarises the results of this work and provides the future outlook.
Chapter 2

Background

This chapter provides an overview of: bolometer operation principles and main characteristics which determine the bolometer performance. Total power and frequency selective detection regimes of bolometer operation are described and discussed. The lumped HEB mixer model and the two-temperature (2-T) model of electron-phonon relaxation are presented as well as an overview of heterodyne receivers designs.

2.1 Bolometric receiver

A simple bolometer consists of three parts. Figure 2.1(a) represents these parts: an absorber where an incident power is absorbed and thermalized; a perfectly coupled thermometer which measures changes of the absorber temperature; and a weak thermal link connecting the absorber and a heat sink to return the absorber into the initial state in an absence of incident power. The absorber is characterised by a heat capacity C, the thermal link by a thermal conductivity G and the heat sink by a temperature $T_{\text{bath}}$.

![Diagram of simple bolometer](image)

Fig. 2.1: (a) Schematic of simple bolometer consisting of an absorber with a heat C, a thermometer and a weak link with a thermal conductivity G connecting the absorber to a heat sink with a temperature $T_{\text{bath}}$. (b) Schematic representation of bolometer working principle. An incoming radiation with a total power $P_0$ increases bolometer temperature by $\Delta T = P_0/G$. After the incoming radiation is removed the bolometer temperature decays back with a time constant $\tau = C/G$. 

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Chapter 2. Background

This device can be used to measure a steady power input $P_0$ which gives a temperature increase of $\Delta T = P_0/G$ with an assumption of uniform heating of the bolometer. In case of a variable power $P(t)$ the dynamics of the bolometer temperature $T_b$ can be described by a heat balance equation:

$$C \frac{dT_b}{dt} + G(T_b - T_{bath}) = P(t) \quad (2.1)$$

When the bolometer is no longer irradiated, i.e. $P(t) = 0$, its temperature relaxes back to $T_{bath}$. Then Equation 2.1 can be solved as:

$$T_b(t) = T_{bath} + \Delta T e^{-\frac{t}{\tau}} \quad (2.2)$$

where $\tau = C/G$ is a bolometer time constant.

### 2.1.1 Direct detection

Being irradiated by the input power $P_0$ the receiver produces a direct current (DC) voltage response $\Delta U_0$ which is proportional to the power of incoming radiation (see Figure 2.2). In this case the receiver measures the total power of incoming radiation independently on frequency in the whole band where the receiver is sensitive. The total power detector is characterised by a voltage responsivity:

$$R_v = \frac{\Delta U_0}{P_0} \quad (2.3)$$

An electrical resistance thermometer (thermistor) (see Figure 2.3) might be used to measure the temperature of bolometer. In the electrical resistance thermometer a change in temperature is converted into a change in resistance $R_t$, which is converted into voltage changes with a readout current. The temperature of such a bolometer irradiated by an incident signal ($\omega_s$) with a power $P(t) = P_0 + P_1 e^{i\omega_s t}$ changes as $T_b = T_0 + T_1 e^{i\omega_s t}$. The voltage responsivity of bolometer with a thermistor biased with a constant current $I_0$ is [134]:

$$R_v = \frac{I_0 \frac{dR_t}{dT}}{G_d - I_0^2 \left(\frac{dR_t}{dT}\right) + i\omega_s C} \quad (2.4)$$

where $G_d = dP/dT$ is a dynamic thermal conductance at the temperature $T_0$. Equation 2.4 is valid if the load resistance $R_L \gg R_t$. The bolometer responsivity is influenced by the thermal feedback which can be expressed as the effective thermal conductance $G_e = G_d - I^2 (dR_t/dT)$. The thermal feedback also modifies the measured bolometer time constant $\tau_e = C/G_e$. It is
2.1. Bolometric receiver

![Bias circuit of electrical resistance thermometer.](image)

**Fig. 2.3:** Bias circuit of electrical resistance thermometer. $I_0$ is the bias current, $U_0$ the bias voltage, $R_L$ the load resistance, $R_t(T)$ the temperature dependent thermometer resistance.

![Voltage responsivity versus frequency graph.](image)

**Fig. 2.4:** Voltage responsivity versus frequency.

It is convenient to define a local sensitivity for the thermometer

$$\alpha = \frac{dR_t}{dT}$$

evaluated at $T_0$. With new definitions the voltage responsivity becomes:

$$R_v = \frac{I_0 R_t \alpha}{G_e (1 + i\omega \tau_e)} \quad (2.5)$$

The module of voltage responsivity:

$$|R_v| = \frac{R_v(0)}{\sqrt{1 + \omega^2 \tau_e^2}} \quad (2.6)$$

where $R_v(0) = I_0 R_t \alpha / G_e$ is the zero frequency responsivity, is plotted in Figure 2.4. The bolometer time constant $\tau_e$ determines the bolometer response rate ($\omega_0 = 1/\tau_e$).

The absorber and thermistor could be combined in one structure as in case of microbolomter which is a thin film resistor with a high temperature coefficient of resistance. The microbolometers were realized in different geometries in order to reduce a thermal coupling of the microbolometer to the heat sink, e.g. placing on a thin membrane [135] or making free-standing bridge bolome-
A lower thermal coupling results in a higher voltage responsivity, but simultaneously the response rate is decreasing.

The total power detector may be a very efficient radiation detector but it does not provide any spectral information. In order to perform spectrometry a narrow band-pass filter is placed at the receiver input, e.g. an interferometer. However, the size of interferometer scales with its resolution. So the maximum practical spectral resolution which might be achieved in THz range using interferometer is $\approx 10^3$.

### 2.1.2 Frequency mixing

Heterodyne receivers have some advantages over direct detection receivers. First, both amplitude and phase information are preserved. Second, a high frequency narrow band-pass filter is not required at the receiver input in order to achieve a high spectral resolution. In heterodyne receivers a down-converting mixer mixes an incident signal ($\omega_s$), which in a general case might be represented as a sum of frequency components, with a monochromatic radiation ($\omega_{LO}$) from an LO (see Fig. 2.5). The total radio frequency (RF) voltage $U(t)$ across the mixer is:

$$U(t) = U_s \cos(\omega_st) + U_{LO} \cos(\omega_{LOT})$$

(2.7)

where $U_s$ and $U_{LO}$ are amplitudes of signal and LO voltages, respectively. Bolometers with a thermistor could be used as mixing elements for heterodyne receivers. The total power dissipated in the bolometer is:

$$P(t) = \frac{U(t)^2}{2R_t}$$

(2.8)

Inserting Equation 2.7 into 2.8 and taking into account that the bolometer temperature can not follow high frequency terms $2\omega_s$, $2\omega_{LO}$ and $\omega_s + \omega_{LO}$ the

---

**Fig. 2.5:** (a) Schematic of down-converting mixer. (b) Schematic of down-conversion in a frequency domain.
total dissipated power becomes:

\[ P(t) = P_s + P_{LO} + 2\sqrt{P_s P_{LO}}\cos(\omega_{IF} t) \] (2.9)

where \( P_s = \frac{U_s^2}{2R_t} \), \( P_{LO} = \frac{U_{LO}^2}{2R_t} \), and \( \omega_{IF} = |\omega_s - \omega_{LO}| \) which should be less then \( 1/\tau_e \). As it follows from Equation 2.9 the IF output \( P_{IF} \) at a frequency \( \omega_{IF} \) can be produced by either an Upper Sideband (USB) \( \omega_s = \omega_{LO} + \omega_{IF} \) or a Lower Sideband (LSB) \( \omega_i = \omega_{LO} - \omega_{IF} \) (see Figure 2.5(b)). Mixers sensitive to both USB and LSB are called Double Sideband (DSB). The performance of mixer is characterised by a mixer conversion gain:

\[ G_m = \frac{P_{IF}}{P_s} \] (2.10)

Another important figure of merit for the mixer is noise. The mixer itself produces noise at the output with a power \( N_{out} \). This noise might be represented with the output noise temperature \( T_{out} \) using the Johnson-Nyquist equation:

\[ T_{out} = \frac{N_{out}}{k_B B} \] (2.11)

where \( k_B \) is the Boltzmann constant and \( B \) a bandwidth. Using the mixer conversion gain the output noise temperature \( T_{out} \) might be referred to the mixer input in case of DSB mixer as:

\[ T_m = \frac{T_{out}}{2G_m} \] (2.12)

A factor “2” in Equation 2.12 comes from a DSB operation of HEB mixer and an assumption that a sideband ratio is one.

2.2 Superconducting HEB mixers

The term “hot electrons” is used to describe a non-equilibrium state of electrons inside the bolometer, i.e. an effective elevation of electron temperature. The first HEB mixer was realised using a doped semiconductor indium antimonide (InSb) [134]. Despite a good sensitivity, devices based on InSb had quite small bandwidth due to the time constants of the order of micro-seconds [137]. After the discovery of electron-heating effect in superconducting films [15] superconductors emerged as a material for HEB mixers [14]. The resistance of a superconductor is strongly affected by the electron temperature in a region close to a \( T_c \), which explains the HEBs’ high sensitivity. HEB mixers made from NbN films were successfully implemented [138] allowing for the achievement of a typical bandwidth of up to 4 GHz [139].

2.2.1 Photoresponse of phonon-cooled HEB mixers

Two types of superconducting HEB mixers differing by the dominating mechanism of electron cooling were reported: phonon-cooled [14] and diffusion-cooled [140]. In a phonon-cooled HEB a thin superconducting film deposited on a substrate acts as an absorber. The film cools down through the substrate,
which plays a role of a heat sink. A thermal link between them is a thermal boundary resistance. The superconducting film acts also as a resistive thermometer. The thermalisation scheme of such a device is depicted in Figure 2.6.

In order to operate as a receiver the HEB is cooled down below its $T_c$ where a thermal coupling between phonons and electrons is week and the electron-electron interaction is strong. The interaction time between electrons $\tau_{ee}$ is shorter than other characteristic time constants, which makes possible to present the HEB as a 2-T system. The first (electron) subsystem consists of quasiparticles and has a temperature $\theta$ and a specific heat $c_e$. The second (phonon) subsystem is formed by phonons in a superconducting film and has a temperature $T_p$ and a specific heat $c_p$. The heat exchange between electron and phonon subsystems is done with characteristic time constants $\tau_{ep}$ and $\tau_{pe}$. In an equilibrium state this interaction times relates as $\tau_{pe} = \tau_{ep} c_p / c_e$ and in order to achieve electron cooling $\tau_{ep}$ should be less than $\tau_{pe}$. Then instead of one heat balance equation 2.1 a system of heat balance equations might be written as [142]:

\[
\begin{align*}
    c_e \frac{d\theta}{dt} &= P(t) - c_e \frac{\theta - T_p}{\tau_{ep}} \\
    c_p \frac{dT_p}{dt} &= c_e \frac{\theta - T_p}{\tau_{ep}} - c_p \frac{T_p - T_{bath}}{\tau_{esc}}
\end{align*}
\]

where $\tau_{esc}$ is an escape time of phonons from the superconducting film into the substrate:

\[
\tau_{esc} = \frac{4d}{\beta u}
\]

where $d$ is a superconductor thickness, $u$ a speed of sound and $\beta$ an acoustic phonon transmission coefficient. The phonon escape time $\tau_{esc}$ should be less then the electron-phonon interaction time $\tau_{ep}$ to prevent heat accumulation in the phonon subsystem. The reverse energy flow carried by the phonons from the substrate into the superconductor is neglected.
2.2. Superconducting HEB mixers

Close to the $T_c$ the electron specific heat as a function of the electron temperature is:

$$c_e(\theta) = \gamma \theta$$

(2.16)

where $\gamma$ is the electron specific heat coefficient. The phonon specific heat at an arbitrary phonon temperature in the Debye approximation is given by [143]:

$$c_p(T_p) = 9nk_B \left( \frac{T_p}{T_D} \right)^3 \int_0^{\frac{T_p}{T_D}} \frac{e^{x}x^4}{(e^{x} - 1)^2} dx$$

(2.17)

where $n$ is an atomic density and $T_D$ the Debye temperature. The phonon temperature $T_p$ is $\approx 0.9 \times \theta$ and could be estimated from the heat balance equations (Equations 2.13 and 2.14) [144].

2.2.2 The lumped element HEB model

In order to analyse the HEB behavior, lumped element model previously developed for NbN HEBs [14] can be used. The model assumes that the electron temperature along the superconducting film is uniform and RF radiation and both DC power have the same effect on the HEB. However, this assumption was not completely true and development of the hot-spot models [145–147] was required. In the hot-spot models the electron temperature profile along the superconducting film was taken into account. Compared to the standard model, modifications of the heat balance equation were done. This modifications allowed for the correct modeling of HEB noise and current versus voltage (I-V) curves, while the standard model requires experimental curves for modeling.

2.2.2.1 Conversion gain

Using standard lumped element formalism expression for the HEB voltage responsivity might be written as [148]:

$$R_v(f_{IF}) = \frac{R_LI_0}{R_L + R_0} \frac{C_0}{\chi} \frac{1}{1 - \frac{C_0 I_0^2 R_L - R_0}{R_L} 1 + \frac{i f_{IF}}{f_0}} = R_v(0) \frac{1}{1 + \frac{i f_{IF}}{f_0}}$$

(2.18)

where $R_0$ is the HEB DC resistance at the bias point, $f_0$ the HEB 3 dB gain roll-off frequency (GBW), and $C_0 = dR/dP$ ($P$ is a sum of dissipated DC and LO powers). An assumption that the impedance of a HEB at the high-frequency limit $Z(\infty)$ is equal to $R_0$ was done. For Nb HEBs it was shown that a real part of $Z(f_{IF})$ goes to $R_0$ at frequencies $>1$ GHz [149]. For MgB$_2$ HEBs a similar investigation on the IF impedance was performed recently [150]. It was shown that a real part of HEB impedance approaches differential resistance $dU/dI$ at low frequencies and $R_0$ at higher frequencies similar to NbN HEBs [151].

A power exchange function $\chi$ is introduced in a similar way as in [152]. It is defined as a ratio of the RF and DC power changes required to keep the device resistance constant. As a general rule a HEB resistance is more sensitive to a DC power then to an RF power, which results in conversion functions larger than one. It was demonstrated that $\chi$ typically takes values from 3 to 1 decaying moving to higher biases [146,151].
The mixer conversion gain is given by [148]:

\[
G_m(f_{IF}) = \frac{2P_{LO}R_L^2(f_{IF})}{R_L}
\]  

(2.19)

where \(P_{LO}\) is an absorbed LO power.

Inserting Equation 2.18 into 2.20 the mixer conversion gain predicted by the standard model is calculated as:

\[
G_m(f_{IF}) = \frac{2P_{LO}R_L I_0^2}{(R_L + R_0)^2 (1 - C_0 I_0^2 R_{L} - R_0/R_{L} + R_0)^2} \frac{1}{1 + (f_{IF}/f_g)^2} = G_m(0) \frac{1}{1 + (f_{IF}/f_g)^2}
\]  

(2.20)

where \(G_m(0)\) is a mixer conversion gain at zero IF.

Another assumption made in this theory is that the resistance of HEB depends on the electron temperature. Because the temperature is linearly proportional to the dissipated power, then \(R = C_0 P\). After some mathematical derivations it was shown that [149]:

\[
C_0 = \frac{1}{I_0^2} \frac{dU}{dI} = \frac{C'}{I_0^2}
\]  

(2.21)

where \(C'\) is a dimensionless self-heating parameter.

### 2.2.2.2 Noise temperature

The main noise sources in a HEB mixer are Johnson noise and thermal fluctuation noise [14]. Output noise temperatures \(T_J\) and \(T_{FL}\) produced by each noise component might be calculated [153] according to the Mather’s nonequilibrium theory of bolometer detector [154] as:

\[
T_J(f_{IF}) = \frac{4R_L R_0 \theta}{(R_L + R_0)^2 (1 - C_0 I_0^2 R_{L} - R_0/R_{L} + R_0)^2}
\]  

(2.22)

\[
T_{FL}(f_{IF}) = \frac{I_0^2 R_L (\frac{\partial R}{\partial \theta})^2 \frac{4 \theta^2}{c_e V \tau_{\theta}}}{(R_L + R_0)^2 (1 - C_0 I_0^2 R_{L} - R_0/R_{L} + R_0)^2} \frac{1}{1 + (2\pi f_{IF} \tau_{\theta}^*)^2}
\]  

(2.23)

where \(V\) is the HEB volume and \(\tau_{\theta}^*\) the electron temperature relaxation time modified by the electro-thermal feedback:

\[
\tau_{\theta}^* = \frac{\tau_{\theta}}{1 - C_0 I_0^2 R_{L} - R_0/R_{L} + R_0}
\]  

(2.24)

The DSB mixer input noise temperature which also includes noise from the IF chain \(T_{IF}\) is [153]:

\[
T_m(f_{IF}) = \frac{T_J + T_{FL} + T_{IF}}{2G_m(0)(1 + (f_{IF}/f_g)^2)^{-1}}
\]  

(2.25)

The thermal fluctuation noise depends on the IF as \((1 + (2\pi f_{IF} \tau_{\theta}^*)^2)^{-1}\). Since \(\tau_{\theta}^*\) and a mixer time constant \(\tau_{mix} = (2\pi f_g)^{-1}\) basically are equal, Equation 2.25 could be rewritten as:

\[
T_m(f_{IF}) = \frac{T_{FL}(0) + (T_J + T_{IF}) (1 + (f_{IF}/f_g)^2)}{2G_m(0)}
\]  

(2.26)
2.2. Superconducting HEB mixers

And then defining a new parameter $f_n$ as a mixer NBW:

$$f_n = f_g \sqrt{\frac{T_{FL} + T_J + T_{LNA}}{T_J + T_{LNA}}}$$  \hspace{2cm} (2.27)

the final equation becomes:

$$T_m(f_{IF}) = T_m(0) \, (1 + \left(\frac{f_{IF}}{f_n}\right)^2)$$  \hspace{2cm} (2.28)

where $T_m(0)$ is a mixer noise temperature at zero IF. It should be noted that according Equation 2.27 $f_n$ is always larger then $f_g$, because the radicand is larger than 1 (see Figure 2.7).

2.2.3 Two-temperature model

In the low temperature limit when $c_e$ is much larger then $c_p$ the electron temperature relaxation could be described with a single time constant $\tau_\theta$ [155]:

$$\tau_\theta = \tau_{ep} + \tau_{esc} \frac{c_e}{c_p}$$  \hspace{2cm} (2.29)

while in a general case a relation between $\tau_\theta$, $\tau_{ep}$ and $\tau_{esc}$ is more complicated.

A two-temperature approach (2-T model) was used in order to describe the response of superconducting films to a modulated electro-magnetic radiation [142]. Taking into account the effect of self-heating electrothermal feedback [156] the HEB conversion gain as a function of IF is [124]:

$$G_m(f_{IF}) \propto \left| \frac{C'}{\xi(f_{IF}) - \frac{C' R_L - R_0}{R_L + R_0}} \right|^2$$  \hspace{2cm} (2.30)

where

$$\xi(\omega) = \frac{(1 + j \omega \tau_1)(1 + j \omega \tau_2)}{(1 + j \omega \tau_0)}$$  \hspace{2cm} (2.31)
\( \tau^{-1}_{3} = \tau_{esc}^{-1} + \tau_{ep}^{-1} \frac{C_e}{C_p} \) \hfill (2.32)

\[ \tau^{-1}_{1,2} = \frac{\tau_{3}^{-1} + \tau_{ep}^{-1}}{2} \left[ 1 \pm \sqrt{1 - 4\left(\frac{\tau_{3}^{-1} + \tau_{ep}^{-1}}{\tau_{esc} \tau_{ep}}\right)^{-2}} \right] \] \hfill (2.33)

However, simplified Equation 2.29 gives a good understanding of a trade-off in HEB mixer development. As it is seen from Equation 2.15 it is required to reduce the film thickness to achieve the shorter phonon escape time. Unfortunately, reduction of film thickness leads to decrease of \( T_c \), i.e. due to a large amount of defects in a film bottom layer. NbN with a bulk \( T_c \) of 16 K has only a 8–11 K \( T_c \) in 3–5 nm films. The reduction of \( T_c \) consequently leads to an increase of electron-phonon interaction time.

### 2.3 THz heterodyne receivers design

The HEB itself operates just as a mixing element. In order to use HEB in a heterodyne receiver the problem of effective signal and LO radiation coupling...
2.3. THz heterodyne receivers design

Fig. 2.9: Integrated planar antennas. (a) Double dipole antenna. Illustration from [157]. (b) Double slot antenna. Illustration from [98]. (c) Slot-ring antenna. Illustration from [158]. (d) Log-periodic antenna. Illustration from [159]. (e) Spiral antenna. Illustration from [97].

into device, DC biasing and IF signal redout should be solved. There are two main approaches for the receiver design that differ by the manner radiation is coupled into the device: waveguide coupling and quasi-optical coupling.

In the waveguide coupling approach a feed horn antenna (see Figure 2.8(a)) is used for radiation coupling from the free space into a machined waveguide with a mounted device (see Figure 2.8(b)). The HEBs integrated with a probe antenna are typically fabricated on thin substrates. The tunable element (backshort) could be used to maximize radiation coupling from the waveguide into the device (see Figure 2.8(c)). The optimal frequency range for radiation coupling for the waveguide receiver is defined by the antenna and waveguide geometry. The drawback of this receiver type is that the waveguide dimensions scale down for higher frequencies and fabrication becomes more challenging. High frequency operation also necessitates a reduction of substrate thickness due to increasing waveguide losses and substrate modes formation. However, waveguide HEB mixers have been successfully developed for frequencies up to 4.7 THz [19,31,33,111,115]. In waveguide receivers axial and lateral positions of the mixer beam are determined only by the feed horn antenna (i.e. by the machining tolerances only). However, the mixer chip mounting in the correct position for maximum coupling could be challenging. Using waveguide approach it is possible to avoid thin film beam splitter utilization for combining signal and LO radiation. The balanced scheme used to improve receiver stability could be realized easily using built in machined hybrid coupler as shown in Figure 2.8(d) [111].

In the quasi-optical coupling approach a lithographic planar antenna directly integrated with a HEB is used. Figure 2.9 demonstrates several types of integrated planar antennas used with HEB mixers, e.g. a double dipole an-
Fig. 2.10: (a) Quasi-optical mixer block used for HIFI instrument of The Hershel Space Observatory. (b) Elliptical dielectric lens with a planar antenna integrated HEB mixer attached. Illustration from [98].

tenna [157], a double slot antenna [98], a slot-ring antenna [158], a log-periodic antenna [159] and a spiral antenna [97]. The spiral antenna is a good choice for a laboratory study of devices at different LO frequencies, because it has a constant real impedance in a broad frequency range. The impedance of a HEB can be easily matched to the antenna impedance by choosing the right HEB geometry. Unfortunately, real spiral antennas have an elliptical polarization, while the radiation of LO source are typically linear polarized. That results in LO coupling losses (at least 50%) and complexity of loss estimation of a beam splitter used for combining signal and LO radiation.

For a planar antenna on a dielectric substrate coupling into the substrate is \( \epsilon^{3/2} \) times (\( \epsilon \) is the dielectric substrate permittivity) higher than into the air. The incoming radiation then should be fed from the substrate side. In this case the radiation propagating at the angles larger than the critical angle will be trapped in the substrate, so an additional beam handling is required. In order to avoid this problem, hyperhemispherical and elliptical dielectric lenses are typically used [160]. The planar antenna integrated HEB mixer is attached to the back side of the lens and packed in a mixer block (see Figure 2.10). The antenna gain in case of hyperhemispherical lens is increased by \( n_l^2 \) \( (n_l \) is the lens dielectric refractive index). In practice, hyperhemispherical and elliptical lenses can be realized approximately by using a hemispherical lens and a dielectric plate of required thickness placed between the hemisphere and the substrate. Use of lenses results in losses caused by the reflection of radiation at the lens/air interface. Reflection losses could be reduced by applying antireflection coating [161]. Application of Parylene C antireflection coating allows for reduction of the reflection loses from 1 dB to 0.2 dB [93].
Chapter 3

MgB$_2$ superconducting ultrathin films

In this chapter the detailed description of HPCVD method, the deposition system design, and the study of achieved films presented in [Paper C] and [Paper D] are summarized.

3.1 MgB$_2$ thin films

In order to increase operation temperature and to improve IF bandwidth of HEB mixers, superconducting materials with a higher $T_c$, which can provide a shorter electron-phonon interaction time are required. MgB$_2$ is one of these materials. Thinner films provide shorter phonon escape time from the film into the substrate, which is another important limitation for the HEB mixers IF bandwidth. Hence, both high $T_c$ and small thickness superconducting films are desirable. The superconductivity in MgB$_2$ was reported in 2001 [127]. MgB$_2$ is a conventional intermetallic compound superconductor with the highest $T_c$ for a traditional phonon mediated superconductor of 39 K reported so far. The crystalline structure of MgB$_2$ is shown in Figure 3.1. It consists of hexagonal magnesium (Mg) layers and honeycomb boron (B) layers in-between. The hexagonal unit cell has the following lattice parameters $a = b = 3.086\, \text{Å}$, $c = 3.524\, \text{Å}$ [127]. Despite MgB$_2$ is a conventional Bardeen-Cooper-Schrieffer (BCS) superconductor, it exhibits a double superconducting gap structure with $2\Delta_{\sigma} \approx 4k_B T_c$ and $2\Delta_{\pi} \approx 1.3k_B T_c$ [162]. In the dirty limit, due to strong interband and intraband scattering two superconducting gaps merge into one energy gap $2\Delta_{\text{dirty}}$ whose temperature dependance deviates from curve predicted by BCS theory [163]. A penetration depth ($\lambda_L$) of 34.5 nm and coherence length ($\xi$) of 8 nm were reported for MgB$_2$ [164,165]. Using the Ginzburg-Landau formula for the depairing current density $J_d = \Phi_0/(\sqrt{3}\pi\mu_0\lambda_L^2\xi)$, where $\Phi_0$ is the flux quantum and $\mu_0$ the permeability of vacuum, it is estimated to be $\approx 3 \times 10^9 \, \text{A/cm}^2$.

The discovery of superconductivity in MgB$_2$ immediately brought a great interest to MgB$_2$ thin films [128,166,167]. Several techniques for in-situ thin film growth were proposed, e.g. pulsed laser deposition (PLD) [128], MBE
Chapter 3. MgB$_2$ superconducting ultrathin films

Fig. 3.1: MgB$_2$ crystal structure. Honeycomb boron layers are in between of hexagonal magnesium layers [127].

Fig. 3.2: Comparison of different MgB$_2$ thin film deposition techniques: MBE [174], co-evaporation [175], and HPCVD [172,176,177]. Illustration from Ref. [177].

[168], HPCVD [129], sputtering [169], e-beam and thermal co-evaporation [170]. The HPCVD grown MgB$_2$ films have a higher $T_c$ compared to films with the same thickness grown by other techniques (see Figure 3.2). Unfortunately, deposition systems utilizing HPCVD method are not commercially available.

The most suitable substrates for MgB$_2$ thin film deposition are Al$_2$O$_3$ and SiC with a lattice mismatch with MgB$_2$ of $\sim$11% (30° in-plane rotation) [171] and $\sim$0.42% [172], respectively. SiC is a more preferable substrate for MgB$_2$ thin film deposition due to a better film/substrate lattice match which results in a reduced number of defects in bottom layers of the film. This leads to a better phonon transparency of the film/substrate interface. It should be also noted, that both thermodynamic calculations [173] and experimental results [129] show that layers of magnesium oxide (MgO) form at the film/substrate interface, when Al$_2$O$_3$ substrates are used. More common substrates for microelectronics industry, such as Si and silicon dioxide (SiO$_2$), react with Mg to form silicides [173] and therefore require the use of appropriate buffer layers.

Significant progress in ultrathin MgB$_2$ film deposition allowed for fabri-
3.2 Chalmers HPCVD system

Initial studies of MgB$_2$ HEB mixers were performed using MBE grown films on c-cut Al$_2$O$_3$ substrates provided by NTT Basic Research Laboratories [181]. Typically, the $T_c$ of MBE grown films is much lower than for HPCVD grown films, but the film surface is smoother, which is essential for the device fabrication and performance. The film deposition process included co-evaporation of Mg and B in a high-vacuum chamber at 280°C and subsequent Ar atmosphere annealing in a rapid-annealing furnace. Films were covered *in-situ* with a 20 nm Au layer to reduce contact resistance between a MgB$_2$ film and metal layers deposited during device fabrication and to prevent film degradation during storage and initial device fabrication steps. A HPCVD method developed
for MgB$_2$ thin film growth can provide high quality ultrathin superconducting films that can maintain a high $T_c$ even when few nanometers thick. On the other hand, the availability of in-house source of thin films is of a great advantage for device development. Therefore, a custom made HPCVD system was constructed at Chalmers University of Technology for MgB$_2$ ultrathin film deposition as a part of the project on MgB$_2$ HEB mixers development.

3.2.1 System design

The HPCVD technique utilizing a combination of both physical and chemical vapor deposition was proposed specifically for MgB$_2$ thin film growth. The Mg source is an evaporative flux from solid Mg and the B source is a diborane ($\text{B}_2\text{H}_6$) gas. In brief, in this process both the Mg pellets and the substrate are placed on a heater (either resistive or inductive) while a mixture of hydrogen ($\text{H}_2$) and $\text{B}_2\text{H}_6$ gases is supplied into the chamber as shown in Figure 3.3(a). The $\text{B}_2\text{H}_6$ gas decomposes above the heated substrate into borane ($\text{BH}_3$) gas. The borane molecules are adsorbed on the substrate surface and react with evaporated Mg to form an MgB$_2$ film. The film growth usually occurs at temperatures ranging from 650°C to 760°C [129,133,172,182], which is above the Mg melting point of 650°C (the area marked with a red oval in Figure 3.3(b)). As one can see, in order to form the correct crystalline phase (MgB$_2$) both the Mg partial pressure and the temperature should fall in a quite tight area in the phase diagram. This necessitate very fine tuning of deposition parameters.

The system photos are presented in Figure 3.4. $\text{H}_2$, $\text{B}_2\text{H}_6$ (5% diluted in $\text{H}_2$), and purging nitrogen ($\text{N}_2$) gases are supplied to the deposition chamber using a computer controlled gas panel consisting of pneumatic valves and mass-flow controllers (see Figure 3.4(a)). A pirani gauge is mounted on the deposition chamber to monitor the pressure during system pumping. A throttle valve operated through a controller with a capacitance manometer is used to set the desired process pressure. A kinetic trap (see Figure 3.4(c)) after the deposition chamber is installed in order to protect following system components from residuals of the deposited material carried by the gas flow. A fore-vacuum pump and a scrubber used for $\text{B}_2\text{H}_6$ disposal are placed behind a main cabinet in an utility room (see Figure 3.4(d)).

A schematic of the MgB$_2$ HPCVD system chamber is presented in Figure 3.3(a). A quartz tube prevents material deposition on water cooled chamber metal walls. Both the substrate and pieces of solid Mg are placed on a heater. A coaxial heating wire is clamped between an upper and a bottom parts of the heater under an area where magnesium is placed (see Figure 3.4(b)). In contrast to the previously presented resistive heater designs the coaxial wire itself is hidden inside the heater, which reduces contamination of the wire during depositions and increases the heater life time. Due to a temperature gradient the temperature of the central part where the substrate is placed is 50 K lower than under Mg pellets. A thermocouple is attached to the bottom part of the heater to monitor the temperature during the deposition process.

The MgB$_2$ thin film deposition procedure is following:

1. The chamber is pumped to the base pressure (10$^{-3}$ Torr).
Fig. 3.4: Chalmers in-house built MgB$_2$ HPCVD system. (a) Top part front view. (b) Deposition chamber inside view. (c) Bottom part front view. (d) The utility room view.
Chapter 3. MgB$_2$ superconducting ultrathin films

Fig. 3.5: MgB$_2$ film resistance measured on 5×5 mm$^2$ size test wafers (SiC) versus deposition mass. Films are deposited at either 20 Torr or 40 Torr.

2. The chamber is flushed with H$_2$ gas and pumped again to the base pressure.

3. The chamber is filled with H$_2$ gas (400 sccm) to the desired pressure (typically 20 Torr).

4. Solid Mg and the substrate are heated to about 700°C.

5. The B$_2$H$_6$ gas mixture is turned on for the desired time.

6. After the deposition is finished the heater is turned off and the substrate is cooled down.

7. The chamber is flushed several times with N$_2$ gas in order to remove possible remaining B$_2$H$_6$ gas.

3.2.2 Safety

During the HPCVD deposition system design and construction several safety issues had to be solved. The gases used in the system are dangerous for the personnel and laboratory environment. The gas panel, the deposition chamber, and other main system components are placed inside the ventilated cabinet. Furthermore, the gas panel is covered with a metal shield and has additional ventilation exhaust with a higher flow to form a negative pressure difference in case of a gas leakage. The cabinet doors have switches connected to an inter-lock system preventing process gases supply when doors are opened. The output of the pressure controller is also connected to the inter-lock system such as gas supply is possible only if the pressure inside the deposition chamber is below 300 Torr.

B$_2$H$_6$ is a pyrophoric gas and can self-inflame even at a room temperature. Moreover, B$_2$H$_6$ has a toxic effect primarily due to its irritant properties. In
3.3 HPCVD grown ultrathin films

In the HPCVD process film thickness is defined by a \( \text{B}_2\text{H}_6 \) flow rate and a deposition time. As a measure of the deposited material amount a product of the \( \text{B}_2\text{H}_6 \) flow rate and the deposition time, so called deposition mass, can be used. Immediately after the chamber is opened, resistance of the deposited film is measured using multimeter from corner to corner of the substrate. The resistance was found to be inversely proportional to the deposition mass over two orders of magnitude, which suggests a good connectivity of the obtained films. Initially, \( \text{MgB}_2 \) thin films were grown on \( \text{Al}_2\text{O}_3 \) substrates. Even the first film deposition using the newly built system was successful, and film with a \( T_c \) of 34 K was achieved (see Figure 3.6(a)). A \( T_c \) of grown films ranged from 33 K (15 nm) to 37 K (40 nm) with a distinct double transition for thinner films. The film surface was covered with lots of spots and particles (see Figure 3.6(a)).

### Table 3.1: HPCVD \( \text{MgB}_2 \) HEB thickness (d), size (W×L), critical temperature (\( T_c \)), resistance at room temperature (\( R_{295 K} \)), resistivity (\( \rho_{295 K} \)), and critical current density (\( J_c \))

<table>
<thead>
<tr>
<th>Device</th>
<th>d(nm)</th>
<th>( W\times L ) (( \mu\text{m}^2 ))</th>
<th>( T_c ) (K)</th>
<th>( R_{295K} ) (( \Omega ))</th>
<th>( \rho_{295K} ) (( \mu\Omega \times \text{cm} ))</th>
<th>( J_c ) (10(^7) A/cm(^2))</th>
</tr>
</thead>
<tbody>
<tr>
<td>E2-1</td>
<td>30</td>
<td>1×1</td>
<td>39.6</td>
<td>39</td>
<td>117</td>
<td>8.8</td>
</tr>
<tr>
<td>E2-2</td>
<td>30</td>
<td>1×1</td>
<td>39.4</td>
<td>40</td>
<td>120</td>
<td>11.0</td>
</tr>
<tr>
<td>E3-2</td>
<td>20</td>
<td>0.5×0.5</td>
<td>38.6</td>
<td>25</td>
<td>50</td>
<td>10.5</td>
</tr>
<tr>
<td>E3-8</td>
<td>20</td>
<td>0.8×0.8</td>
<td>39.2</td>
<td>20</td>
<td>40</td>
<td>12.0</td>
</tr>
<tr>
<td>E6-4</td>
<td>12</td>
<td>1×1</td>
<td>33.5</td>
<td>44</td>
<td>53</td>
<td>2.0</td>
</tr>
<tr>
<td>E6-7</td>
<td>12</td>
<td>1×1.5</td>
<td>34.5</td>
<td>67</td>
<td>54</td>
<td>2.9</td>
</tr>
<tr>
<td>E8-2</td>
<td>10</td>
<td>0.3×0.3</td>
<td>34.0</td>
<td>52</td>
<td>52</td>
<td>2.5</td>
</tr>
<tr>
<td>E8-7</td>
<td>10</td>
<td>0.5×0.5</td>
<td>32.5</td>
<td>87</td>
<td>87</td>
<td>1.2</td>
</tr>
<tr>
<td>E10-7</td>
<td>8</td>
<td>1×1</td>
<td>30.0</td>
<td>196</td>
<td>157</td>
<td>0.9</td>
</tr>
<tr>
<td>E10-8</td>
<td>8</td>
<td>1×1</td>
<td>31.0</td>
<td>230</td>
<td>182</td>
<td>1.2</td>
</tr>
<tr>
<td>E15-7</td>
<td>5</td>
<td>1×1</td>
<td>32.5</td>
<td>130</td>
<td>65</td>
<td>2.8</td>
</tr>
</tbody>
</table>

order to avoid an exposure of laboratory environment to \( \text{B}_2\text{H}_6 \), which is highly undesirable, a remotely controlled bypass line with a \( \text{B}_2\text{H}_6 \) gas sensor was installed after the fore-vacuum pump (see Figure 3.4(d)). After the completion of film deposition procedure the system exhaust is switched to the bypass to make sure there is no \( \text{B}_2\text{H}_6 \) gas left in the chamber. The inter-lock system prevents switching to the bypass during the deposition process.

\( \text{H}_2 \) is a flammable gas and can self-explode in a certain concentration with oxygen (\( \text{O}_2 \)). \( \text{H}_2 \) gas cleaned from \( \text{B}_2\text{H}_6 \) is mixed at the scrubber exhaust with \( \text{N}_2 \) to prevent formation of explosive concentrations of the oxyhydrogen. Another \( \text{N}_2 \) gas line is connected to an oil return inlet of the fore-vacuum pump in order to avoid accumulation of \( \text{H}_2 \) in the pump oil. The pump \( \text{N}_2 \) gas line has a lower flow and is always turned on, while the exhaust \( \text{N}_2 \) gas line with a higher gas flow is turned on only during the HPCVD system operation. The \( \text{N}_2 \) gas flows are controlled with gas flow meters which are also connected to the inter-lock system.
Fig. 3.6: First HPCVD grown MgB$_2$ films on Al$_2$O$_3$ substrates deposited at Chalmers University (20 sccm, 120 s, 40 Torr). (a) The resistance versus temperature curve for the first film. (b) SEM image of the second film. (c) High magnification SEM image of the second film.
3.3. HPCVD grown ultrathin films

HPCVD films are assumed to grow in a Volmer-Weber mode and large (300 nm in diameter) hexagonal crystallites corresponding to the MgB$_2$ unit cell are clearly distinguishable in scanning electron microscope (SEM) image (see Figure 3.6(c)). For MgB$_2$ films on Al$_2$O$_3$ substrates the residual resistance ratio (RRR = $R_{295 K}/R_{ons}$, where $R_{295 K}$ is the room temperature resistance and $R_{ons}$ the onset resistance) was 1.5–2.5 suggesting a high defect concentration. The RRR values are much lower than value (about 10) reported previously for clean MgB$_2$ films [133].

Further deposition process development and optimisation were performed using SiC substrates. The discussed films have a $T_c$ ranging from 35 K (5 nm thick) to 41 K (30 nm thick) (see Figure 3.7(a)). The RRR of the films is ranging from 2 to 6 indicating an improvement of film quality. The film surface was also studied with atomic force microscope (AFM). The measured mean square roughness (see Figure 3.8(d)) was about 1 nm, which is lower than for previously reported HPCVD as grown ultrathin MgB$_2$ films [183]. A low roughness is one of the key characteristics affecting fabrication of micro- and nanostructures in thin films. We observed that reduction of the deposition pressure from 80 Torr to 20 Torr continuously leads to smoother film surfaces. For deposition pressures above 30 Torr a droplet formation occurs in the deposition chamber resulting in rougher films. Therefore, most of the discussed films used for HEB fabrication were grown at a pressure of 20 Torr. Film epitaxial growth is confirmed by both the transmission electron microscope image (see Figure 3.8(b)) and MgB$_2$ epitaxial response in X-ray diffractometer (XRD) scan (see Figure 3.8(c)).

Film DC parameters in patterned microstructures were studied in several batches of HEBs fabricated using either ultraviolet (UV) or electron beam (e-beam) lithography based process (see Chapter 4). Summary of DC measurement results for devices selected for THz characterisation are summarised in Table 3.1. MgB$_2$ films were covered with a 20 nm gold (Au) layer using magnetron sputtering directly after the deposition. This Au layer was used both to protect the deposited film from degradation in the atmosphere as well as
to be able to use the same fabrication process previously developed for HEBs made from MBE grown films [Paper A], [Paper B]. For batches E1-E8 a 2 nm thick Ti layer was deposited prior the 20 nm Au layer deposition to improve a layer adhesion. Since batch E9 the in-situ precleaning with argon plasma was used to remove the native oxide, improve the Au layer adhesion, and reduce contact resistance. There was no Ti layer used in the last case.

There are several tools to measure the conductive film thickness: contact and optical surface profilometers, AFM, TEM, ellipsometer, etc. Ellipsometry is a non-invasive method, however it requires preliminary knowledge of the MgB$_2$ film optical properties. Initially, for the deposition process development, film thickness was measured both with a contact profilometer and an AFM on MgB$_2$ films etched away on a fraction of the substrate using a hydrochloric (HCl) acid. Later, selected samples have been also studied using TEM to investigate the film/substrate interface as well as to measure MgB$_2$ film thickness. All thicknesses presented in Table 3.1 were confirmed with TEM measurements, except for device E2-2 for which it was estimated from the deposition rate.
3.3. HPCVD grown ultrathin films

Fig. 3.9: Critical temperature and critical current density versus resistivity measured for the devices (a) from the same batch and (b) from batches of various thickness.

At room temperature sheet resistance of unpatterned films was measured with a four-point probe technique. Then by knowing the film thickness from TEM measurements the room temperature resistivity was calculated both for unpatterned films and for microstructures. These values correspond to the previously published resistivity values for films of similar thickness [180, 183–185]. The resistivity obtained from resistance of submicron size bridges (see Table 3.1) was ranging from $50 \, \mu \Omega \text{cm}$ (for a 20 nm thick film) till $182 \, \mu \Omega \text{cm}$ (for a 8 nm thick film). It is a factor of 2 higher than e.g. in Ref. [184] and [185], but much smaller bridges have been used. The high resistivity of the 30 nm thick film could be explained by a higher (40 Torr) deposition pressure, while the origin of the low resistivity in the 5 nm thick film is unclear.

The film resistivity affects design of HEB mixers. In order to provide the best performance, the impedance of HEB should be matched to the impedance of the integrated planar antenna (in our case a 100 Ω spiral antenna). With a resistivity of about 50–100 $\mu \Omega \text{cm}$ the aspect ratio of HEB (width/length) should be less than 1. Together with a requirement keeping a bolometer area small (due a limited available LO power) it will lead to the reduction of bolometer width in the design (in comparison to HEB mixers made from MBE grown MgB$_2$ films [Paper A], [Paper B]). That will increase the contact resistance between the HEB and the metal antenna, which subsequently increases the noise temperature.

In order to better understand the nature of the increased resistivity in thin films, the critical current density ($J_c$) has to be discussed. Whereas a $T_c$ for thicker films remains the same in microbridges, for films thinner than 10 nm a $T_c$ is reduces by a few degrees. Nevertheless, all films show excellent superconducting transition. The $J_c$ values obtained from I-V characteristics of fabricated devices are presented in Table 3.1. For the 30 nm and 20 nm thick films the $J_c$ is about $1 \times 10^8$ A/cm$^2$ (at 4.2K), hence is one of the highest $J_c$ reported so far for MgB$_2$ thin films. ($\approx$10% of the depairing current). Even for films thinner than 10 nm the $J_c$ is $(1-3) \times 10^7$ A/cm$^2$. The same or higher resistivity and $J_c$ of our films can possibly be explained by the lower deposition
rate in the discussed HPCVD system as compared to [184], which facilitate more uniform and homogenies MgB$_2$ film growth [186].

As mentioned above the $J_c$ in submicron size bridges made from films thinner than 10 nm is lower than for thicker films. However, it is approximately a factor of 10 higher than for the previously reported microbridges made from MBE and HPCVD grown MgB$_2$ films. The high yield (above 75%) allowed for the study of correlation between the resistivity and the $J_c$ of the submicron size bridges made from the same 10 nm thick film (see Figure 3.9(a)). The lower resistivity corresponds to the higher $J_c$. The same correlation is observed also for the $T_c$ measured in submicron size bridges after the fabrication (see Figure 3.9(a)). The spread of parameters suggests that the 10 nm film is quite inhomogenies over the substrate area. The same dependance (see Figure 3.9(b)) of $T_c$ and $J_c$ on resistivity is observed for the devices made from films of various thickness (Table 3.1).

### 3.4 Films thinning down using Ar$^+$ ion beam milling

Recently, argon ion (Ar$^+$) beam milling was proposed as a technique for achieving ultrathin MgB$_2$ film from initially grown thicker films [180, 184, 185]. In order to study the effect of a thinning down on our HPCVD grown MgB$_2$ films, three films of various thickness were grown. The films were deposited with the same deposition parameters (20 Torr, 120 s) except $B_2H_6$ gas flows: Film A (5 sccm), Film B (10 sccm), and Films C (20 sccm). The etching utilizing Oxford Ionfab 300 Ion Beam System (2 sccm Ar gas flow, 13 mA beam current, 350 V beam voltage, and 30°tilt) was performed in several steps with sheet resistance measurements between them. Three steps with a duration of 2 min each followed by three steps with a duration of 10 min each. The film sheet resistance was measured with the four-point probe technique (see Figure 3.10: Sheet resistance measured using four-point probe technique versus etching time. Deposition time and deposition pressure are 120 s and 20 Torr, respectively.)
3.4. Films thinning down using $\text{Ar}^+$ ion beam milling

Due to the higher deposition mass, Film C should be approximately twice thicker than Film B and approximately four times thicker than Film A. Film B and Film C reach the same sheet resistance as Film A after approximately 20 min and 40 min of milling, respectively. Film A has completely gone after about 16–20 min of etching. The dependence of sheet resistance on etching time suggests that expected relations between film thicknesses based on the gas flows is correct.

Assuming that both the film resistivity and the etching rate are constant along the film vertical profile the sheet resistance is $R_s = \frac{r}{(d-\rho t)}$, where $r$ is the etching rate, and $t$ is the etching time. Fit to the experimental data gives the etching rate of 1–1.2 nm/min. This value corresponds to the etching rate observed during HEB fabrication. Film thicknesses for Film A, Film B, and Film C used for fitting are 20 nm, 40 nm, and 60 nm, respectively, and close to the values estimated using the deposition mass. It is still of a great interest how the milling will affect film homogeneity, film surface, and submicron structures in HPCVD grown MgB$_2$ films.
Chapter 3. \textit{MgB}_2 superconducting ultrathin films
Chapter 4

MgB$_2$ HEB design and fabrication

Several batches of submicron and micrometer scale HEBs were fabricated from superconducting MgB$_2$ films grown by either MBE or HPCVD. An e-beam lithography based fabrication process was used for submicron size devices designed for noise performance characterisation, which is sensitive to the limited available LO power. For GBW characterisation micrometer scale devices were fabricated using UV lithography based process. Since GBW measurements are performed at lower frequencies (more LO power is available) and elevated bath temperatures (less LO power is needed), large size devices are acceptable.

In this chapter, the detailed description of device fabrication processes is presented.

4.1 E-beam lithography based process

The HEBs were fabricated using superconducting MgB$_2$ films either provided by NTT Basic Research Laboratories (MBE grown films) or deposited at Chalmers University of Technology (HPCVD grown films). The HEB chip design is shown in Figure 4.1. A broadband spiral antenna was chosen as the most suitable antenna type for HEB characterisation since the same device could be tested at various frequencies.

The fabrication of devices from MBE grown films was challenging. The bolometer high frequency impedance should be close to the spiral antenna impedance of 90 $\Omega$ in order to provide high efficiency coupling of THz radiation. Due to the high resistance of used MBE grown MgB$_2$ films ($\approx$ 1000 $\Omega/\square$ for 20 nm thick films) the bolometer should be short and wide to fulfill this requirement. A desirable aspect ratio is about 10:1, e.g. a 2 $\mu$m wide bolometer should be 0.2 $\mu$m in length. For such tasks the e-beam lithography allows pattern transfer with feature size down to 5 nm and provides more flexibility than projection UV lithography. In addition, since MgB$_2$ degrades during exposure to water and oxygen [187,188], some kind of protection to preserve the quality of MgB$_2$ films during the processing should be considered, e.g. a SiN$_x$ or SiO$_2$ passivation layer. The fabrication procedure developed for MBE grown MgB$_2$
films was also used for the fabrication of devices down to 0.3 μm in size from HPCVD grown films.

The fabrication procedure utilizing e-beam lithography, Ar+ ion beam milling and lift-off process includes the following steps:

1. **Alignment marks and chip frames**: Initially, alignment marks for pattern alignment at subsequent processing steps and chip frames are fabricated. After the e-beam lithography, metal evaporation (10 nm titanium (Ti), 150 nm Au, and 30 nm Ti) and lift-off are performed (see Figure 4.2(a)). The chip frame is used both for short circuiting of bolometers and avoiding possible device damaging by the electrostatic charge; and cutting lines definition for the wafer dicing. The top Ti layer is used to protect structures during Ar+ ion beam milling steps.

2. **Contact pads**: Contact pads defining the bolometer length are patterned. After the e-beam lithography, metal evaporation (10 nm Ti, 100 nm Au, and 60 nm Ti) and lift-off are performed (see Figure 4.2(b)). The top Ti layer is used to protect structures during Ar+ ion beam milling steps.

3. **Spiral antenna**: The broadband planar spiral antenna is patterned. The antenna center part is overlapping with contact pads. After the e-beam lithography, metal evaporation (10 nm Ti, 270 nm Au, and 70 nm Ti) and lift-off are performed (see Figure 4.2(c)). The top Ti layer is used to protect structures during Ar+ ion beam milling steps.

4. **Thin Au layer removal and passivation**: The 20 nm thick protective Au layer was etched away using Ar+ ion beam milling (see Figure 4.2(d)). To prevent the degradation of the MgB2 film during the rest of processing steps, immediately after the etching, the wafer was passivated with 40 nm thick SiNx film by RF magnetron sputtering process (see Figure 4.2(e)).
Fig. 4.2: Fabrication process sequence using e-beam lithography. (a) Alignment marks. (b) Contact pads. (c) Spiral antenna. (d) Thin Au layer removal. (e) Passivation with SiN$_x$. (f) Bolometer width patterning. (g) Ar$^+$ ion beam milling with a resist mask. (h) Final device.
Chapter 4. MgB$_2$ HEB design and fabrication

Fig. 4.3: SEM images of MgB$_2$ HEB made using e-beam lithography based fabrication process.

5. **Width definition and etching**: For the bolometer width definition etching mask was patterned using negative e-beam resist (see Figure 4.2(f)). The SiN$_x$ passivation and MgB$_2$ film were etched away except from the bolometer area protected by the resist (see Figure 4.2(g)).

6. **Dicing**: Finally, the wafer covered for mechanical protection with photoresist was cut into 1.5×3.3 mm$^2$ chips with the diamond dicing saw along the frame lines and washed in acetone to remove resist residuals (see Figure 4.2(h)).

The SEM image of the device fabricated using e-beam lithography based process is presented in Figure 4.3. The SEM picture in the inset of Figure 4.3 was done during the preparation of one of the samples for TEM analysis.

### 4.2 UV lithography based process

In order to acquire information about film parameters in microstructure during HPCVD process optimization faster, the UV lithography based process was used for HEB fabrication. Compared to the approximately one week required for fabrication when e-beam based process is applied, just 1-2 days are needed for UV lithography based process which involves less steps. The fabrication sequence is as following:

1. **HEB length definition**: Initially, the bolometer length and alignment marks are defined with an image reversal photoresist which provides negative slope profile (see Figure 4.4(a)). The patterning was followed by metal evaporation (10 nm Ti, 270 nm Au) and lift-off steps (see Figure 4.4(b)).
Fig. 4.4: Fabrication process sequence using UV lithography. (a) HEB length definition with resist. (b) Lift-off process. (c) Thin Au layer removal. (d) HEB width and spiral antenna definition with resist. (e) Ar\(^+\) ion beam milling with a resist mask. (f) Final device.
2. **Thin Au layer removal**: At this stage the 20 nm thick protective Au layer was etched away using Ar$^+$ ion beam milling (see Figure 4.4(c)).

3. **Spiral antenna definition**: Next, the spiral antenna with the inner part corresponding to the bolometer width and chip frames were patterned with positive photoresist (see Figure 4.4(d)). Then the developed photoresist was used as an etching mask for Ar$^+$ ion beam milling. The metal and MgB$_2$ layers were etched away down to the substrate (see Figure 4.4(e)).

4. **Dicing**: Finally, the wafer covered with photoresist for mechanical protection was cut into 1.3$\times$3.5 mm$^2$ chips with the diamond dicing saw along the frame lines and washed in acetone to remove resist residuals (see Figure 4.4(f)).

The SEM image of the device fabricated using UV lithography based process is presented in Figure 4.5. The UV lithography does not allow for features below 1 µm in size, so such the devices were used mostly for DC characterisation and heterodyne mixing experiments. The HPCVD grown MgB$_2$ films have lower resistance (50–200 Ω/□ for 5–10 nm thick films) compared to MBE grown films, so the required aspect ratio of device dimensions is about 1:1. The available LO power is limiting the maximum width of our HEBs to couple of microns. From another side fabrication of narrow HEBs is not desirable due to a higher contact resistance. As a result, low noise MgB$_2$ HEB mixers could be fabricated using UV lithography based process in most of the cases. However, extra fabrication step for bolometer microbridge passivation is required in order to improve device robustness.
Chapter 5

HEB mixers characterisation techniques

In order to characterise HEB mixers, fabricated chips have to be placed in a complex measurement setup which provides cooling to cryogenic temperatures, effective coupling of signal and LO radiation, voltage biasing, and readout of IF signal. The sensitivity figure of merit for mixers is a receiver input noise temperature which can be measured using the Y-factor technique. Losses and noise of measurement setup components affect measured receiver noise. Therefore, noise contribution of these components has to be analysed in order to study noise performance of HEB mixers themselves. The intrinsic mixer parameters (conversion gain and output noise temperature) can be measured with the U-factor technique using the achieved receiver noise temperature. Mixing of radiation from two sources, when the frequency of one source (LO) is fixed and the frequency of another source is tuned (signal) allows for the direct measurement of mixer GBW. However, the calibration of IF chain and tunable source output power is required.

This chapter describes techniques used for MgB$_2$ HEB mixers THz characterisation.

5.1 Sensitivity characterisation

In order to provide effective radiation coupling into devices, fabricated MgB$_2$ HEBs were mounted in a mixer block with a 5 mm elliptical Si lens (see Figure 5.1(a)). The mixer block was placed inside a cryostat (see Figure 5.2(a)) providing cooling down to LHe temperatures. A parabolic off-axis mirror was placed inside the cryostat to focus an incident radiation into the device in order to improve radiation coupling from a LO. A Zitex™ IR block filter was mounted on a 4K screen of the cryostat. A bias-T followed the mixer block to apply a voltage bias to the device and to separate an IF response (see Fig. 5.2(a)). Several amplifiers were used in the IF chain to measure the IF response. One cryogenic low-noise amplifier (LNA) was used inside the LHe cryostat (Chalmers 1.5–4.5 GHz indium phosphide (InP) LNA) in order to amplify a low power IF signal. Two room temperature LNAs were used.
outside the cryostat (Chalmers 1.5–4.5 GHz Gallium arsenide (GaAs) LNA and MITEQ 0.1–10 GHz LNA) to amplify the IF signal further in order to overcome the noise floor. For the characterisation of HEBs with large noise bandwidth cryogenic and room temperature SiN1.5–4.5GHz band LNAs were substituted with a set of Chalmers 1.0–9.0 GHz InP LNAs.

The schematics of experimental setup is presented in Figure 5.2(b). A far-infrared (FIR) gas laser radiation (LO beam) was combined with signal from either hot or cold loads (Eccosorb sheets) using a Mylar® beam splitter. The emission lines of the FIR gas laser used for mixer sensitivity characterisation were 0.69 THz (formic acid (CH$_2$O$_2$) line), 1.63 THz, and 2.56 THz (difluoromethane (CH$_2$F$_2$) lines). A high-density polyethylene (HDPE) window let the incoming radiation enter the cryostat. The amplified IF signal was measured through a tunable 50 MHz band-pass YIG-filter with a powermeter. A Golay cell connected to the oscilloscope (not presented in Figure 5.2(b)) was placed behind the beam splitter to monitor the FIR gas laser output power during experiments. Various bath temperatures were used during tests. The temperature of boiling LHe under the standard conditions (4.2 K) were used as a base temperature. Pumping of helium vapour was performed to decrease a bath temperature down to 2 K. A resistive heater mounted directly on the mixer block was used for measurements at elevated bath temperatures up to 30 K (see Fig. 5.2(a)).

### 5.1.1 Y-factor technique

In order to measure the DSB receiver noise temperature $T_{rec}$ the standard Y-factor technique [189] was used. $Y$ is a ratio between receiver output powers with the hot $P_{hot}$ and the cold $P_{cold}$ loads (in this case 295 K and 77 K, respectively):

$$Y = \frac{P_{hot}}{P_{cold}} = \frac{2G_{tot}G_{IF}k_{B}(T_{rec} + T_{295K})B}{2G_{tot}G_{IF}k_{B}(T_{rec} + T_{77K})B} = \frac{T_{rec} + T_{295K}}{T_{rec} + T_{77K}}$$

(5.1)
5.1. Sensitivity characterisation

Fig. 5.2: Mixer noise and gain characterisation. (a) The cold plate of LHe cryostat. (b) The schematic of measurement setup.
where $G_{tot}$ is the total receiver gain, $G_{IF}$ the IF chain gain, $T_{IF}$ the IF chain input noise temperature, $B$ the bandwidth, and $T_{295K}$, $T_{77K}$ the Callen-Welton temperatures [190] of hot and cold loads. The noise temperature then could be calculated as:

$$T_{rec} = T_{295K} - Y T_{77K}$$

(5.2)

Since THz superconducting mixers (e.g. HEB mixers) are characterised in a complex set-up, both the loss and the noise contributions of optical components have to be analysed. That allows for de-embedding of the mixer input noise temperature. Figure 5.3 represents the signal path through the optical and electrical components in the receiver. A contribution of optical elements to a noise temperature can be calculated using the general formula for lossy components $T_{eq} = (L-1)T$ (where $L$ is a component loss and $T$ is a Callen-Welton temperature of component) and then deducted from the measured noise temperature (Table 5.1). The losses in the Si lens were treated as a part of mixer loss and was not deducted from the noise temperature. The DSB receiver noise temperature is then:

$$T_{rec} = T_{opt} + T_m L_{opt} + \frac{T_{IF}}{2G_{tot}}$$

(5.3)

where $T_{opt}$ is the noise contribution of optical components and $L_{opt}$ the optical losses.

### 5.1.2 U-factor technique

In order to measure both the mixer conversion gain and the output noise temperature, the U-factor technique [94] was applied. The U-factor is defined as a ratio between receiver output powers when the receiver is in an operating state and a reference state which can be characterised by an equivalent temperature $T_{REF}$. As a reference state either a superconducting state or a normal state could be used. In a superconducting state a HEB works as a microwave short and reflects all power coming from an IF chain ($T_{REF} = T_{IF}$). A normal
Table 5.1: Optical losses along the signal path at 0.69 THz (L_{0.69THz}) and 1.63 THz (L_{1.63THz}).

<table>
<thead>
<tr>
<th>Component</th>
<th>L_{0.69THz}(dB)</th>
<th>L_{1.63THz}(dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Air path (50 cm)</td>
<td>0.03</td>
<td>0.55</td>
</tr>
<tr>
<td>Cryostat window (1 mm HDPE)</td>
<td>0.7</td>
<td>0.7</td>
</tr>
<tr>
<td>IR filter (2 Zitex™ sheets)</td>
<td>0.6</td>
<td>0.6</td>
</tr>
<tr>
<td>Si lens reflection</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Total</td>
<td>2.33</td>
<td>2.85</td>
</tr>
</tbody>
</table>

State could be achieved by a heavy pumping of HEB with the LO. For a HEB in a normal state an output power is determined mostly by the thermal noise with an effective temperature which is equal to the electron temperature of HEB in this state (i.e. about $T_c$). In both reference states, an output power of the receiver is determined by a sum of the reference and the IF chain noise temperatures:

$$U = \frac{2 G_{tot} (T_{rec} + T_{295K})}{T_{IF} + T_{REF}}$$  \hspace{1cm} (5.4)

In this case the mixer conversion gain could be calculated as:

$$G_m = G_{tot} L_{opt} = \frac{U (T_{IF} + T_{REF})}{2 (T_{rec} + T_{295K})} L_{opt}$$  \hspace{1cm} (5.5)

Using Equations 2.12 and 5.3, Equation 5.4 could be rewritten as:

$$U = \frac{T_{out} + T_{IF} + 2 G_{tot} (T_{opt} + T_{295K})}{T_{IF} + T_{REF}}$$  \hspace{1cm} (5.6)

Finally, the mixer output noise temperature becomes:

$$T_{out} = U (T_{IF} + T_{REF}) - T_{IF} - 2 G_{tot} (T_{opt} + T_{295K})$$  \hspace{1cm} (5.7)

Another way to obtain the mixer conversion gain and the output noise temperature is to calculate it directly from the IF response of HEB mixer at an operation state:

$$P_{out} = k_B B (T_{295K} + T_{rec}) \frac{2 G_m G_{IF}}{L_{opt}}$$  \hspace{1cm} (5.8)

where $G_{IF}$ is an IF chain gain. If both the gain and the noise temperature of the IF chain are well known, the mixer conversion gain could be derived from Equation 5.8 as:

$$G_m = \frac{P_{out} L_{opt}}{2 k_B B (T_{295K} + T_{rec}) G_{IF}}$$  \hspace{1cm} (5.9)

In this case, the mixer output noise temperature is:

$$T_{out} = \frac{P_{out} L_{opt}}{2 k_B B G_{IF}} - T_{IF} - \frac{2 G_m (T_{295K} + T_{opt})}{L_{opt}}$$  \hspace{1cm} (5.10)
Fig. 5.4: Mixer GBW characterisation. (a) The cold plate of LHe cryostat. (b) The schematic of measurement setup.
5.2 GBW characterisation

For GBW measurements, MgB$_2$ HEB mixers were mounted in a mixer block with a 12 mm elliptical Si lens (see Figure 5.1(b)). The mixer block was placed in the LHe cryostat just in front the cryostat window. The mixer block output was connected directly to the cryostat output bypassing both the bias-T and the cryogenic LNA (see Figure 5.4(a)). The same resistive heater was mounted on the mixer block to perform measurements at elevated bath temperatures.

The full measurement setup schematics is presented in Figure 5.4(b). Radiation from two sources was combined using the Mylar® beam splitter. The frequency of Source 1 was fixed while the frequency of Source 2 was tuned. Either the FIR laser at 0.69 THz line or the backward wave oscillator (BWO) at 0.4 THz were used as a fixed frequency source. SD based frequency multiplier sources for corresponding frequency were used as a tunable frequency source. For GBW measurements at 0.1 THz, a Gunn diode source and a tunable high-electron-mobility transistor (HEMT) based frequency multiplier source were utilized. Signals from both sources were mixed by rectangular waveguide directional coupler with a horn antenna at the output for quasi-optical coupling of combined radiation into the receiver. Another broadband (20 kHz–45 GHz) bias-T was placed outside the cryostat to apply a voltage bias to the device and to separate the IF response. Two broadband MITEQ (0.1–20 GHz) LNAs followed the bias-T. The amplified mixing signal $P_{IF}$ was measured with a spectrum analyser:

$$P_{IF} = P_s \frac{1}{L_{opt}} G_m G_{IF} \quad (5.11)$$

The gain of entire IF chain (except for the mixer unit) was measured with a noise figure analyser. Variation of tunable THz sources output power was measured both with HEB direct detection response on amplitude modulated THz signal and the Golay cell. After measurements, both calibrations were applied to recorded curves in order to obtain the IF response of HEB mixers themselves.

5.3 S/N ratio characterisation

The mixer characterisation using the Y-factor technique is practical for noise temperatures less than 10 000 K ($Y = 0.1 \text{ dB}$). For lower Y-factor values the stability of the LO source becomes more critical. Device characterisation well outside the optimal bias regions and LO pumping levels (and at bath temperatures close to the $T_c$) becomes problematic without proper LO source stabilization. Therefore, heterodyne mixing was utilized in order to measure mixer signal to noise (S/N) ratio, which could be done in a broader conditions range. The experiments were performed using the FIR gas laser at 0.69 THz as an LO. The Schottky diode based frequency multiplier source was used as a signal source. The absolute power of the signal source (including mixer-to-source beam mismatch losses) was of no importance at that stage. However, the output power of the signal source was kept constant during experiments. After the cryogenic LNA, the IF signal was split into two branches outside the cryostat: 1) with the room temperature LNAs and the band-pass YIG-filter
Fig. 5.5: Schematic of measurement setup for S/N ratio characterisation.
(for output noise measurements); and 2) directly fed into the spectrum analyser (for mixing signal measurements). The YIG-filter was set at 2 GHz. In order to exclude any effect from the signal source on the output noise measurements, the signal source frequency was detuned by 2.5 GHz from the LO.

The mixing signal $P_{IF}$ was recorded along with the receiver output noise power $P_{out}$ for the same operation points. Since the incident power from the signal source, the optical losses, and the IF chain gain were constant through the experiments, variation of the $P_{IF}$ are due to changes of the mixer gain (see Equation 5.11). Therefore, the mixer gain (in relative units) can be compared at different LO pumping levels and bath temperatures.

By using Equations 2.12 and 5.3, Equation 5.8 could be rewritten as:

$$P_{out} = k_B B \left( \frac{2 G_m T_{295K}}{L_{opt}} + T_{out} + \frac{T_{IF}}{G_{IF}} \right) G_{IF}$$  \hspace{1cm} (5.12)

In case of $T_{IF} \ll T_{out}$, the receiver output noise is mostly proportional to the mixer output noise temperature (see Equation 5.12). The S/N ratio then is calculated as:

$$S/N = \frac{P_{IF}}{P_{out}}$$  \hspace{1cm} (5.13)
Chapter 6

MgB$_2$ HEBs THz characterisation results

This chapter summarises the results on THz characterisation of MgB$_2$ HEB mixers fabricated from both MBE and HPCVD grown MgB$_2$ superconducting thin films. The results are presented in [Paper A], [Paper B], [Paper D], [Paper E], [Paper F], [Paper G], and [Paper H].

6.1 Devices fabricated from MBE grown films

6.1.1 DC characterisation

One device from each of the three batches B14, N1, N3 was chosen THz characterisation (see Table 6.1). HEB B14-1 discussed below was 10 nm thick and 1×1 $\mu$m$^2$ in size with a $T_c$ of 8.5 K. HEB N3-2 was 20 nm thick and 1×0.2 $\mu$m$^2$ in size with a $T_c$ of 22.5 K. HEB N1-2 was 20 nm thick and 1×0.5 $\mu$m$^2$ in size with a $T_c$ of 22 K. The resistance versus temperature (R-T) curves (see Figure 6.1(a)) were measured in a dip-stick for all HEBs. The devices were biased at

![Graph showing R-T curves for HEBs B14-1, N1-2, and N3-2.](a)

![Graph showing R-T curves in logarithmic scale for HEBs N1-2 and N3-2.](b)

Fig. 6.1: R-T curves (a) for HEBs B14-1, N1-2, and N3-2 and (b) in logarithmic scale for HEBs N1-2 and N3-2. (Data adopted from [Paper B])
Table 6.1: MBE MgB$_2$ HEB thickness (d), size (W×L), critical temperature ($T_c$), resistance at room temperature ($R_{295K}$), resistivity ($\rho_{295K}$), and critical current density ($J_c$). (Data adopted from [Paper A] and [Paper B])

<table>
<thead>
<tr>
<th>Device</th>
<th>d(nm)</th>
<th>W×L ($\mu$m$^2$)</th>
<th>$T_c$(K)</th>
<th>$R_{295K}$($\Omega$)</th>
<th>$\rho_{295K}$($\mu\Omega$cm)</th>
<th>$J_c$($10^7$A/cm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>B14-1</td>
<td>10</td>
<td>1×1</td>
<td>8.5</td>
<td>160</td>
<td>160</td>
<td>0.7</td>
</tr>
<tr>
<td>N1-2</td>
<td>20</td>
<td>1×0.5</td>
<td>22.0</td>
<td>400</td>
<td>850</td>
<td>5.5</td>
</tr>
<tr>
<td>N3-2</td>
<td>20</td>
<td>1×0.2</td>
<td>22.5</td>
<td>330</td>
<td>1650</td>
<td>5.0</td>
</tr>
</tbody>
</table>

Results of DC measurements are very different from the data acquired with the devices fabricated from HPCVD grown films (see Chapter 3). The resistivity of these 10–20 nm films was much smaller (50–90 $\mu\Omega$cm), whereas critical current density was higher ((2–12)$\times 10^7$ A/cm$^2$ in submicron size bridges).

6.1.2 Direct detection characterisation

Some preliminary pumping tests of HEB N1-2 were conducted prior to the noise measurements in order to study the effect of THz radiation on the device. For pumping experiments, the cryostat was placed directly in front of the FIR gas laser front panel. The I-V curves for HEB N1-2 are given in Figure 6.2. The mixer was pumped to the I-V curve close to the optimum with the total available LO power estimated to be $\sim 100\mu$W in front of the cryostat (Curve 3 in Figure 6.2(a)). A high $T_c$ of 22-23 K according to the BCS theory corresponds to 8 meV $\sigma$-gap (or 1.9 THz, $2\Delta = \hbar\omega$, where $\hbar$ is the Dirac constant), where a conduction prevails for dirty samples [192,193]. However, at 1.63 THz the switching similar to the one of NbN devices under the pumping at frequencies below the superconducting gap frequency was not observed. It was demonstrated experimentally, that for the MgB$_2$ thin film in dirty limit with a $T_c$ as high as 33 K absorption of radiation occurs in a superconducting gap...
6.1. Devices fabricated from MBE grown films

Fig. 6.2: I-V curves for HEB N1-2. (a) Curve 1: 4.2 K without LO pumping; Curve 2: Heater 1 without LO pumping; Curve 3: 4.2 K the maximum LO pumping; Curve 4: Heater 1 with the maximum LO pumping; Curve 5: Heater 2, the heating was increased until curve 5 coincided with curve 4. (b) The numbers in the field represent the voltage response on the lock-in amplifier at 1.63 THz. (Data adopted from [Paper A])

of 1.3 THz [194]. Curves 4 (2) correspond to the increased bath temperature with (without) LO pumping, respectively. For Curve 5 LO was switched off and a bath temperature was further increased by the resistive heater until it overlapped with Curve 4. The identity of Curves 4 and 5 demonstrate that 1.63 THz radiation has the same effect on a HEB as the rise of a bath temperature.

Direct detection experiments were performed in order to estimate which I-V curve corresponds to the HEB’s maximum sensitivity to the THz radiation. The voltage response of HEB N1-2 on amplitude modulated THz radiation was recorded for a set of bath temperatures and bias points (see Figure 6.2(b)). The FIR gas laser radiation was attenuated by $\sim 20$ dB to reach a small signal limit, when the THz radiation has no visible effect on I-V curves. The FIR gas laser radiation was modulated with the chopper 20 Hz. With the HEB in a current biased mode, a lock-in amplifier with a separate voltage pre-amplifier was used to measure voltage response of the HEB. The maximum responsivity was achieved at bias points ranging from 2 mV to 4 mV and from 0.3 mA to 0.5 mA, i.e. at 25-35% of the critical current at 4.2 K. Taking into account optical losses, the maximum responsivity at 1.63 THz can be estimated to be in a range of 1–2 kV/W.

6.1.3 Mixer sensitivity characterisation

HEB B14-1 had a $T_c$ of 8.5 K, relatively low for MgB$_2$. Therefore, this device could be directly compared to NbN HEBs. LO pumped I-V curves of B14-1 at both 4.2 K and 2 K are presented in Figure 6.3. The minimum DSB receiver noise temperature corrected for optical losses versus the IF for device B14-1 at 4.2 K is presented in Figure 6.4(a). The I-V curves of B14-1 under LO pumping at 2 K are presented in Figure 6.3(b). The reduction of bath
Fig. 6.3: (a) I-V curves for HEB B14-1: under 1.63 THz LO pumping (a) at 4.2 K (LO2 is an optimal I-V curve) and (b) at 2 K (LO3 is an optimal I-V curve). (Data adopted from [Paper B])

Fig. 6.4: DSB receiver noise temperature corrected for optical losses versus IF for HEB B14-1 (a) at 1.63 THz (the bias points are $U_0 = 0.8$ mV $I_0 = 28$ µA at 4.2 K and $U_0 = 1.3$ mV $I_0 = 23$ µA at 2 K) and (b) 2.6 THz (the bias point is $U_0 = 1.38$ mV and $I_0 = 31$ µA at 2 K). (Data adopted from [Paper B])

temperature resulted in a $\sim 30\%$ increase of the critical current and a $\sim 30\%$ reduction of the receiver noise temperature (see Figure 6.4(a)). The corrected DSB noise temperature acquired with Y-factor measurements for HEB B14-1 was fitted with Equation 2.28. The values of $T_m(0)$ and $f_N$ obtained from a fit are 1050 K and 3.2 GHz for 4.2 K; 700 K and 3.2 GHz for 2 K.

The LO power, required to reach the minimum receiver noise temperature, was calculated using the isotherm method (LO2 curve in Figure 6.3(a)) was 70 nW. The isotherm method assumes that both DC and LO powers have similar effect on HEB resistance [149]. At 2 K the required LO power was estimated to be 80 nW. The LO power required for the minimum noise is in the same ballpark as one reported for NbN HEB mixers.

The available LO power was enough to pump the device into the normal state and to perform U-factor measurements. The noise temperature of the IF chain was determined by the noise temperature of the first LNA which was
Table 6.2: Mixer conversion gains (G_m) and output noise temperatures (T_out) for HEB B14-1 at f_{IF} = 1.8 GHz calculated using Equations 5.5 and 5.7 with superconducting and normal reference states, and using Equations 5.9 and 5.10. (Data adopted from [Paper B])

<table>
<thead>
<tr>
<th>T_{bath}(K)</th>
<th>G_m(dB)</th>
<th>T_{out}(K)</th>
<th>G_m(dB)</th>
<th>T_{out}(K)</th>
<th>G_m(dB)</th>
<th>T_{out}(K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.2</td>
<td>-19.1</td>
<td>31</td>
<td>-19.6</td>
<td>27</td>
<td>-19.9</td>
<td>26</td>
</tr>
<tr>
<td>2</td>
<td>-18.2</td>
<td>21</td>
<td>-18.1</td>
<td>22</td>
<td>-18.9</td>
<td>18</td>
</tr>
</tbody>
</table>

mounted on the cryostat’s cold plate. The gain of this LNA was 30 dB and the noise temperature was \( \approx 2 \) K. For the whole IF chain the noise temperature was estimated to be not exceeding 3 K. The total gain of the IF chain, used for the gain method calculation, was 77 dB at 1.8 GHz.

At 4.2 K, at the optimal operation point of \( U_0 = 0.8 \) mV \( I_0 = 28 \) \( \mu \) A the U-factor was 8.2 dB for the superconducting state reference and 4.7 dB for the normal state reference. An uncorrected DSB receiver noise temperature of 2500 K and \( T_{REF} = 9 \) K were taken for calculation using Equations 5.5 and 5.7. At 2 K, the following values were used for the mixer conversion gain and the output noise calculation (\( U_0 = 1.3 \) mV \( I_0 = 23 \) \( \mu \) A bias point): U-factor for a superconducting state reference of 7.2 dBm, U-factor for a normal state reference of 4.2 dBm, a receiver noise temperature of 1500 K and \( T_{REF} = 9.3 \) K. Mixer conversion gains and output noise temperatures, calculated using all three methods, are summarized in Table 6.2. The values obtained by all three methods are very close to each other, which can be interpreted as a confirmation of reliability. While changing the bath temperature from 4.2 K to 2 K the mixer conversion gain increased by \( \sim 1 \) dB, whereas the mixer output noise temperature decreased by 5–10 K. Both of these facts lead to a decrease of the receiver noise temperature. It is of interest to compare this device to a NbN HEB mixer since \( T_c \)s are quite close. The reported conversion gain for NbN HEB was -12 dB with a mixer output noise temperature of about 40 K [94,139]. The U-factor measurements for HEB B14-1 were performed at a 1.8 GHz IF which is quite close to the 3-dB roll-off frequency. Therefore, a correction of about +2 dB should be applied. The receiver noise temperatures and NBWs are in the same ballpark.

Characterisation of MgB\(_2\) HEBs with a higher \( T_c \), in a mode where LO frequency is higher than superconducting gap frequency, requires operation at higher bath temperatures or utilization of LO sources with higher frequencies. Therefore, preliminary Y-factor measurements were performed with HEB B14-1 at 2.6 THz and 2 K. The available output power from the FIR gas laser at this frequency was lower compared to 1.63 THz but still enough to pump the device. The DSB receiver noise temperature versus the IF (\( U_0 = 1.38 \) mV \( I_0 = 31 \) \( \mu \) A) is presented in Figure 6.4(b). The fit with Equation 2.28 gives a zero IF noise temperature of 1250 K and NBW of 3.2 GHz. At 2.6 THz, the receiver noise temperature of HEB B14-1 appeared to be higher compared to a 1.63 THz LO.

The same experimental setup was used for HEB N3-2 characterisation and
a thin plastic film was placed between the mixer block and the cryostat cold plate to minimize a LHe boiling rate during “heated” tests. The I-V curves for HEB N3-2 at 4.2 K and 12 K with and without 1.6 THz LO pumping are presented in Figure 6.5(a). At a bath temperature of about 12 K the HEB critical current has reduced to the half of its value at 4.2 K. The required LO power for the minimum noise operation at 12 K is 1.7 µW compared to 2.6 µW at 4.2 K. The measured receiver noise temperatures across a 1–4 GHz IF band for bath temperatures of 4.2 K and 12 K fitted with Equation 2.28 are presented in Figure 6.5(b). Measurements were performed at bias points of $U_0 = 1.6 \text{ mV}$, $I_0 = 180 \mu \text{A}$ and $U_0 = 1.8 \text{ mV}$, $I_0 = 200 \mu \text{A}$, respectively. At certain IFs the mixer response on a hot-cold load was unstable, which resulted in errors in noise temperature measurements (e.g. at 3.2 GHz for 12 K and 1.9 GHz, 2.9 GHz for 4.2 K). The corrected receiver noise temperature increased from 1700 K to 2150 K with an increase of bath temperature but a NBW of 5 GHz remained unchanged.

A direct measurement of GBW at frequencies $>1 \text{ THz}$ is problematic due to a low availability of coherent sources with a tunable frequency. One of the possible solutions is a use of BWOs or multiplier sources with frequencies $<1 \text{ THz}$. For NbN HEB mixers made from ultrathin films a typical critical temperature is about 9 K. This $T_c$ gives a superconducting gap frequency of about 0.6 THz at 4.2 K. Hence, NbN devices work with mentioned power sources in the regime where the LO frequency is higher than the gap frequency. Consequently, this mixing experiments could be extrapolated to higher frequencies. For devices with a high $T_c$ (and hence, large superconducting gap) such low frequency mixing experiments can not be extrapolated to higher frequencies because of slightly different mechanism of mixer operation. In this case, low frequency THz radiation is absorbed only in a normal domain of HEB bridge where a superconducting gap is suppressed by a DC power. Instead of mixing experiments for N3-2 U-factor measurements were performed across the IF band in

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**Fig. 6.5:** (a) I-V curves for HEB N3-2 with (without) 1.63 THz LO at 12 K and 4.2 K. (b) DSB receiver noise temperatures corrected for optical losses versus IF for HEB N3-2 at 1.63 THz and, 4.2 K (circles) and 12 K (squares). The bias points are $U_0 = 1.6 \text{ mV}$, $I_0 = 180 \mu \text{A}$ and $U_0 = 1.8 \text{ mV}$, $I_0 = 200 \mu \text{A}$, respectively. (Data adopted from [Paper B])
6.2 Devices fabricated from HPCVD grown films

6.2.1 Gain bandwidth characterisation

GBW measurements were performed at three LO frequencies of 0.1 THz, 0.4 THz, and 0.69 THz. The first two frequencies were expected to be below the superconducting gap frequency at 4.2 K, so the tested HEBs were heated up to 25–35 K in order to suppress the superconducting gap. The GBW was observed to be almost independent on both the bias voltage and the bath temperature. The higher output power of 0.1 THz LO allowed for GBW measurements of thicker devices at a wider range of bath temperatures and device sizes. Figure 6.7 presents I-V curves measured in LHe cryostat and the mixing signal at 0.1 THz for 30 nm thick HEB E2-2 with a $T_c$ of 39.5 K. The mixing signal curves taken at different bias points and bath temperatures coincide perfectly. HEBs E3-8 (20 nm thick, $T_c = 38.5$ K) and E6-4 (12 nm thick, 33.5 K) were tested at various LO frequencies. Figure 6.8 demonstrates that the GBW of these devices is independent on the LO frequency at least in 0.1–0.69 THz range.

The summary of GBW measurements performed for the HEBs of various thickness is plotted in Figure 6.9. A GBW of 6.8 GHz was observed for HEB

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**Fig. 6.6:** Conversion gain (circles) and output noise temperature (squares) versus the IF for HEB N3-2 at 1.63 THz and (a) 4.2 K, $U_0 = 1.6$ mV, $I_0 = 180$ $\mu$A and (b) 12 K, $U_0 = 1.8$ mV, $I_0 = 200$ $\mu$A. (Data adopted from [Paper B])

order to extract the GBW. Moreover, this method provides both the mixer conversion gain and the output noise temperature. The results of U-factor measurements for 4.2 K and 12 K are presented in Figure 6.6. Higher ripples for IFs $<1.5$ GHz correspond to the region of LNA’s high return loss. Experimental data were fitted with Equation 2.20. The zero IF mixer conversion gain and the GBW achieved from the fit are -15.1 dB and 3.4 GHz; -14.7 dB and 3.5 GHz at 4.2 K and 12 K, respectively. The HEB shows almost the same conversion gain and GBW at both bath temperatures, but the output noise at 12 K is higher, which resulted in a higher receiver noise temperature. The similar effect of bath temperature was observed for HEB B14-1.
Chapter 6. MgB$_2$ HEBs THz characterisation results

Fig. 6.7: GBW of HEB E2-2 (30 nm thick, $T_c = 39.5\, K$). (a) I-V curves measured in LHe cryostat at various bath temperatures and (b) mixing signal at 0.1 THz at various bias points. (Data adopted from [Paper E])

Fig. 6.8: GBW of HEBs (a) E3-8 (20 nm thick, $T_c = 38.5\, K$) at 0.1 THz and 0.4 THz LOs and (b) E6-4 (12 nm thick, $T_c = 33.5\, K$) at 0.4 THz and 0.69 THz.
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Fig. 6.9: Normalized IF signal of four MgB\textsubscript{2} HEB mixers measured at 0.1 THz (E2-2), 0.4 THz (E3-8), and 0.69 THz (E6-4, E10-8).

Table 6.3: HPCVD MgB\textsubscript{2} HEB thickness (d), critical temperature (T\textsubscript{c}), GBW, time constant (τ), electron and phonon heat capacities ratio (c\textsubscript{e}/c\textsubscript{ph}) and critical current density (J\textsubscript{c})

<table>
<thead>
<tr>
<th>Device</th>
<th>d (nm)</th>
<th>T\textsubscript{c} (K)</th>
<th>GBW (GHz)</th>
<th>τ (ps)</th>
<th>c\textsubscript{e}/c\textsubscript{ph}</th>
<th>τ\textsubscript{ep} (ps)</th>
<th>τ\textsubscript{esc} (ps)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E2-2</td>
<td>30</td>
<td>39.5</td>
<td>1.5±0.1</td>
<td>106</td>
<td>0.57</td>
<td>3.5±1</td>
<td>22±2</td>
</tr>
<tr>
<td>E3-8</td>
<td>20</td>
<td>38.5</td>
<td>2.5±0.15</td>
<td>64</td>
<td>0.59</td>
<td>4±1</td>
<td>20±1.5</td>
</tr>
<tr>
<td>E6-4</td>
<td>12</td>
<td>33.5</td>
<td>6.8±0.25</td>
<td>24</td>
<td>0.73</td>
<td>5±0.5</td>
<td>5±0.5</td>
</tr>
<tr>
<td>E10-8</td>
<td>8</td>
<td>31.0</td>
<td>10.3±1.2</td>
<td>16</td>
<td>0.82</td>
<td>6±0.2</td>
<td>3±1</td>
</tr>
</tbody>
</table>

E6-4 made from the 12 nm thick MgB\textsubscript{2} film. The GBW is about 2-3 times larger than for typical phonon-cooled NbN HEB mixers made from 3–5 nm thick NbN films. The critical temperatures of the discussed HEBs were in the range of 30–40 K where similar electron-phonon interaction times are expected. Therefore, the increase of GBW for thinner films is expected to be defined mostly by the reduction of the phonon escape time.

In order to estimate these characteristic times, a fit to experimental data was done with the 2-T model (see Chapter 2) similar to Ref. [124]. The same Debye temperature (750 K) and electron specific heat (3 mJ/mol K\textsuperscript{2}) were used for fitting. The HEB parameters and the results are summarized in Table 6.3. The characteristic times follow expected trends (an increase of electron-phonon interaction time and a reduction of escape time). The estimated phonon escape times are twice shorter compared to the escape times measured for HEBs fabricated from MBE grown films [124] suggesting a better acoustic matching at a film/substrate interface. It is obvious that in order to archive more reliable results for device thinner than 10 nm measurements should be performed up
to higher IFs (at least 20 GHz), which requires a fabrication of a new mixer block and a re-calibration of the whole IF chain.

6.2.2 Mixer sensitivity characterisation

6.2.2.1 Initial results

The GBW characterisation provides some useful information about potential devices performance. However, it was not the main goal of the study since the ultimate characteristics of HEB mixers are receiver noise temperature and NBW. At first stages, sensitivity characterisation was challenging. Initial devices were made from films thicker than 10 nm with high $T_c$ (close to the bulk value) and high critical current densities. For LO pumping to expected optimal I-V curves, a thick beam splitter (200 µm) with a high transmission loss was used. The available LO power was still not enough to pump the device at 4.2 K, so the bath temperature had to be raised above 20 K. The thick beam splitter and elevated bath temperatures used for device characterisation resulted in a quite high measured DSB receiver noise temperature of 6000 K (see Figure 6.10(a)) for HEB E6-4, which after applying correction for optical losses becomes 3100 K.

Better results were achieved for batch E8 made from a 10 nm thick film. Corrected for optical losses DSB receiver noise temperature of 1600 K (see Figure 6.10(b)) was measured for HEB E8-2 with a $T_c$ of 32 K at 0.69 THz and 15 K. At 20 K the noise temperature increased to 2500–3000 K. For HEB E8-7 the receiver noise temperature was measured versus the IF. Recorded I-V curves are shown in Figure 6.11(a). The I-V curve under the optimal LO power (the highest Y-factor) is IV-opt. The corresponding output IF power curve (Figure 6.11(a), PV-opt) varies with bias voltage with a maximum at about 0.5 mV. The lowest receiver noise temperature was obtained at bias voltages slightly above the maximum on the PV-opt curve (1–2 mV). In the normal state, I-V curve IV-norm is totally linear with a resistance of 50Ω equal to the resistance near the beginning of superconducting transition. The output IF power curve (PV-norm) is also bias independent indicating that the HEB is in a normal state. The noise temperature is approximately 2000 K in

Fig. 6.10: DSB receiver noise temperature measured by Y-factor technique for HEBs (a) E6-4 and (b) E8-2. (Data adopted from [Paper D] and [Paper F])
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Fig. 6.11: HEB E8-7 (a) IV curves: IV-noLO - in the mixer block at 10 K; IV-opt - under the optimal LO power; IV-norm - pumped by the LO into the normal state. Output IF power versus bias voltage curves measured at 2 GHz: PV-opt corresponds to the optimal LO (IV-opt); PV-norm corresponds to the normal state (IV-norm). (b) DSB receiver noise temperature (circles) and the output power (stars) versus the IF. The dotted and dashed lines are fits for 6 GHz and 8 GHz NBWs, respectively. (Data adopted from [Paper F])

a 1.3–3 GHz IF range (see Figure 6.11(b)). The output IF power versus the IF curve exhibits some notches in 3–4 GHz range and at 4.3 GHz, which is also accompanied by the rise of noise temperature (see Figure 6.11(b)). It could be associated with the cryogenic LNA and leads to a reduced NBW of 6–8 GHz. For further measurements, the cryogenic LNA was replaced.

6.2.2.2 Low noise MgB$_2$ HEB mixers

Significant progress, comparing to the initial results, was achieved with MgB$_2$ HEB mixers $1 \times 1 \mu$m$^2$ in size with a $T_c$ of 30 K fabricated from a 8 nm thick HPCVD grown film for which Ar$^+$ cleaning was applied (see Chapter 3). These devices had room temperature resistances of $\approx 200 \Omega$ (see Figure 6.12). I-V curves for HEB E10-7 are given in Figure 6.13. Device E10-8 from the same batch had very similar critical current and I-V curves as for device E10-7. Therefore, further data would be given for HEB E10-7. Sheet resistance obtained from nanobridges was higher by a factor of 4 compared with sheet resistance measured on this film prior processing. The $T_c$ was reduced by 4 K. The Far Infrared (FIR) gas laser was used as a LO, with emission frequencies of 0.69 THz, 1.63 THz, and 2.56 THz. At 2.56 THz the output power was not sufficient to pump the mixer with a thin beam splitter (12.5$\mu$m) and hence, it was only used with a mirror to record I-V curves. With the optimal LO (0.69 THz) power, I-V curves at 5 K, 15 K, and 20 K fully overlap each other, indicating that the LO power at 0.69 THz is absorbed independently of the temperature and the bias voltage (see Figure 6.13(a)). At 5 K, the shape of the IV curves did not depend on the LO frequency from 0.69 THz to 2.56 THz (see Figure 6.13(b)) suggesting that absorption of THz radiation occurs in the $\pi$-gap (smaller gap). The same IV curves were achieved by simply rising the bath temperature with the LO turned off. The shapes of the curves are similar
Fig. 6.12: R-T curve for HEB E10-7. Summary of the receiver noise temperature at 0.69 THz (triangles) and 1.63 THz (circles) LOs. Empty symbols are receiver noise temperatures corrected for Si lens losses. (Data adopted from [Paper G])

to those for NbN HEB mixers.

With the 0.69 THz LO, receiver noise temperature was measured using the Y-factor technique at various LO power levels and in a bias voltage range up to 25 mV. The corresponding set of I-V curves at 5 K (each relates to a certain LO power) is given in Figure 6.14(a). The receiver noise temperature measured along IV-3 is given in Figure 6.14(a) (filled dark blue squares, right ordinate). For a bias voltage of 7 mV the receiver noise temperature is shown as a function of bias current (magenta squares, top abscissa). The lowest noise temperature is obtained in a bias voltage range corresponding to the maximum output noise (5–10 mV). The bias point range for the lowest receiver noise temperature is marked with the red oval (IV-3 to IV-5). As the mixer temperature increases, the optimal LO power range shrinks. At 20 K the lowest receiver noise was achieved only around IV-3. For the given set of I-V curves, which excessively covers the optimal LO-bias voltage range, the mixer output noise (see Figure 6.14(b)) increases continuously as the LO power is reduced from the heavily overpumped state (IV-7) till the underpumped state (IV-1) is reached. The mixer gain starts to saturate just above IV-5, i.e. above the optimal bias zone. The resulting S/N ratio (see Figure 6.14(d)) increases continuously as the LO power is reduced from the heavily overpumped state (IV-7) to IV-5. The (A-log(T_{rec})) for IV-3 is also plotted in Figure 6.14(d), where A is a fitting parameter for plotting. The logarithm of 1/T_{rec} follows closely the S/N ratio curve, as it is expected from Equation 5.13:

$$\log(S/N) \approx \log\left(\frac{P_{IF}}{k_B B T_{rec}}\right) \propto -\log(T_{rec})$$

(6.1)

demonstrating that the bias voltage and LO power optimization for both S/N ratio and receiver noise temperature coincides across the I-V plane. This fact illustrates that, despite the broadband antenna is used for the HEB mixer, the direct detection effect (shift of the bias point due to the switch between hot and cold loads) does not have any impact on the choice of the mixer
Fig. 6.13: HEB E10-7 I-V curves (a) in the cryostat at 5 K (no LO, blue solid), at 15 K (no LO, red dashed), at 20 K (no LO, green dash-dotted), three fully overlapping IV curves at the optimal LO power at 5 K, 15 K, and 20 K; (b) at different LO power levels (at 5 K): under the 0.69 THz, 1.63 THz, and 2.56 THz LO pumping, IV7 (black solid) at an elevated temperature without LO pumping. (Data adopted from [Paper G])

Fig. 6.14: HEB E10-7 with 0.69 THz LO pumping and at 5K. The area of the highest S/N ratio is marked on the I-V plane. (Data adopted from [Paper H])
operation point. In a 3 THz band, a black body at 295 K (77 K) emits $\approx 2.8 \text{ nW}$ ($\approx 1.6 \text{ nW}$) in the single spatial mode [12]. This is $\approx 1\%$ of a typical optimal LO power for NbN HEB mixers, and hence, this radiation has a significant impact on a mixer bias point especially at smaller bias voltages. For NbN HEB mixers this effect can either decrease or increase the apparent Y-factor (receiver noise temperature). However, for the discussed MgB$_2$ HEB mixers the direct detection effect is negligible.

The three sets of I-V curves at 5 K, 15 K, and 20 K (corresponding to IV-3, IV-4, and IV-5) are plotted in Figure 6.15(a). For the matching I-V curves, the output noise power versus bias voltage curves also totally overlap each other, which means that the mixer output noise temperature is independent on a bath temperature. In Figure 6.16(a), the output noise power at the same bias point (7 mV and 200 $\mu\text{A}$) is plotted as a function of bath temperature. In contrast to the output noise, mixer gain has decreased at higher temperatures (Figure 6.15(c)). The absorbed LO power was calculated using the isotherm method (see Figure 6.16(a)). The logarithm of absorbed LO power is plotted in Figure 6.16(a) (magenta diamonds) along with the mixer conversion gain (red squares). A reduction of mixer gain (by 2.5 dB) from 5 K to 20 K is proportional to a reduction of LO power (by 2.4 dB) for the given I-V curve, as it would be expected from the HEB mixer lumped element model. The logarithm of the receiver noise temperature follows exactly the same temperature trend as the S/N ratio (green triangles and filled stars in Figure 6.16(a)).
Mixer gain (filled circles) and output noise temperature (filled squares) calculated using the U-factor technique with a normal reference state are plotted in Figure 6.16(b) for 5 K, 15 K, and 20 K (all at the same bias point of 7 mV and 0.23 mA). Mixer gain is inversely proportional to the temperature, whereas output noise remains almost the same. This is also confirmed by the mixing experiment, as it can be seen in Figure 6.16(a). As follows from Figure 6.14(a) the receiver noise temperature is constant over quite a wide range of LO power. Across this range (IV5-IV3), both mixer gain and output noise vary by a factor of 2: from 120 K to 220 K and from -10.7 dB to -8.3 dB, respectively (see Figure 6.16(b)). Apart from a lower LO power, the operation at IV3 has an advantage of higher output noise. With an output noise of 220 K, the IF LNA noise becomes much less critical for the overall receiver noise temperature. This is particularly important for the broadband IF LNAs which optimization can now be focused on input matching (no need for an isolator) rather than on the noise. In Figure 6.16(b) both maximum output noise temperature and corresponding mixer gain (within the minimum receiver noise zone) are plotted for 5 K, 15 K, and 20 K mixer temperatures.

In order to obtain the HEB NBW, the noise temperature was measured across a wide IF band with a step of 50 MHz. Both 1.5–4.5 GHz and 1.0–9.0 GHz IF LNAs were used for the experiments. Measurements with the 1.5–4.5 GHz LNA were intended to verify whether HEB-LNA interference might be affecting obtained results. In Figure 6.17(a), the receiver noise temperature measured with the 1.5–4.5 GHz LNA at both 0.69 THz and 1.63 THz LOs is shown. The noise temperature increases proportionally over the whole IF range, indicating that NBW is the same at both LOs, and hence supporting...
Fig. 6.17: (a) HEB E10-7 receiver noise temperature versus the IF recorded at 5 K. Filled symbols: 1.63 THz. Open symbols: 0.69 THz. Circles: 1.5–4.5 GHz LNA. Triangles: 1.0–9.0 GHz LNA. (b) The receiver noise temperature (at 1.63 THz) as a function of IF recorded at 5 K, 15 K, and 20 K. Results for HEBs E10-7 (line) and E10-8 (symbols) are shown. (Data adopted from [Paper H])

the idea of heterodyne response bolometric nature in discussed devices. The noise temperature at lower IFs as measured with the 1.5–4.5 GHz LNA fully overlaps with the data obtained using the 1.0–9.0 GHz LNA. The hump at 3.7 GHz is present at both data sets and originates from the bias-T used for experiments. The noise temperature spectrum at 1.63 THz was measured at 5 K, 15 K, and 20 K for both HEBs E10-7 and E10-8 (see Figure 6.17(b)). The fitting curves are for an 11 GHz NBW. The summary of measured receiver noise temperatures measured at both 0.69 THz and 1.63 THz LO frequencies is given in Figure 6.12. Considering a possible reduction of reflection losses at the Si lens by 20% with an anti-reflection coating the minimum noise temperatures at 5 K are 830 K (0.69 THz) and 930 K (1.63 THz). At 15 K, the noise temperature rises by 20% from its value at 5 K. At 20 K, the noise temperature rises by 75%. As it can be noticed, the noise temperature difference between 0.69 THz and 1.63 THz is about 12%, which is similar to the rate observed for NbN HEB mixers at higher LO frequency.

6.2.3 Further improvement

As it is demonstrated in Figure 6.16(a), devices with a higher $T_c$ are needed in order to increase mixer gain and consequently improve noise performance at higher bath temperatures. HEB E15-7 with a $T_c$ of 33 K made from a 5 nm thick HPCVD grown MgB$_2$ film has demonstrated a lower noise temperature at 20 K compared to HEBs from batch E10 ($T_c = 33$ K) (see Figure 6.18). For device E15-7, a significant increase of the noise temperature (2500 K) was observed only at 25 K. At 30 K, the noise temperature of 15 000 K was estimated using S/N ratio approach. In order to push further the high temperature operation of MgB$_2$ HEB mixers, devices with even higher $T_c$ have to be utilized. Most likely, it would be possible to achieve only by increasing the film thickness, which would lead to a NBW reduction. Another direction to improve
6.2. Devices fabricated from HPCVD grown films

Fig. 6.18: HEB E15-7 receiver noise temperature (at 1.63 THz) versus the IF recorded at 5 K, 15 K, 20 K, and 25 K. The NbN HEB mixer data is from Ref. [32].

Fig. 6.19: MgB$_2$ HEB DSB receiver noise temperature versus HEB width.
MgB$_2$ HEB mixer noise performance is to decrease the contact resistance between the film and Au antenna. The observed dependence of noise temperature on device width (see Figure 6.19) suggests that the contact resistance has a significant contribution. The contact resistance might be reduced either by increasing HEB width, which will, unfortunately, lead to increase of required LO power, or by changing the fabrication procedure to improve the film/antenna contact.

However, MgB$_2$ HEB mixer already demonstrate noise performance comparable with state-of-the-art NbN HEB mixers but with a three times larger NBW (see Figure 6.18). Despite NbN HEB mixers can have lower noise temperature than the discussed MgB$_2$ HEB mixers at IFs below 1 GHz, the noise temperatures averaged over the IF bandwidth are in the same ballpark.
Chapter 7

Conclusion and future outlook

In this thesis, study of the novel HEB mixers for THz frequencies based on MgB\textsubscript{2} thin films have been discussed. \textbf{MgB\textsubscript{2} HEBs of submicron sizes were fabricated and characterised at THz frequencies.} Transition to submicron sizes has reduced LO power requirements and allowed for the pumping of MgB\textsubscript{2} HEBs to optimal I-V curves at the LHe temperature using available FIR gas laser. \textbf{Study of HEBs made from MBE grown MgB\textsubscript{2} films shows that both the output noise temperature and the conversion gain of HEB mixers are proportional to the T\textsubscript{c}.} This is valid for the optimal operation conditions: optimal LO power and DC bias. At the same time, utilization of films with a higher T\textsubscript{c} results in a broader NBW. Already having reached a T\textsubscript{c} of 22 K, HEB mixers can operate above 12 K with only a 25\% increase of the noise temperature, compared to that at 4.2 K. \textbf{MgB\textsubscript{2} HEB mixers can have a noise temperature as low as 700 K.} Three different methods for mixer conversion gain estimation: the gain method and U-factor methods with superconducting and normal reference states, were applied and compared. Good agreement with an error margin of \(\pm 0.5\) dB was demonstrated, which indicates the reliability of methods.

\textbf{An HPCVD system was constructed and launched at Chalmers University of Technology. It is applicable for ultrathin film deposition down to 5 nm without a need for post-processing.} Both the low resistivity of 50–90 \(\mu\Omega\text{cm}\) and the high \(J_c\) of up to \(1.2\times10^8\) A/cm\(^2\) indicate a rather good quality of the achieved films. The micron and submicron size HEB mixers can be fabricated from these films with a high yield (above 75\%). The best deposited films that were used in fabrication of HEBs, were only 5 nm thick with a T\textsubscript{c} of 33 K and a \(J_c\) of \((1–3)\times10^8\) A/cm\(^2\).

MgB\textsubscript{2} HEB mixers possess a unique combination of low noise, wide noise bandwidth, and high operation temperature when 5–8 nm thick superconducting MgB\textsubscript{2} films are used with a T\textsubscript{c} of 30–33 K. It was demonstrated that compared to the gain bandwidth (GBW) of NbN HEB mixer (\(\approx 3\)GHz), \textbf{the GBW for HEBs made from 8 nm thick HPCVD grown MgB\textsubscript{2} films was 10 GHz.} The GBW was inversely proportional to the film thickness and independent on both the bias voltage, the bath temperature, and LO fre-
quency (from 0.1 THz to 0.69 THz), which simplifies device characterisation. A **NBW of 11 GHz with a minimum receiver noise temperature of 930 K at 1.63 THz and 5 K was achieved.** At 15 K and 20 K, the noise temperature was 1100 K and 1600 K, respectively. From 0.69 THz to 1.63 THz the noise has increased by only 12%. The minimum noise temperature was achieved in a quite large range of bias voltages (5–10 mV) and LO power. A **similar noise temperature of \(\approx 1000 \text{ K}\)** and a larger **NBW of 13 GHz** were achieved with HEB mixers with a \(T_c\) of 33 K made from 5 nm thick films. Such devices have demonstrated a better noise performance at 20 K (1500 K), and operation at 25 K with a noise temperature of 2500 K. At 30 K the noise temperature was estimated to be 15 000 K.

Previously, a receiver noise temperature of 1600 K and a NBW of 6–8 GHz was measured for a 10 nm thick devices. An improvement of sensitivity and NBW was due to a larger bolometer width (lower contact resistance), applied in-situ contact cleaning, and a smaller film thickness. An increase of noise temperature at elevated bath temperatures is determined by a reduction of mixer conversion gain (less LO power is absorbed in the bolometer), while output noise of the HEB remains the same. A high output noise temperature (210 K), compared to values reported for NbN HEB mixers (60 K), lowers demands for the low noise IF chain. Instead of cryogenic LNAs at LHe temperature, LNAs at room temperature or LNAs mounted on higher stages of cryocooling system might be used. In this case crycoolers with a smaller cold plate and lower cooling power can be utilized, which is important for spaceborne telescopes where resources are always limited. Fabricated devices with a Si\(_N_x\) passivation demonstrated high robustness and did not lose their properties after continuous storage in a nitrogen atmosphere. However, for a space applications special reliability tests would be required.

Good sensitivity and a large bandwidth as well as operation at elevated bath temperature have been achieved in HEBs from several batches. A combination of these parameters in one device would provide a perfect instrument for the sub-mm wave astronomy. \(\text{MgB}_2\) HEB mixers have shown a potential to substitute current NbN (NbTiN) HEB mixers in certain applications, e.g. observation of wide doppler broadened emission from extra-galactic objects or operation on spaceborne satellite based telescopes utilizing light weight closed cycle cryocoolers. For utilization in future space missions, further investigation is required. The following steps in \(\text{MgB}_2\) HEB mixer development should be performed:

- **Despite a small increase of noise temperature was demonstrated when LO frequency increased from 0.69 THz to 1.63 THz, the low noise performance should still be demonstrated at higher frequencies, up to 5 THz.**

- **HPCVD process should be improved in order to reduce degradation of \(T_c\) with the film thickness reduction in order to achieve low noise operation at bath temperatures \(>20\text{ K}\).**

- **Simultaneously, further development of the process is needed to be able to change the \(T_c\) of \(\text{MgB}_2\) films without changing other film parameters, e.g. in order to lower the \(T_c\) to reduce LO power requirements.**

- **Modification of fabrication process is required in order to improve the**
antenna/film contact and consequently to reduce contact resistance without increasing bolometer width.

- Currently used SiC substrates do not provide a possibility of HEB fabrication on thin membranes for realization of waveguide receivers. Other substrate materials should be tested, e.g. thin SiC on Si substrate.

- Stability of MgB$_2$ HEB mixers should be investigated by measuring Allan variance. Possibly, the development of receivers utilizing balanced HEB mixers scheme would be required.
Chapter 8

Summary of appended papers

Paper A

MgB$_2$ hot-electron bolometer mixers at terahertz frequencies

Submicron size HEBs were fabricated with no degradation of the initial film $T_c$ from a 20 nm MgB$_2$ MBE grown film with a $T_c$ of 22 K. In the direct detection mode, the maximum voltage responsivity was in the range of 1–2 kV/W at 1.63 THz and the optimal bias current is around 1/4-1/3 of the $I_c$ at 4.2 K. 1.63 THz radiation has the same effect on the HEB’s IV-curve as a rise in temperature indicating that the response of the device is bolometric.

Contribution: Device layout design. Fabrication process development. Fabrication and responsivity characterisation of HEBs with a higher $T_c$. Co-writing of the paper.

Paper B

Effect of the critical and operational temperatures on the sensitivity of MgB$_2$ HEB mixers

Results of the noise and gain bandwidth investigation of HEB mixers made from 10 nm thick MgB$_2$ films with a $T_c$ of 8.5 K and 20 nm thick MgB$_2$ film with a $T_c$ of 22.5 K are presented. At an LO frequency of 1.63 THz the minimum receiver noise temperature was 700 K with a NBW of 3.5 GHz and a gain of -18 dB for a device with a $T_c$ of 8.5 K. For a device with a $T_c$ of 22.5 K the corresponding values were 1700 K, 5 GHz and -15 dB. For the latter device the Tr was 2150 K at a bath temperature of 12 K, which is not achievable with Nb-compound based HEB mixers. Different methods for measurements of the HEB mixer gain and the output noise are presented and compared.

Contribution: Device layout design. Fabrication process development. Fabrication of the HEB with a higher $T_c$, part of THz characterisation of HEBs with low and high $T_c$. Writing of the paper.
Paper C

Study of MgB$_2$ ultrathin films in submicron size bridges

A custom built HPCVD system for MgB$_2$ ultrathin film deposition: construction, deposition process development, and optimization are discussed. Achieved films on SiC substrates have a $T_c$ ranging from 35 K (10 nm thick films) to 41 K (40 nm thick films). The 20 nm thick unpatterned film had a room temperature resistivity of 13 $\mu\Omega$cm, whereas it becomes 50 $\mu\Omega$cm in submicron size bridges with a $J_c$ (4.2 K) up to $1.2 \times 10^8$ A/cm$^2$. The lower value of resistivity corresponds to the higher of both $T_c$ and $J_c$. The surface roughness, measured with an AFM, is approximately 1.5 nm. Possibility of thinning down of MgB$_2$ film by Ar$^+$ ion-beam milling is studied.


Paper D

MgB$_2$ hot electron bolometer mixers for THz heterodyne instruments

Experimental investigation of the MgB$_2$ HEB mixers for low noise mixing at terahertz frequencies is presented. The GBW measured by mixing of two THz sources is inversely proportional to the film thickness and it is at least 6 GHz for 15 nm thick devices. Performance of MgB$_2$ HEBs was compared to performance of one of the NbN HEB mixers made for the Herschel Space Observatory (one of the flight units), for which both the GBW and the NBW was measured. MgB$_2$ HEB mixers show a GBW at least a factor of three broader compared to the NbN HEB measured in the same set-up.

Contribution: Device layout design. Fabrication process development. Fabrication of HEBs. DC and part of THz characterisation of HEBs.

Paper E

Wideband THz HEB mixers using HPCVD MgB$_2$ thin films

Results of experimental study of the GBW of MgB$_2$ HEB mixers at 0.1 THz and 0.4 THz are presented. Antenna integrated 0.25–1.5 um$^2$ area devices were made from thin MgB2 films deposited with a custom made HPCVD system. The GBW was found to be independent on the bias conditions, the bath temperature, and the LO frequency. At 0.69 THz and 23 K the noise temperature of this mixer was 3000 K (corrected for optical losses).

Contribution: Device layout design. Fabrication process development. Fabrication of HEBs. DC and part in THz characterisation of HEBs. Writing of the paper.
Paper F

Broadband MgB\textsubscript{2} Hot-Electron Bolometer THz Mixers operating up to 20 K

Performance of submicron size HEB mixers made from thin MgB\textsubscript{2} superconducting films is discussed. With a superconducting transition temperature of about 30 K, such THz mixers can operate with high sensitivity at temperatures up to 20 K. Due to very small dimensions LO power requirements are rather low. In the IF band of 1–3 GHz the double sideband receiver noise temperature is 1600 K at 10 K operation temperature, 2000 K at 15 K, 2500–3000 K at 20 K. The NBW is estimated to be 6–8 GHz.

Contribution: Device layout design. Fabrication process development. Fabrication of HEBs. DC and part in THz characterisation of HEBs. Co-writing of the paper.

Paper G

Low noise terahertz MgB\textsubscript{2} hot-electron bolometer mixers with an 11 GHz bandwidth

THz HEB mixers with a low noise temperature, a wide NBW, and a high operation temperature made from an 8 nm thick superconducting MgB\textsubscript{2} film are presented. A NBW of 11 GHz with a minimum noise temperature of 930 K at 1.63 THz and 5 K are obtained. At 15 K and 20 K, the noise temperature is 1100 K and 1600 K, respectively. From 0.69 THz to 1.63 THz the receiver noise increases by only 12%. Device current-voltage characteristics are identical when pumped with LOs from 0.69 THz up to 2.56 THz, and match well with IV curves at elevated temperatures. Therefore, the effect of the THz waves on the mixer is totally thermal, due to absorption in the $\pi$ conduction band of MgB\textsubscript{2}.

Contribution: Device layout design. Fabrication process development. Fabrication of HEBs. DC and part in THz characterisation of HEBs. Co-writing of the paper.

Paper H

Gain and noise in THz MgB\textsubscript{2} hot-electron bolometer mixers with a 30 K critical temperature

The detailed study of HEB mixers made from an 8 nm thick superconducting MgB\textsubscript{2} film is presented. Variation of the mixer characteristics such as noise temperature, gain, output noise, and LO power at 5 K, 15 K, and 20 K, and at 0.69 THz and 1.63 THz LO frequencies is investigated. The low noise performance is achieved in quite wide bias point range (5–10 mV). The main reason for the noise temperature to rise at higher temperatures is a reduction of the mixer gain, which occurs proportionally to the LO power reduction. On contrary, the output noise remains constant (for the same bias point). The mixer gain and output noise temperature are in the range of -(8–11) dB and 120–220 K, respectively.
Contribution: Device layout design. Fabrication process development. Fabrication of HEBs. DC and part in THz characterisation of HEBs. Co-writing of the paper.
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