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# ALMA Resolves C I Emission from the $\beta$ Pictoris Debris Disk

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## Abstract

The debris disk around  $\beta$  Pictoris is known to contain gas. Previous ALMA observations revealed a CO belt at  $\sim 85$  au with a distinct clump, interpreted as a location of enhanced gas production. Photodissociation converts CO into C and O within  $\sim 50$  a. We resolve C I emission at 492 GHz using ALMA and study its spatial distribution. C I shows the same clump as seen for CO. This is surprising, as C is expected to quickly spread in azimuth. We derive a low C mass (between  $5 \times 10^{-4}$  and  $3.1 \times 10^{-3} M_{\oplus}$ ), indicating that gas production started only recently (within  $\sim 5000$  a). No evidence is seen for an atomic accretion disk inward of the CO belt, perhaps because the gas did not yet have time to spread radially. The fact that C and CO share the same asymmetry argues against a previously proposed scenario where the clump is due to an outward-migrating planet trapping planetesimals in a resonance, nor can the observations be explained by an eccentric planetesimal belt secularly forced by a planet. Instead, we suggest that the dust and gas disks should be eccentric. Such a configuration, we further speculate, might be produced by a recent tidal disruption event. Assuming that the disrupted body has had a CO mass fraction of 10%, its total mass would be  $\gtrsim 3 M_{\text{Moon}}$ .

**Key words:** circumstellar matter – methods: observational – radiative transfer – stars: individual (beta Pictoris) – submillimeter: planetary systems – techniques: interferometric

## 1. Introduction

In debris disk systems, the continuous collisional destruction of larger bodies such as comets or asteroids produces abundant amounts of dust, with the smallest grains quickly removed by radiation pressure (Backman & Paresce 1993; Wyatt 2008). A debris disk provides evidence that planetesimal-sized bodies were formed during the earlier protoplanetary phase (Artymowicz 1997; Matthews et al. 2014) and gives us the opportunity to study the properties of the building blocks of planets. Studying these systems is therefore intimately linked to our efforts of understanding how planets form.

The debris disk around the young ( $23 \pm 3$  Ma; Mamajek & Bell 2014) A6V star (Gray et al. 2006)  $\beta$  Pictoris has been used as a laboratory to study the early evolution of planetary systems ever since its discovery by the *Infrared Astronomical Satellite* (Aumann 1985). Smith & Terrile (1984) obtained the first resolved image showing an edge-on disk. Since then, the properties of the dust disk have been extensively studied with observations at multiple wavelengths. Today, we know that the belt of parent bodies is located at  $\sim 100$  au (Dent et al. 2014) and that  $\beta$  Pic hosts a giant planet (e.g., Chilcote et al. 2017,

and references therein) with a semimajor axis of  $\sim 10$  au (Lecavelier des Etangs & Vidal-Madjar 2016; Wang et al. 2016), first imaged by Lagrange et al. (2009, 2010).

Even before the dust disk was discovered, evidence from optical and ultraviolet (UV) absorption lines suggested the presence of gas around  $\beta$  Pic (Slettebak 1975; Slettebak & Carpenter 1983). The  $\beta$  Pic disk is thus part of a small subsample of debris disks where gas has been detected. Currently, there are about 20 such gaseous debris disks known (e.g., Redfield 2007; Moór et al. 2011; Roberge et al. 2014; Lieman-Sifry et al. 2016; Matrà et al. 2017b).

The spatial distribution of the gas around  $\beta$  Pic has been studied with resolved observations in the optical and recently with the Atacama Large Millimeter/submillimeter Array (ALMA). These data showed that the gas disk is radially extended (with some species traced out to several hundred au) and in Keplerian rotation (Olofsson et al. 2001; Brandeker et al. 2004; Nilsson et al. 2012; Dent et al. 2014). Besides this stable component, time-variable absorption features shifted with respect to the systemic velocity are attributed to exocomets evaporating in the vicinity of the star (e.g., Vidal-Madjar et al. 1994; Kiefer et al. 2014, and references therein). The latter phenomenon has also been seen around a number of other (mostly young) A-type stars (e.g., Welsh & Montgomery 2015, and references therein).

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Similarly to the dust, the gas in the  $\beta$  Pic disk is thought to be continuously produced from the destruction of solid material rather than leftover from the protoplanetary phase. Evidence for such a secondary scenario comes, for example, from theoretical arguments on the dynamical lifetime of the gas (Fernández et al. 2006). Also, models of the excitation of the CO 3–2 and 2–1 transitions observed by ALMA imply that not enough  $\text{H}_2$  is present in the disk to shield CO from photodissociation over the lifetime of the disk, thus the necessity of a gas replenishment mechanism (Matrà et al. 2017a). Studying this secondary gas opens up the interesting possibility to constrain the composition of the parent bodies (e.g., Kral et al. 2016; Matrà et al. 2017a, 2018).

To date, multiple metallic species such as C, O, Na, Al, or Ca have been detected (e.g., Brandeker et al. 2004; Roberge et al. 2006; Brandeker et al. 2016). Recently, the first detection of hydrogen was reported by Wilson et al. (2017). CO remains the only molecule detected so far (e.g., Dent et al. 2014; Matrà et al. 2018). The observed elemental abundances are strikingly different from solar abundances. While the abundance of H is much lower than solar (Wilson et al. 2017), C is highly overabundant with respect to other metals (Roberge et al. 2006; Cataldi et al. 2014). Fernández et al. (2006) showed that the carbon overabundance provides a braking mechanism, preventing other metals that are strongly affected by radiation pressure (such as Na) from being quickly ejected from the system. Carbon also plays a crucial role in determining the excitation conditions of atomic fine-structure or molecular rotational transitions (e.g., Zagorovsky et al. 2010). This is because in a secondary, hydrogen-depleted disk, collisional excitation is likely dominated by electrons, and ionization of carbon is the main electron source.

Using spectrally resolved observations of C II with *Herschel*<sup>15</sup>/HIFI, the spatial distribution of carbon was constrained by Cataldi et al. (2014). They found that most of the carbon gas is located at  $\sim 100$  au, with tentatively more emission from the southwest (SW) side of the disk. At about the same time, ALMA spatially resolved CO 3–2 emission, revealing a clump of emission on the SW side of the disk at  $\sim 85$  au (Dent et al. 2014). The CO clump coincides with a radial peak of the millimeter continuum (Dent et al. 2014) and a clump seen at mid-IR wavelengths (Telesco et al. 2005; Li et al. 2012). Dissociation by interstellar UV photons limits the lifetime of CO in the disk to significantly less than an orbit (Visser et al. 2009). It is thus clear that CO needs to be produced continuously and is a source for both C and O. This might provide a natural explanation for the observed supersolar abundance of C with respect to metals such as Na (Xie et al. 2013). The CO itself is believed to be derived from the destruction of volatile-rich, cometary bodies, where the clump corresponds to a location of increased collision rate and thus gas production. Several hypotheses have been put forward to explain the existence of the clump. First, it could be the location of a giant collision. The clump then results from the fact that the orbits of the collision debris always all go through the collision point (Jackson et al. 2014). Second, the clump could be due to cometary bodies trapped in a resonance with an outward-migrating yet unseen giant planet (Wyatt 2003, 2006). Using ALMA follow-up observations of the CO 2–1 transition

at higher resolution, Matrà et al. (2017a) dismissed the giant collision scenario based on the large radial extent of the clump. Third, Nesvold & Kuchner (2015) proposed that the interaction between a spiral density wave and a vertical displacement wave, both induced by  $\beta$  Pic b, can produce an azimuthally asymmetric collision rate.

Assuming that indeed all C and O is derived from the dissociation of CO, Kral et al. (2016) modeled the hydrodynamical evolution of carbon and oxygen in the disk. They assumed that the produced atomic gas is subject to the magnetorotational instability (MRI) and predict an atomic accretion and decretion disk (Xie et al. 2013; Kral & Latter 2016).

CI was previously seen in absorption against  $\beta$  Pic (Vidal-Madjar et al. 1994; Jolly et al. 1998; Roberge et al. 2000). Recently, Higuchi et al. (2017) presented the first observation of CI in emission. In this paper, we present the first spatially resolved observations of CI, revealing its distribution in the disk. Our paper is organized as follows. We describe the observations in Section 2 and present the results in Section 3. In Section 4, we present simple gas emission models to study the total mass and spatial distribution of the carbon gas. We discuss our results in Section 5 and conclude in Section 6.

## 2. Observations and Data Reduction

We observed the  $\beta$  Pic disk using band 8 receivers of ALMA on 2015 December 19 during the ALMA cycle 3 Early Science campaign (project ID 2013.1.00459.S, PI: Brandeker). The observations were split into two execution blocks (EBs). The total integration time was 2.1 hr (with 1.2 hr on  $\beta$  Pic), and the median precipitable water vapor (pwv) was 0.6 mm with standard deviation of 0.1 mm. The array consisted of 36 antennas arranged in a hybrid configuration containing both short and long baselines ranging from 15 m to 6.3 km. In principle, we are thus sensitive to angular scales between  $\sim 0''.02$  and  $\sim 5''$  on the sky.<sup>16</sup> However, the visibilities from the longer baselines were affected by large atmospheric phase fluctuations and therefore flagged during the calibration process (see below). The observations were executed as a mosaic to obtain uniform sensitivity over the whole disk. One pointing was centered on the star, and two additional pointings were centered at  $\pm 6''$  along the position angle of the disk. The size of the primary beam is  $11''.8$ . Antenna elevations varied between  $27^\circ$  and  $60^\circ$ .

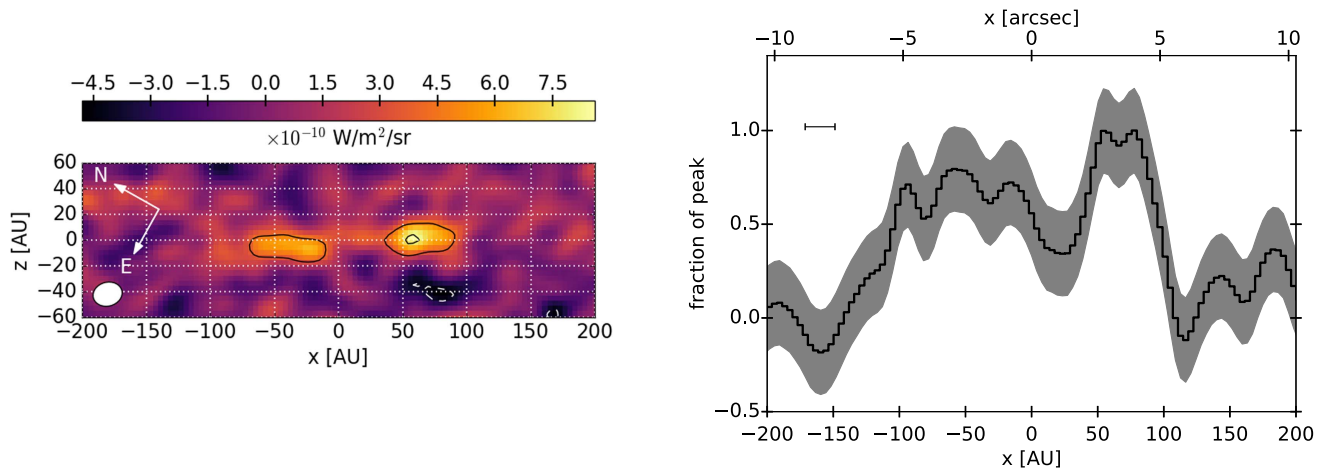
We placed three spectral windows, each with 1920 channels and a channel spacing of 488 kHz (total bandwidth 937.5 MHz), onto the following transitions: C I  $^3P_1\text{--}^3P_0$  at 492.16 GHz, CS 10–9 at 489.75 GHz, and SiO 11–10 at 477.50 GHz. For C I, this corresponds to a channel spacing of  $0.30 \text{ km s}^{-1}$  and an effective spectral resolution<sup>17</sup> of  $0.34 \text{ km s}^{-1}$  (spectral averaging factor  $N=2$ ). In addition, a fourth spectral window with 128 channels and a total bandwidth of 1875 MHz was placed at 479 GHz in order to observe the dust continuum.

The data were calibrated using CASA 4.7.0 (McMullin et al. 2007). We performed standard water vapor radiometer (WVR) calibration and system temperature corrections. The following calibration sources were observed: J0522–3627 (bandpass), J0538–4405 (phase), J0519–4546, and J0538–4405

<sup>15</sup> *Herschel* is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.

<sup>16</sup> See ALMA Cycle 6 Technical Handbook, Section 3.6 (Spatial Filtering), <https://almascience.nao.ac.jp/documents-and-tools/cycle6/alma-technical-handbook>.

<sup>17</sup> See ALMA Cycle 6 Technical Handbook, Table 5.2.



**Figure 1.** Left: moment 0 of the C I 492 GHz emission from the  $\beta$  Pic disk. Contours are drawn at intervals of  $3\sigma$ , with negative contours drawn as dotted lines. The beam is illustrated as a white ellipse in the lower left. The dashed rectangle illustrates the region used to measure the total flux. Right: emission profile along the  $x$ -axis of the moment 0 map, normalized to the peak value. The gray shaded area illustrates the  $\pm 1\sigma$  error interval. The symbol in the upper left shows the projection of the beam onto the  $x$ -axis.

(flux). However, we discarded the data from the two flux calibrators and instead used J0522–3627 to calibrate both bandpass and flux because this source had a significantly better measurement of its absolute flux in the ALMA Calibrator Source Catalog.

The antenna time-dependent gain calibration solutions were adversely affected by the high atmospheric phase fluctuations on the longer baselines. We therefore flagged all baselines longer than 2 km, effectively removing one-third of the baselines. In addition, two bad antennas (DA44 and DA54) were also flagged. This allowed us to derive acceptable calibration solutions.

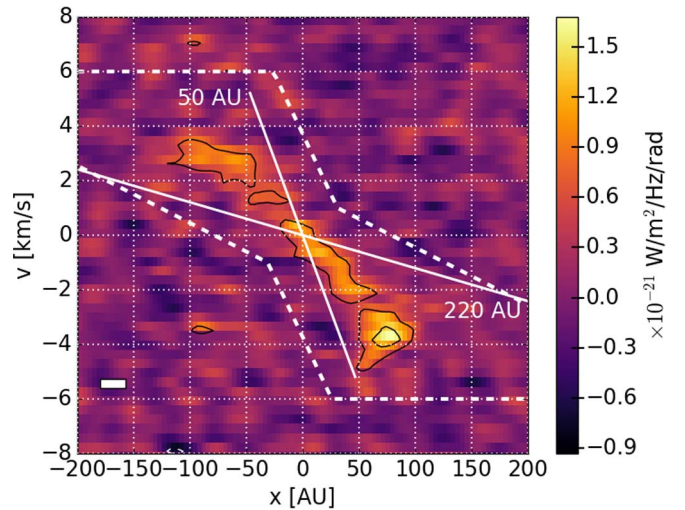
For the spectral windows placed onto emission lines, we performed continuum subtraction using the `uvcontsub` task within CASA. We then imaged the visibilities using the `CLEAN` task within CASA. In order to increase our surface brightness sensitivity, we applied a taper of  $1''$ , thus significantly reducing the contribution of the remaining long baselines (at 492 GHz, an angular scale of  $1''$  corresponds to a baseline length of 126 m). We also produced a continuum image using `CLEAN` with the same taper, combining all spectral windows except the one centered on CS 10–9, which is in a region of bad atmospheric transmission and therefore particularly noisy.

Because of the low antenna elevations and the suboptimal array configuration, the sensitivity of the data is significantly worse than requested. Consequently, the data initially did not pass Quality Assurance 2 (QA2). However, we still decided to publish the data, as the signal-to-noise ratio (S/N) is sufficient to provide new information on the  $\beta$  Pic system.

### 3. Results

#### 3.1. Line Emission

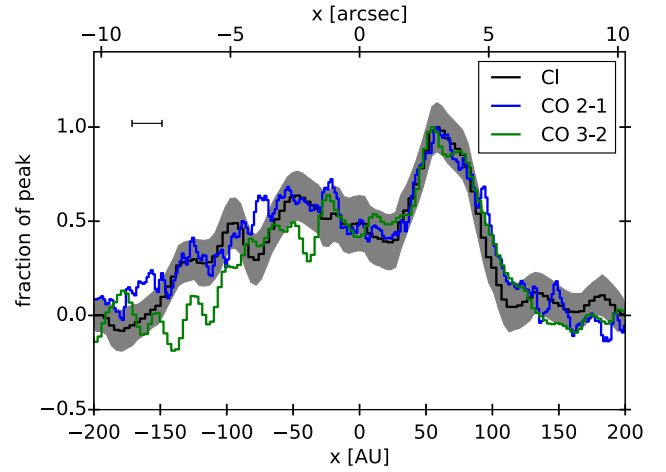
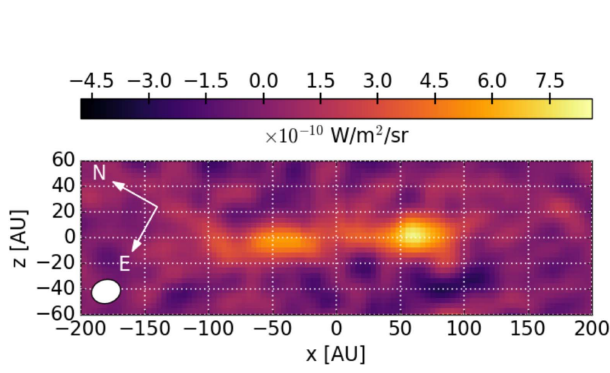
The CS 10–9 and SiO 11–10 lines remained undetected. We detect and resolve C I  $^3P_1$ – $^3P_0$  emission. The left panel of Figure 1 shows the moment 0 map, produced by integrating the data cube along the spectral axis within  $\pm 6 \text{ km s}^{-1}$  (with respect to the systemic velocity of the star, assumed to be  $v_{\text{heliocentric}} = 20.5 \text{ km s}^{-1}$ ; Brandeker 2011). The figure has been rotated to align the horizontal direction with the main dust disk (position angle of  $+29^\circ 3'$ ; Lagrange et al. 2012). The beam size is  $1''.18 \times 0''.95$  ( $23 \text{ au} \times 19 \text{ au}$ ) with a major-axis position angle with respect to the north of  $44^\circ$ . We achieve a  $1\sigma$  sensitivity of  $\sim 2.3 \times 10^{-17}$



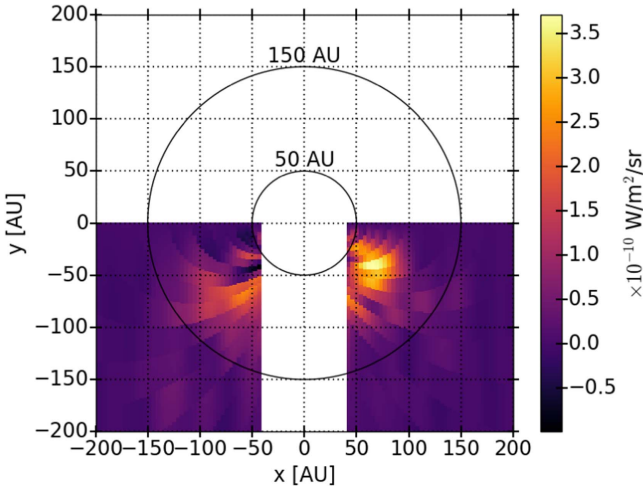
**Figure 2.** Position–velocity diagram of the C I emission. Contours are drawn at  $3\sigma$  intervals. The spectro-spatial resolution is illustrated in the lower left by the white rectangle. The two solid lines show the radial velocity (for circular Keplerian orbits around a  $1.75 M_\odot$  star seen edge-on) at 50 and 220 au, the approximate radial extent of the CO (Matrà et al. 2017a). The dashed lines show the region in  $x$ – $v$  space used to derive a moment 0 map and emission profile with improved S/N.

$\text{W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$  ( $\sim 70 \text{ mJy beam}^{-1}$ ) in the individual channels. We perform photometry by considering a rectangular aperture extending  $\pm 115 \text{ au}$  in the horizontal direction (measured from the stellar position; see Figure 1) and  $\pm 30 \text{ au}$  in the vertical direction (measured from the midplane). This yields a total flux of  $(1.6 \pm 0.2) \times 10^{-19} \text{ W m}^{-2}$  ( $9.8 \pm 1.4 \text{ Jy km s}^{-1}$ ), where the error is random without any systematic calibration uncertainty taken into account. We did not correct for the primary beam, as it changes the total flux only within the quoted error bars (the same applies for the continuum; Section 3.3). The measured flux is consistent with the value of  $(1.7 \pm 0.4) \times 10^{-19} \text{ W m}^{-2}$  ( $10.3 \pm 2.3 \text{ Jy km s}^{-1}$ ) derived from single-dish observations by Higuchi et al. (2017). The same method yields  $3\sigma$  upper limits of  $5.9 \times 10^{-20} \text{ W m}^{-2}$  ( $3.6 \text{ Jy km s}^{-1}$ ) for CS 10–9 and  $2.9 \times 10^{-20} \text{ W m}^{-2}$  ( $1.8 \text{ Jy km s}^{-1}$ ) for SiO 11–10.

The right panel of Figure 1 shows the emission profile along the  $x$ -axis of the moment 0 map, obtained by integrating within  $\pm 30 \text{ au}$  in the vertical direction. Both the moment 0 map and



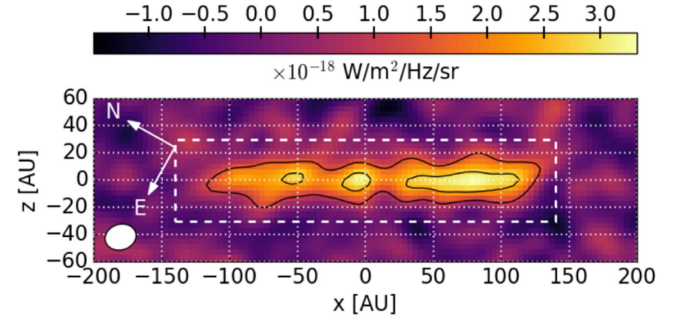
**Figure 3.** Same as Figure 1, but using only the region in  $p$ - $v$  space illustrated by the dashed lines in Figure 2 to improve the S/N. For the moment 0 (left), no contours are shown since, by construction, the noise levels are now nonuniform and depend on  $x$ . The color scale is the same as in Figure 1. In the emission profile (right) we also included the CO 3–2 and 2–1 emission as observed by Matrà et al. (2017a).



**Figure 4.** Deprojection (face-on view) of the C I emission derived from the  $p$ - $v$  diagram (Figure 2), where we chose to place all flux in front of the sky plane (the line of sight runs in the positive direction of the  $y$ -axis). Points with  $|x| < 40$  au are masked.

the emission profile are suggestive of an asymmetry with a peak on the SW side of the disk. The same asymmetry is seen for the CO emission (Dent et al. 2014; Matrà et al. 2017a) and tentatively also for C II (Cataldi et al. 2014). However, the SW/NE flux ratio within the rectangular box of Figure 1 is not significant at  $0.9 \pm 0.2$  (we calculate the error on the ratio  $\frac{a}{b}$  by propagating the error like this:  $\sigma_{a/b}^2 = 1/b^2\sigma_a^2 + a^2/b^4\sigma_b^2$ ). The SW/NE ratio of the peaks in the emission profile is  $1.3 \pm 0.5$ . Thus, there is not necessarily more flux on the SW side of the disk, but the flux seems to be more compact.

Figure 2 shows the position–velocity ( $p$ - $v$ ) diagram (i.e., the data cube integrated along the vertical spatial direction within  $\pm 30$  au). This figure thus shows the radial velocity of the emission as a function of the projected position along the disk midplane. By using the  $p$ - $v$  diagram, we can constrain the radial distribution of the emission despite the edge-on orientation of



**Figure 5.** ALMA continuum image of the  $\beta$  Pic disk at 480 GHz. Contours are drawn at intervals of  $3\sigma$ . The white dashed rectangle indicates the region within which the flux was measured.

the disk. Indeed, Figure 2 also shows the radial velocity for circular Keplerian orbits at 50 and 220 au around a  $1.75 M_\odot$  star (Crifo et al. 1997), seen edge-on. This is the approximate radial extent of the CO as found by Matrà et al. (2017a). As can be seen, no significant C I emission is detected beyond these lines, suggesting that most C I emission is confined to the same region as the CO.

We may use the  $p$ - $v$  diagram to define a region in  $p$ - $v$  space that contains all significant emission. Then, when integrating over the spectral axis, we only take data points within this region into account (rather than everything within  $\pm 6$  km s $^{-1}$  as was done to produce Figure 1). The region is illustrated by the dashed lines in Figure 2, and the resulting moment 0 map and emission profile are shown in Figure 3. The SW/NE flux ratio (within the same box as in Figure 1) is now  $1.2 \pm 0.2$ . Most importantly, the S/N of the emission profile is significantly improved and the SW/NE asymmetry more clearly visible. We measure a SW/NE peak ratio of  $1.6 \pm 0.4$ . Thus, the significance of the peak ratio asymmetry is only marginal. However, in the right panel of Figure 3 we also show the profiles of the CO 3–2 and 2–1 emission (see Figure 2 of Matrà et al. 2017a), for which the SW/NE flux ratios are  $1.08 \pm 0.08$  (CO 2–1) and  $1.49 \pm 0.13$  (CO 3–2) and the peak ratios are  $1.42 \pm 0.14$  (CO 2–1) and

$1.51 \pm 0.14$  (CO 3–2). The C I emission follows the CO 2–1 emission surprisingly well, with the same distinct peak on the SW side of the disk and the same asymmetric extent (out to  $\sim 150$  au in the NE and  $\sim 100$  au in the SW). This suggests that the asymmetry is indeed real. This is a surprising result. The asymmetry in CO can be readily understood from its short (less than one orbit) lifetime due to photodissociation: if CO is primarily produced in a clump, photodissociation prevents CO from spreading azimuthally, thus preserving the asymmetry. On the other hand, the C produced from CO photodissociation is expected to spread in azimuth within a few orbits. In Section 5.5 we discuss possible solutions to this puzzle.

From the moment 0 maps, it is also apparent that the observed emission is slightly tilted, with the NE side below and the SW side above the midplane of the main outer disk (defined by  $z = 0$ ). A similar tilt is seen for CO (Dent et al. 2014; Matr  et al. 2017a). As is discussed by Matr  et al. (2017a), two reasons might be imagined for this observation: either the gas disk is indeed tilted with respect to the dust disk, or the tilt is a projection effect, resulting from an azimuthally asymmetric gas disk in combination with a slight deviation from a perfect edge-on inclination. Interestingly, the inner dust disk seen in scattered light has a similar tilt (e.g., Milli et al. 2014; Apai et al. 2015; Millar-Blanchaer et al. 2015). This dust component, known as *warp* or *secondary disk*, is localized inward of 80 au (Lagrange et al. 2012) and seems thus slightly inward of the gas. Also, it has already been suggested that this inner dust disk is not perfectly edge-on (e.g., Milli et al. 2014; Millar-Blanchaer et al. 2015).

The reader interested in the procedures to estimate the errors quoted in this section is referred to Appendix A.

### 3.2. Deprojection of the C I Emission

Assuming that the gas follows circular Keplerian orbits, we can use the  $pv$  diagram (Figure 2) to obtain a face-on view of the emission (e.g., Dent et al. 2014; Matr  et al. 2017a). Indeed, each point in the  $pv$  diagram corresponds to two points in the  $xy$ -plane of the disk (where we define  $y$  as the coordinate running along the line of sight), one in front of and one behind the sky plane. There remains the degeneracy of how to distribute the flux of a given  $pv$  point among the two points in the  $xy$ -plane. As discussed by Matr  et al. (2017a), the degeneracy can be broken if the disk is not perfectly edge-on. However, for simplicity, we follow Dent et al. (2014) and assume that the disk is edge-on. Our primary interest is to illustrate the radial extent of the emission and the position of the clump. We thus choose to place all flux in front of the sky plane, but other physically motivated choices are possible (Dent et al. 2014). Figure 4 shows the deprojection. Points of the  $pv$  diagram with  $|x| < 40$  au were masked because the radial velocity in this region tends toward zero for all radii, i.e., it becomes difficult to assign a radius to a given radial velocity. Emission is seen approximately out to 150 au. The clump appears at a similar position angle as seen in CO (Dent et al. 2014). Details of the deprojection procedure are described in Appendix C. Since the optical depth of the emission is not negligible, the deprojection does not show the true distribution of the emission in the  $xy$ -plane, but rather how much emission the observer receives from various locations in the  $xy$ -plane.

### 3.3. Continuum

The continuum image at  $\sim 485$  GHz is shown in Figure 5. The  $1\sigma$  noise level is  $4.4 \times 10^{-19} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$  ( $1.3 \text{ mJy beam}^{-1}$ ). The beam size is  $1''.19 \times 0''.96$  ( $23 \text{ au} \times 19 \text{ au}$ ) with the position angle of the major axis being  $46^\circ$ . We measure a total flux of  $(1.12 \pm 0.07) \times 10^{-27} \text{ W m}^{-2} \text{ Hz}^{-1}$  ( $112 \pm 7 \text{ mJy}$ ) in the rectangular region ( $\pm 140$  au from the star along  $x$  and  $\pm 30$  au from the midplane along  $z$ ) indicated in the figure (see Appendix A for details on the error calculation). The measured flux is consistent with a Rayleigh–Jeans extrapolation of the flux measured by ALMA at  $870 \mu\text{m}$  (Dent et al. 2014) and is a factor of  $\sim 2$  below what is expected from the infrared to millimeter SED fit by Vandenbussche et al. (2010).

As was already seen in the ALMA data by Dent et al. (2014), the continuum is brighter on the SW side of the disk at projected separations between 50 and 100 au. However, the SW/NE integrated flux ratio is only  $1.17 \pm 0.14$ . In any case, the asymmetry is analogous to what is seen in thermal mid-IR images between 8.7 and  $18.3 \mu\text{m}$  (Telesco et al. 2005), as well as for C and CO.

## 4. Modeling

### 4.1. Simple Estimation of the Total Carbon Mass

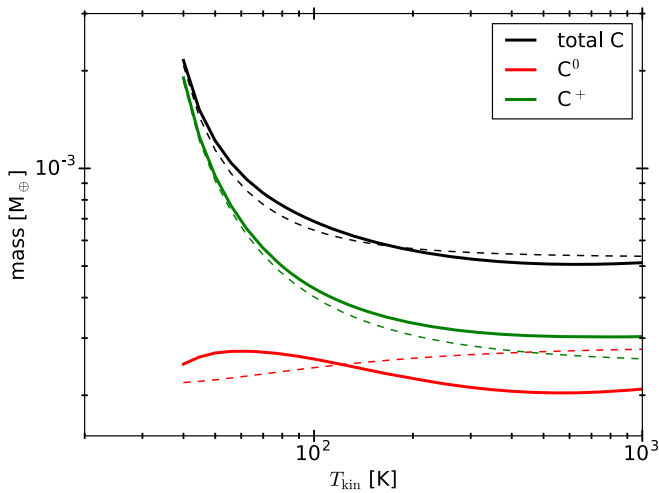
In this section, we estimate the total carbon mass in the  $\beta$  Pic disk under some simplifying assumptions. With a 1D model, we want to reproduce the C I flux measured in the present work and the C II flux measured with *Herschel*/PACS (Pilbratt et al. 2010; Poglitsch et al. 2010) by Brandeker et al. (2016; ObsID 1342198171) (we sum the flux values of the PACS spaxels listed in their Table 1). *Herschel*/HIFI also measured the C II flux (Cataldi et al. 2014). However, the flux measured by PACS is likely a better estimate of the total C II flux from the disk, because the HIFI half-power beam width is only  $\sim 200$  au.

We need to compute the statistical equilibrium (SE) of the level populations, as in general the emission cannot be assumed to be in local thermal equilibrium (LTE). The gas in the  $\beta$  Pic disk is thought to be of secondary origin and thus depleted in hydrogen (e.g., Matr  et al. 2017a). We thus assume that the dominant collider species is electrons and that photoionization of carbon is the main electron source (Fern ndez et al. 2006; Kral et al. 2016), i.e., the density of ionized carbon equals the electron density. Under these assumptions, the total carbon mass is estimated in two steps. For a given kinetic temperature, we first determine the amount of ionized carbon necessary to reproduce the C II emission. The second step is to determine the amount of neutral carbon necessary to reproduce the C I flux observed by ALMA, using the electron density derived in the first step.

To solve the SE and radiative transfer, we use `pythonradex`,<sup>18</sup> a python implementation of the RADEX code (van der Tak et al. 2007) with atomic data from the LAMDA database<sup>19</sup> (Sch ier et al. 2005). This code uses an escape probability formalism to solve the radiative transfer and assumes the geometry of a uniform sphere. In general, the radiative transfer depends on the geometry of the emitting region. The gas observed around  $\beta$  Pic is clearly nonspherical and nonsymmetric. The assumption of a uniform sphere is thus a clear

<sup>18</sup> <https://github.com/gica3618/pythonradex>

<sup>19</sup> <http://home.strw.leidenuniv.nl/~moldata/>



**Figure 6.** Mass of  $C^0$ ,  $C^+$ , and total C (derived from the model described in Section 4.1) as a function of the assumed kinetic temperature. For the full lines, the statistical equilibrium has been solved, while for the dashed lines, LTE has been assumed.

limitation of this model. The masses derived here should therefore be considered first-order estimates.

We choose the size of the sphere such that its volume corresponds to the volume of an elliptic torus with semimajor axis of 35 au in the radial direction and semiminor axis of 10 au in the vertical direction (see Figures 1–3). Note that even in the optically thin case, such an assumption on the scale over which the emission is produced is necessary, unless the emission is in LTE. This is because for a given mass the electron density depends on the assumed volume.

We include radiative excitation and de-excitation (hereafter simply (de-)excitation) by the cosmic microwave background (CMB), the stellar radiation (at 85 au), and the dust continuum, where the latter is taken at 85 au as seen in Figure B1 of Kral et al. (2017) and is the dominant component. However, it turns out that including radiative (de-)excitation from these sources does not change our results because (de-)excitation is dominated by collisions and spontaneous emission.

We then consider a wide range of kinetic temperatures  $T_{\text{kin}}$  from 40 to 1000 K. For lower temperatures, the C II line quickly becomes strongly optically thick such that meaningful constraints on the mass are no longer possible (i.e., the model cannot reproduce the observed flux regardless of how much the mass is increased). However, based on our more detailed modeling in Section 4.2, we deem lower temperatures unlikely. Detailed thermodynamical modeling by Kral et al. (2016) also suggests that the temperature is above  $\sim 50$  K within 100 au, although in their model the temperature drops to 20 K at 150 au.

Figure 6 shows the derived total carbon mass as a function of  $T_{\text{kin}}$ . The figure also shows the individual  $C^0$  and  $C^+$  masses. To assess the importance of non-LTE effects, we also show corresponding curves for which LTE has been assumed. Both C I and C II are, generally speaking, close to LTE. For higher temperatures, the  $C^0$  mass required to reproduce the observed C I flux is *higher* in LTE than in non-LTE. This simply happens because in LTE higher levels get populated more quickly with increasing temperature, thus depopulating the level that produces the C I emission. The maximum optical depths

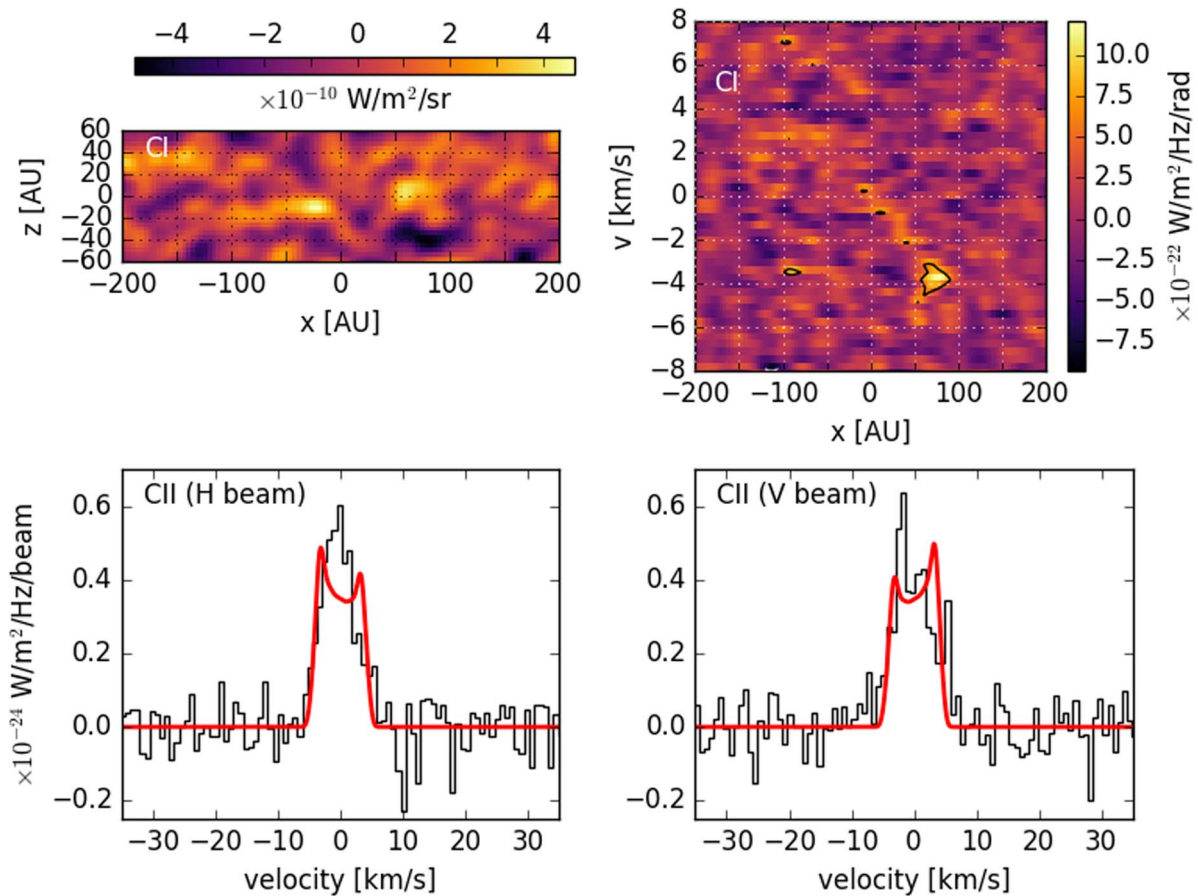
encountered for the considered temperature range are 0.5 for C I and 3.9 for C II.

From Figure 6, we determine a total carbon mass between  $5 \times 10^{-4}$  and  $3.1 \times 10^{-3} M_{\oplus}$ . The lower bound is quite robust to changes of the size of the emitting region, as it is close to the LTE value. For example, increasing or decreasing the radius of the emitting sphere by 50% does not change the lower bound by more than 15%. On the other hand, it is clear that the upper bound is more uncertain, as it can quickly increase if one allows for lower temperatures and/or smaller emitting volumes (i.e., increased optical depth). Another parameter that can strongly affect the optical depth (and thus the upper bound of the mass range) is the assumed line broadening parameter. Here we used  $b = 0.57 \text{ km s}^{-1}$ , derived in Appendix B.

Previous studies estimating the carbon gas mass in the  $\beta$  Pic disk had only the C II flux and line profile at disposal. These more detailed models derived higher masses by using the spectrally resolved C II observations from *Herschel*/HIFI: Cataldi et al. (2014) obtained  $1.3 \times 10^{-2} M_{\oplus}$ , while Kral et al. (2016) derived  $1.5 \times 10^{-2} M_{\oplus}$  (the latter study also used an upper limit on the C I flux). In the Kral et al. (2016) model, the total C mass is dominated by ionized carbon that is located beyond  $\sim 100$  au. The C I flux is of little importance for the total C mass budget of that model. The discrepancy thus cannot be explained by the fact that we include the C I measurement. On the other hand, most of the carbon in the Cataldi et al. (2014) model is located between 150 and 300 au with an ionization fraction of roughly 50%, i.e., there is a significant contribution of neutral carbon to the total mass. However, our ALMA data show no C I emission beyond  $\sim 120$  au. That model indeed overpredicted the C I flux by a factor of  $\sim 20$ , suggesting that it contains too much neutral carbon, partially explaining the difference in the mass estimates. But Cataldi et al. (2014) also derived a higher mass of ionized carbon compared to our estimate. In addition, their fit to the resolved C II line profile (see their Figure 2(b)) clearly suggests that C II emission beyond 150 au is needed to fit the line core (this is also an issue for our 3D models [Section 5.2], which generally do a bad job in fitting the C II line core). So maybe there is largely ionized carbon gas beyond  $\sim 150$  au present and the reason why we derive a lower ionized carbon mass here is because we assumed (based on the C I data) a too small volume (i.e., too high density and thus more excitation, and therefore less mass needed). However, even when increasing the volume of our 1D model, we still derive a lower mass of ionized carbon compared to Kral et al. (2016) and Cataldi et al. (2014) and thus cannot fully resolve the discrepancy, which might be due to the different assumptions of the models. The relatively small HIFI beam (FWHM of  $\sim 200$  au) could also play a role. For example, deviations from axisymmetry in the distribution of ionized carbon could introduce additional uncertainty in the mass estimates of Cataldi et al. (2014) and Kral et al. (2016) since C II emission from large radii is only detected by HIFI if it arises close to the line of sight toward the star.

#### 4.2. 3D Modeling

In this section, we model the 3D spatial distribution of the carbon gas using our new ALMA observations of C I and the previously published spectrally resolved *Herschel*/HIFI observation of C II



**Figure 7.** Comparison of the uniform ring model to the data. The top row shows the residual moment 0 map (left) and  $pv$  diagram (right) for the CI emission. Contours are in steps of  $3\sigma$ . The bottom row compares the modeled CII emission (red lines) to the HIFI data (black lines).

(Cataldi et al. 2014; ObsID 1342238190). For a given, arbitrary distribution of carbon gas, we first solve the ionization balance in each grid cell. We use the ionization rate from Zagorovsky et al. (2010) (scaled with distance to the star) and assume that the gas is optically thin to ionizing photons. The star is the main source of ionizing photons, but ionization from the interstellar radiation field (ISRF) is also included. The ionization balance is solved analytically by assuming that all electrons come from the photoionization of carbon. The ionization fraction thus only depends on the distance to the star, the local gas density, and the kinetic temperature (via the recombination coefficient). Next, we use the derived electron density to solve the SE of the level populations using atomic data from the LAMDA database. The following processes can (de)excite an atom: spontaneous emission, collisions with electrons (we neglect other colliders), and radiative (de)excitation by line photons and the background radiation field, where the latter is assumed to be composed of the CMB, the star, and the dust continuum. For the dust continuum, we employ the field shown in Figure B1 of Kral et al. (2017) (that figure actually shows the field in the midplane of the disk at the position angle of the clump [L. Matr  2018, private communication], but for simplicity, we only take the radial dependence into account). In principle, a full radiative transfer computation is necessary to solve the SE. However, we take a simplified approach and assume that the line emission is essentially optically thin. Basically, while the emission can become optically thick along the disk midplane (in

our best-fit models, the maximum optical depth is typically of the order of 1), it is optically thin in the vertical direction, i.e., the photon escape fraction is high. Thus, we assume that the background field is not attenuated by the gas (all atoms are subject to the full background field) and that (de)excitation by line photons can be neglected. These assumptions make the SE easy to solve. We further discuss this approximation in Appendix D. The background radiation turns out to be unimportant for our models.

Having solved the SE, we compute the emitted spectrum for each grid cell, redshifting or blueshifting it according to its radial velocity. The final step is then to ray-trace the emission along the line of sight to take optical depth into account. The result is a model data cube that can be compared to observations. For simplicity, we consider isothermal models and fix  $T_{\text{kin}} = 75 \text{ K}$  everywhere. We found that for lower temperatures the CI/CII flux ratio tends to be too high, while the inverse is true for higher temperatures.

To compare to the CII data, we take the corresponding model data cube, multiply by the HIFI beam, and integrate spatially to get a model HIFI spectrum (Cataldi et al. 2014). For the CI ALMA observations, we convolve the model data cube to the same spatial and spectral resolution as the observations and multiply by the primary beam. The residual moment 0 maps (respectively  $pv$  diagrams) shown in Figures 7, 8, and 11 are obtained by subtracting the model moment 0 map ( $pv$  diagram) from the data moment 0 map ( $pv$  diagram) shown in Figure 1 (Figure 2).

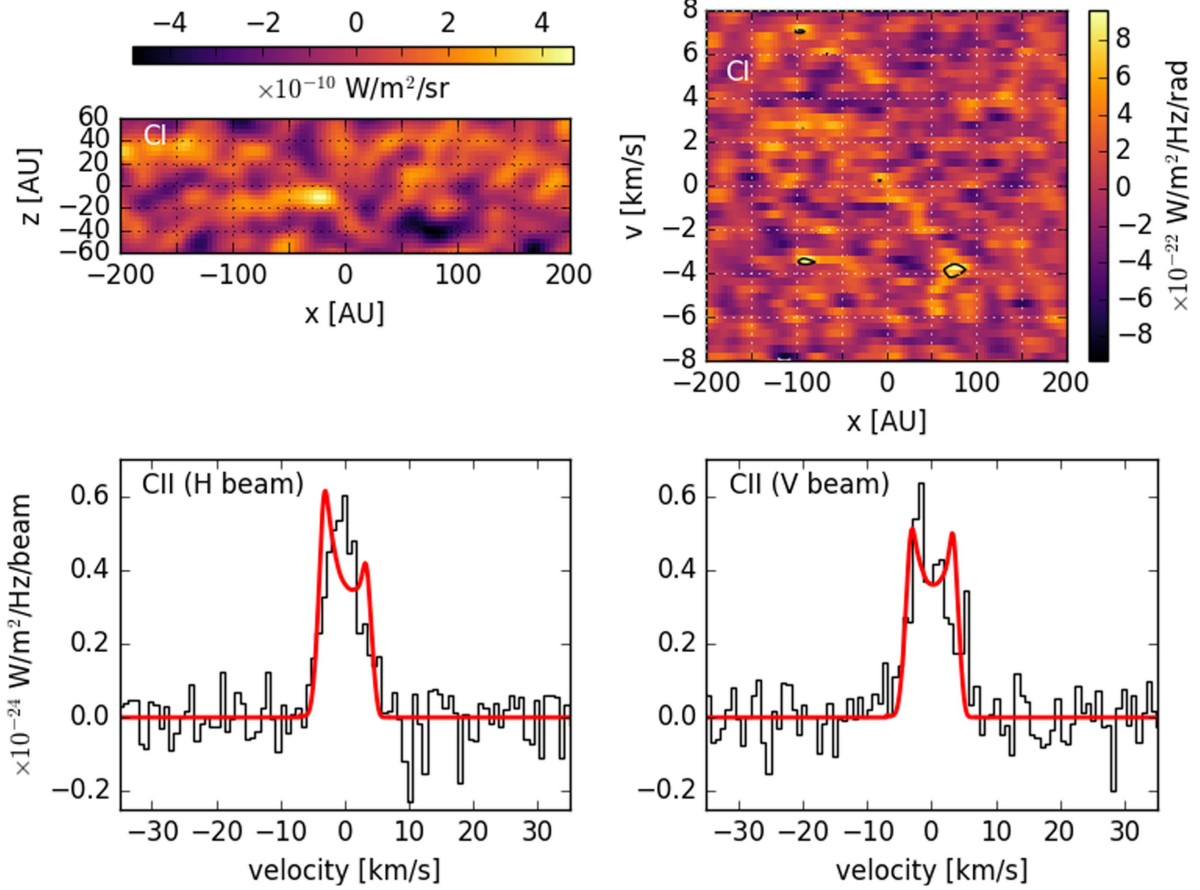


Figure 8. Same as Figure 7, but for the “ring + clump” model.

#### 4.2.1. Uniform Ring Model

We first consider a simple, symmetric model consisting of a ring with uniform surface density. The number density reads

$$n_{\text{ring}}(r, z) = \begin{cases} \frac{\Sigma}{\sqrt{2\pi} H(r)} \cdot \exp\left(-\frac{z^2}{2(H(r))^2}\right) & \text{if } r_{\min} \leq r \leq r_{\max}, \\ 0 & \text{otherwise} \end{cases}, \quad (1)$$

where  $r$  and  $z$  are cylindrical coordinates (with  $z$  perpendicular to the disk midplane),  $H(r)$  is the scale height,  $r_{\min}$  and  $r_{\max}$  define the radial extent of the ring, and  $\Sigma$  is the constant surface density. The scale height in hydrostatic equilibrium for a vertically isothermal disk is given by (e.g., Armitage 2009)

$$H(r) = \sqrt{\frac{kTr^3}{\mu m_p GM_*}}, \quad (2)$$

with  $k$  the Boltzmann constant,  $T$  the temperature,  $m_p$  the proton mass,  $G$  the gravitational constant, and  $M_*$  the stellar mass. For the mean molecular weight  $\mu$ , we follow Matr  et al. (2017a) and assume  $\mu = 14$ . At 85 au and for  $T = 75$  K, the scale height is 4.2 au.

We compute a grid of models over the parameter space listed in the first four rows of Table 1. Note that we also test different values for the (dynamical) stellar mass that affects the orbital velocities (and scale height). To each model, we assign a  $\chi^2$  measure by using expressions analogous to Equation (2) in Booth et al. (2017) (we take the correlation of neighboring data

points into account by using an appropriate noise correlation ratio for each data set). We sum the  $\chi^2$  from the *Herschel*/HIFI data (C II) and the ALMA data (C I).

Figure 7 shows the C I residuals in the  $xz$  and  $xv$  plane, as well as the C II line emission of the model with the lowest  $\chi^2$ . The corresponding model parameters are given in Table 1. The model provides a decent fit to the data, but unsurprisingly it is not able to reproduce the clump observed in the SW. Thus, we consider a more complicated model by adding a clump to the uniform ring in the next section. Such a model has no direct physical justification but is useful to empirically constrain the spatial distribution of the gas and get an estimate of the gas mass.

#### 4.2.2. Uniform Ring with a Clump

The clump is modeled as

$$n_{\text{clump}}(x, y, z) = n_0 \cdot \exp\left(-\frac{(x - x_0)^2 + (y - y_0)^2}{2\sigma_{xy}^2}\right) \cdot \exp\left(-\frac{z^2}{2(H(r))^2}\right), \quad (3)$$

where  $x$  runs along the disk midplane in the sky plane and  $y$  along the line of sight (and  $x^2 + y^2 = r^2$ ). Furthermore,  $x_0 = r_c \cos(\phi_c)$  and  $y_0 = r_c \sin(\phi_c)$  designate the center of the clump, where we have defined  $r_c$  as the clump’s radial distance to the star and  $\phi_c$  as its azimuthal angle in the  $x$ - $y$ -plane. We fix  $\phi_c = -32^\circ$  (Matr  et al. 2017a). The standard deviation of the

**Table 1**  
Explored Parameter Space and Best-fit Values for the “Ring” and “Ring + Clump” Models Fitting  
the C I ALMA Data and the C II *Herschel*/HIFI Data Simultaneously

Parameter	Unit	min	max	$n$	Spacing	Best Fit	
						“Ring”	“Ring + Clump”
$M_*$	$M_{\beta\text{Pic}}$	0.6	1	3	lin	0.8	0.8
$M_{\text{ring}}$	$M_{\oplus}$	$2.7 \times 10^{-4}$	$2.7 \times 10^{-3}$	6	log	$6.7 \times 10^{-4}$	$6.7 \times 10^{-4}$
$r_{\text{min}}$	au	30	70	3	lin	50	50
$r_{\text{max}}$	au	120	160	3	lin	120	120
$M_{\text{clump}}$	$M_{\oplus}$	$2.7 \times 10^{-5}$	$2.7 \times 10^{-4}$	6	log	...	$1.1 \times 10^{-4}$
$r_c$	au	70	100	3	lin	...	70
$\sigma_{xy}$	au	20	40	3	lin	...	40
$\Sigma$	$\text{cm}^{-2}$	...	...	...	...	$2.4 \times 10^{16}$	$2.4 \times 10^{16}$
$n_{\text{mid}} (r = 85 \text{ au})$	$\text{cm}^{-3}$	...	...	...	...	140	140
$n_{\text{clump}}$	$\text{cm}^{-3}$	...	...	...	...	...	280

**Note.** The number of values explored for each parameter is denoted by  $n$ . We also indicate whether the values are uniformly distributed in linear or logarithmic space.  $M_{\text{ring}}$  and  $M_{\text{clump}}$  are the masses of the ring and the clump, respectively. The reference mass of  $\beta$  Pic is assumed to be  $M_{\beta\text{Pic}} = 1.75M_*$  (Crifo et al. 1997). We also list the constant surface density of the ring  $\Sigma$ , the midplane number density of the ring  $n_{\text{mid}}$  at 85 au, and, for the “ring + clump” model, the number density at the center of the clump  $n_{\text{clump}}$  resulting from the superposition of the ring and the clump.

**Table 2**  
Same as Table 1, but for the Parameter Space Explored by the Models with Eccentric Orbits

Parameter	Unit	min	max	$n$	Spacing	Best Fit
$M_*$	$M_{\beta\text{Pic}}$	0.6	1	3	lin	0.8
$M_{\text{tot}}$	$M_{\oplus}$	$2.0 \times 10^{-4}$	$3.3 \times 10^{-3}$	6	log	$6.2 \times 10^{-4}$
$e_{\text{min}}$	...	0	0.4	5	lin	0
$e_{\text{max}}$	...	0.1	0.5	5	lin	0.3
$r_{\text{per}}$	au	60	100	3	lin	80
$\omega$	deg	-135	135	7	lin	-45

**Note.** The total mass of the model is  $M_{\text{tot}}$ , the pericenter distance is  $r_{\text{per}}$ , and the argument of pericenter is  $\omega$ .

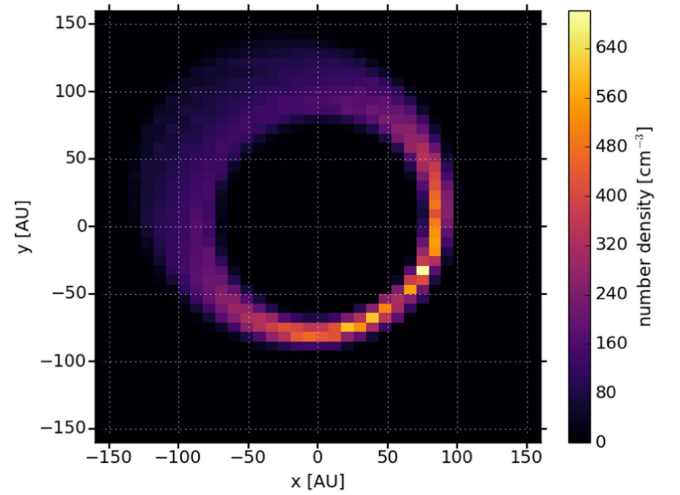
clump density distribution in the  $x$ - $y$ -plane is  $\sigma_{xy}$ , and the density at the center is  $n_0$ . The total carbon number density is then given by  $n_C = n_{\text{ring}} + n_{\text{clump}}$ . We compute models over the parameter space listed in Table 1. Figure 8 is the analog of Figure 7 for the best “ring + clump” model. As can be seen, the model does a slightly better job in modeling the clump.

#### 4.2.3. Eccentric Gas Distribution

The “ring + clump” model of the previous section is purely empirical and does not have a direct physical justification. As mentioned earlier, proposed mechanisms to get such a morphology are either a giant collision or resonant trapping of cometary bodies by a migrating giant planet. However, as we discuss in Section 5.5, based on our new C I data, we deem both of these possibilities unlikely.

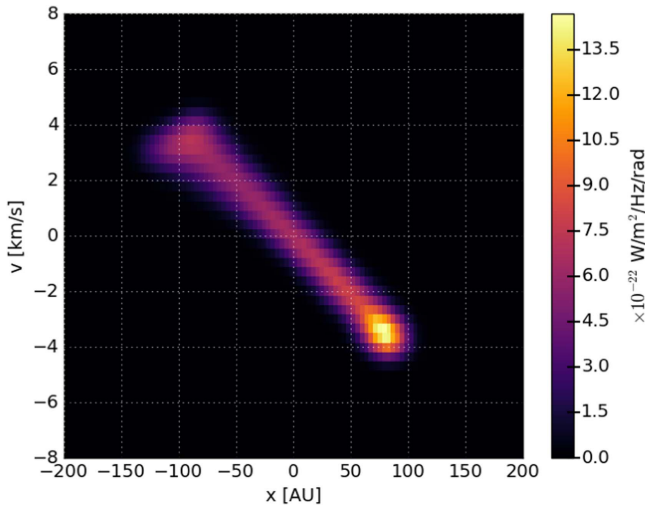
Another way to get a morphology with an emission clump on one side of the disk is to relax the assumption of circular orbits and instead consider gas on eccentric orbits. In Section 5.5.6, we discuss how such orbits could arise in the first place. As an example, we here consider a model where the eccentricity of the orbits is uniformly distributed between two values  $e_{\text{min}}$  and  $e_{\text{max}}$  and where all orbits share the same pericenter and the same argument of periapsis. The pericenter is then a region of higher density and can mimic a clump as seen in the observations.

The derivation of the gas density for this model is given in Appendix E. We again compute a grid of models with the parameters listed in Table 2. Figure 9 shows a face-on view of



**Figure 9.** Face-on view (midplane number density) of the C gas for the best-fit model with eccentric orbits described in Section 4.2.3.

the midplane carbon gas density, and Figure 10 shows the  $p$  $v$  diagram of the modeled C I emission. As is seen in Figure 11, this model is similarly effective in reproducing the observed C I emission, although it has some difficulties in reproducing the C II line. We emphasize that the purpose of this model is merely to demonstrate that eccentric gas orbits are able to reproduce the general morphology with the clump. A more detailed model will be presented in a forthcoming paper.



**Figure 10.** The  $pv$  diagram of the C I emission for the best-fit model with eccentric orbits, degraded to the spectro-spatial resolution of the ALMA data.

An interesting consequence of eccentric orbits is that the gas along the line of sight toward the star has nonzero radial velocity. Thus, emission (or absorption) toward the star is shifted with respect to the systemic velocity. For example, our best-fit model predicts that the emission peak toward the star appears  $0.4 \text{ km s}^{-1}$  blueshifted. Another consequence is an additional velocity broadening compared to the circular case, with broadening parameter  $b_{\text{ecc}} \approx 0.4 \text{ km s}^{-1}$  (this is smaller than and thus consistent with the broadening measured from the  $pv$  diagram; see Appendix B). The velocity shift and broadening depend on the eccentricity and orientation of the disk. To verify this velocity shift and constrain the model, we would need to know the absolute stellar radial velocity to better accuracy than  $\sim 80 \text{ m s}^{-1}$  (for a  $5\sigma$  detection of the shift).

The column densities of neutral carbon toward the star for the three models discussed in Sections 4.2.1–4.2.3 are  $(6\text{--}7) \times 10^{16} \text{ cm}^{-2}$ , slightly above the value of  $(2\text{--}4) \times 10^{16} \text{ cm}^{-2}$  measured in absorption by Roberge et al. (2000). For ionized carbon, the models range between  $5 \times 10^{16} \text{ cm}^{-2}$  and  $1.2 \times 10^{17} \text{ cm}^{-2}$ , while Roberge et al. (2006) report  $2 \times 10^{16} \text{ cm}^{-2}$ .

#### 4.3. Absence of an Atomic Accretion Disk

Recently, Kral et al. (2016) presented a model that computes the temperature, ionization, and hydrodynamical evolution of the atomic carbon and oxygen in the  $\beta$  Pic disk. In this model, the atomic gas is produced in a parent belt from photodissociation of CO and then evolves viscously under the influence of the MRI, i.e., it forms an accretion and decretion disk. Kral et al. (2016) predict that the carbon is mostly neutral in the inner parts of the accretion disk.

However, Figures 2 and 4 indicate that no atomic accretion disk has formed (yet), as there seems to be little C I emission inside of  $\sim 50 \text{ au}$  (but see also Section 5.4). To confirm this, we compute the C I emission expected from the model and compare it to our data. We thus take the Kral et al. (2016) distribution of neutral carbon and electrons, temperature profile, and scale height (see their Figure 9) and compute the C I emission with the methods described in Section 4.2. Figure 12 shows the moment 0 map and  $pv$  diagram of the model and the residuals when subtracting the model from the

ALMA C I data. It is clear from this figure that the accretion profile predicted by Kral et al. (2016) produces too much C I emission in the inner regions of the disk. This is also clearly visible in the  $pv$  diagram, where too much emission is present at high velocities.

## 5. Discussion

### 5.1. Dynamical Mass of the Star

For all the 3D models described in Section 4.2, the grid searches indicate that a dynamical mass of  $0.8M_*$  (with  $M_* = 1.75 M_\odot$  the assumed stellar mass; Crifo et al. 1997) is preferred to reproduce the data. While this result has to be interpreted with care given that we did not derive any error bars, it is interesting to note that Olofsson et al. (2001) derived the same  $0.8M_*$  dynamical mass by modeling spatially and spectrally resolved Na I emission. They ascribed their finding to radiation pressure opposing the gravity of the star. In fact, radiation pressure on Na is so strong that a braking mechanism is required to keep it on the observed Keplerian orbits and prevent it from being blown out (e.g., Liseau 2003; Brandeker et al. 2004). Fernández et al. (2006) suggested that all species affected by radiation pressure are largely ionized and coupled into a single fluid by Coulomb interactions, with carbon acting as a braking agent. In this situation, neutrals are also expected to be coupled (the only exception would be neutrals that do not ionize yet still feel a significant radiation force). Thus, one might actually expect that Na I and C I share the same dynamics. The dynamical mass (respectively the radiation pressure coefficient) is coupled to the composition of the gas (Fernández et al. 2006) and could thus give interesting information on the elemental abundances. However, given the unknown uncertainty of the derived dynamical mass, which could also be influenced by the assumptions of our models, we do not draw any further conclusions at this stage.

### 5.2. Issue with the C II Line Profile Core

All the 3D models presented in Section 4.2 have difficulties in reproducing the core of the C II line profile (see Figures 7, 8 and 11). The issue is particularly pronounced for the model with eccentric orbits. The fits to the C II line profile by Cataldi et al. (2014) indicate that the line core requires ionized carbon beyond  $\sim 150 \text{ au}$  to be present. As already discussed in Section 4.1, there might thus exist a gas component with a high ionization fraction beyond  $\sim 150 \text{ au}$ . This component might also be required to prevent the metals observed there from being blown out by radiation pressure (see Section 5.7). It is possible that our simple models are unable to capture this extended gas component. For example, a more complex density and/or temperature profile might be required to reproduce it. Note that while the Cataldi et al. (2014) model fits the C II line profile, it would be a bad fit to our new C I data, as it strongly overpredicts the C I flux.

### 5.3. Overall Timescale of CO and C Production

The strong spatial correlation between the C I and CO emission (Figure 3) suggests a scenario where the carbon is mainly produced from photodissociation of CO, i.e., the mass-loss rate of CO equals the production rate of C. Thus, from the CO mass-loss rate and our estimate of the total C mass, we can

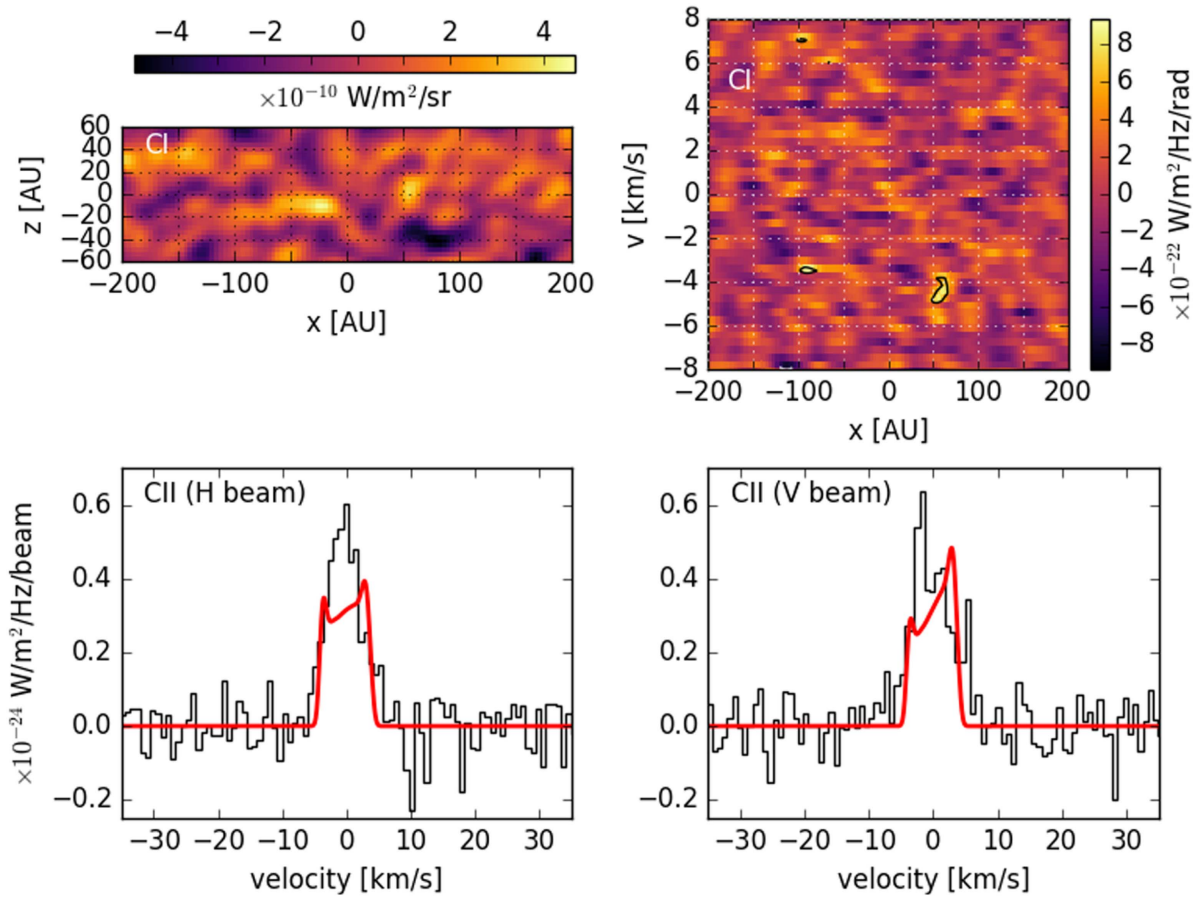


Figure 11. Same as Figure 7, but for the best-fit model with eccentric orbits.

estimate the time since C (and CO) production started in the  $\beta$  Pic disk, provided that no carbon has yet been removed.

### 5.3.1. Revised CO Lifetime

It was previously thought that photodissociation of CO in the  $\beta$  Pic disk is dominated by the ISRF. For example, taking self-shielding into account, Matrà et al. (2017a) calculated a CO lifetime of  $\sim 300$  a in the clump against the ISRF. Here we revise this value, showing that photodissociation from the star actually dominates over the ISRF.

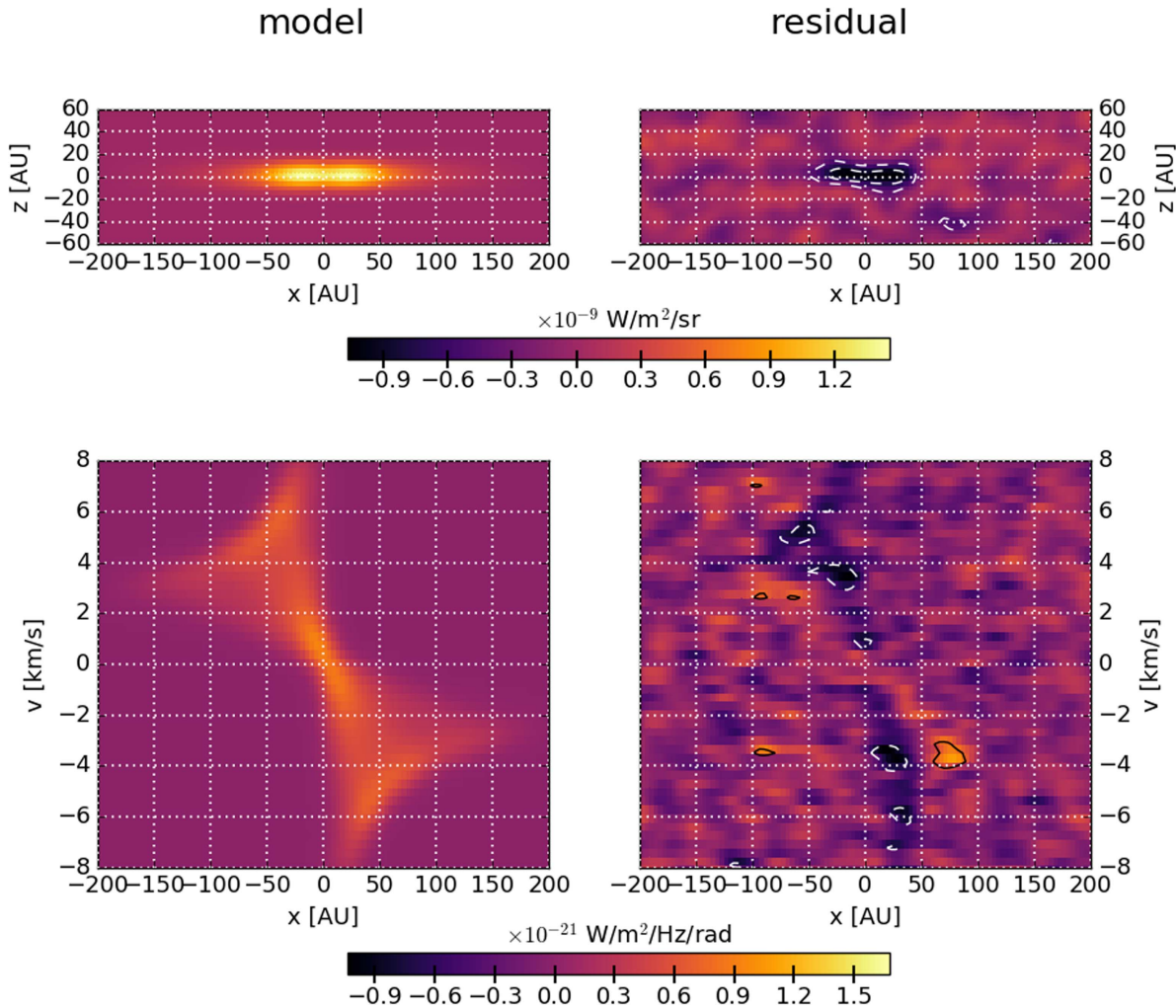
We compute the CO photodissociation rate using photodissociation cross sections from the Leiden Observatory database of “photodissociation and photoionization of astrophysically relevant molecules”<sup>20</sup> (Visser et al. 2009; Heays et al. 2017). We calculate an unshielded lifetime against the ISRF (Draine 1978; Lee 1984) of  $\sim 130$  a.

For the stellar spectrum, the basis is a PHOENIX model as described in Fernández et al. (2006). This model is then complemented with data in the UV from the Space Telescope Imaging Spectrograph aboard the *Hubble Space Telescope* (Roberge et al. 2000), as well as from the *Far Ultraviolet Spectroscopic Explorer* (Bouret et al. 2002; Roberge et al. 2006). This is important because  $\beta$  Pic shows additional emission in the UV above the predictions from a standard stellar atmosphere model. These additional UV photons impact the calculated lifetime of CO. The lifetime corresponding to the

observed stellar spectrum is  $\sim 70$  a at 85 au. However, since the light we observe has traveled through the full CO and C column, this is actually the lifetime of a CO molecule sitting behind this column. To obtain the unshielded lifetime against the star, we have to multiply by the CO self-shielding function (Table 6 in Visser et al. 2009) and the shielding function of the C ionization continuum (Rollins & Rawlings 2012), evaluated at the full CO and C<sup>0</sup> column densities against the star (Roberge et al. 2000). Thus, the unshielded lifetime against stellar photons at 85 au is  $\sim 20$  a.

From Matrà et al. (2017a) and Roberge et al. (2000), we know the vertical column density at the clump location and the horizontal column density of CO against the star, respectively. By applying a rough scaling based on the deprojected CO emission in Matrà et al. (2017a), we estimate horizontal and vertical column densities at the clump location and along the line of sight to the star. For C<sup>0</sup>, the horizontal column density against the star is taken from Roberge et al. (2000), while for the vertical column density we take our best-fit “ring + clump” model as a reference, which is also used to scale the Roberge et al. (2000) horizontal column density to the clump location. For the shielding toward the star, it is not difficult to see that the average CO molecule experiences half of the total column density against the star. For a Gaussian sphere, the average column density per molecule toward the ISRF turns out to be around half of the column density seen from the center of the sphere. We choose shielding factors corresponding to these average column densities. Applying these shielding factors to the unshielded lifetimes derived above, we find that the overall

<sup>20</sup> <http://home.strw.leidenuniv.nl/~ewine/photo/>



**Figure 12.** Model CI emission (left column) computed from the predictions by Kral et al. (2016), and residuals (right column) when subtracting the model from the ALMA data. The top row show the moment 0, and the bottom row the pv diagram. Contours are in steps of  $3\sigma$ , with negative contours drawn as dotted lines.

CO lifetime at 85 au is similar in the clump and in the disk:  $\sim 50$  a.

### 5.3.2. C Production Timescale

Using the CO mass of  $3.4 \times 10^{-5} M_{\oplus}$  derived by Matrà et al. (2017a), a CO lifetime of 50 a leads to a CO mass-loss rate of  $1.2 \times 10^{11} \text{ kg s}^{-1}$ . Under the assumptions that (1) the CO mass-loss rate is constant, (2) C is produced only from CO photodissociation (C might also be produced from the destruction of other carbon-bearing molecules, such as methane, but we expect this to be a minor contribution given typical abundances in solar system comets; e.g., Mumma & Charnley 2011), and (3) no C is removed from the system, we can use the carbon mass derived in Section 4.1 to calculate the timescale over which CO and C production has been ongoing:  $t_{\text{CO}} = t_{\text{C}} = N_{\text{C}} / \dot{N}_{\text{CO}}$ , with  $N_{\text{C}}$  the total number of carbon atoms and  $\dot{N}_{\text{CO}}$  the destruction rate of CO in molecules per second. Using the C mass range derived from our 1D model (Section 4.1), we find a timescale between  $1.7 \times 10^3$  and  $1.1 \times 10^4$  a. When using the mass from the best-fitting “ring + clump” model of Section 4.2.2, we find a timescale of  $\sim 3000$  a. These are very short timescales compared to the age of the system. Thus, any event invoked to explain the observed CO clump (e.g., a giant collision) needs to occur at a correspondingly high rate—otherwise, it would be unlikely to observe the results of such an event so shortly after it

occurred. In the following, we adopt 5000 a as an average estimate of the production timescale.

A caveat remains that some of the C produced from CO photodissociation has already been removed. Kral et al. (2016) suggested that in steady state atomic gas is removed by forming an accretion disk inside and a decretion disk outside of the CO-producing parent belt. However, our data argue against such a scenario (see Section 4.3). Another possibility is chemical processes that might be able to change the amount of carbon in the disk (Higuchi et al. 2017). This would require a sufficiently high  $\text{H}_2$  density. Removing carbon by radiation pressure seems unlikely. First, both neutral C and ionized C do not feel any radiation pressure around  $\beta$  Pic. However, as shown by Fernández et al. (2006), ions are coupled into a single fluid via Coulomb interactions. But the effective radiation pressure on this fluid is not sufficient for blowout (this explains why, e.g., Na is seen in Keplerian rotation despite feeling strong radiation pressure), so C is not blown out as part of the fluid either. Recondensation onto dust grains is also irrelevant (Grigorieva et al. 2007, although they considered the recondensation of water, but similar arguments apply for C gas). Finally, accretion by a planet seems unlikely. Gap-opening planets (Jupiter-class) are the best candidates. But even such planets have a finite accretion efficiency (typically 75%–90%) limited by the leakage of flow across their gaps (Lubow

& D’Angelo 2006). So to increase the estimated lifetime by a factor of 10 or more, the hypothetical planet would have to sit close to the observed belt and accrete with an efficiency of 90% or higher. In addition, planets down to  $1 M_{\text{Jup}}$  have been excluded beyond 30 au by direct imaging searches (Absil et al. 2013).

#### 5.4. Why Is There No Accretion Disk?

Kral et al. (2016) predicted the formation of a C accretion disk based on thermo-hydrodynamical modeling. However, we showed in Section 4.3 that no such accretion disk is present. If the C gas production indeed started as recently as estimated in Section 5.3, the absence of an accretion disk is actually not surprising. Indeed, the timescale for viscous accretion from a radius  $r$  can be estimated by

$$t_{\text{vis}} = \frac{r^2}{\alpha c_s H}, \quad (4)$$

with  $c_s$  the sound speed and  $H$  the scale height. We assume  $c_s = \sqrt{\frac{kT}{\mu m_p}}$  with  $T = 75$  K and  $\mu = 14$ , and  $H$  as in Equation (2) with  $r = 85$  au. A very high  $\alpha \gtrsim 4$  (taking the upper bound of the timescale range calculated in Section 5.3) would be required to match the viscous timescale with the time since C production started. In other words, for any reasonable value of  $\alpha$ , the gas has not yet had enough time to form an accretion disk.

However, a certain amount of carbon is still needed in the inner regions of the disk, where metals such as Na or Fe are seen in Keplerian rotation. These species are strongly affected by radiation pressure, and C is needed to prevent them from being blown out. As was shown by Fernández et al. (2006), C, which does not feel any radiation pressure around  $\beta$  Pic, is acting as a braking agent in the form of  $\text{C}^+$  via Coulomb interactions. In order to test whether the amount of carbon needed to brake metals is consistent with the new ALMA C I data, we consider an accretion disk model extending from 10 to 50 au with a carbon surface density  $\Sigma_{\text{C}} \propto r^{-1}$  and temperature  $T \propto r^{-0.5}$  (with  $T = 75$  K at 85 au; Lynden-Bell & Pringle 1974). We compute the emission from this model as described in Section 4.2. We then search for C I emission only in those regions of the data cube where the model predicts emission. However, we want to exclude regions of the data cube that can contain emission from the outer disk. Thus, for those data points with  $|v| < v_{\text{orb}}(50 \text{ au})$  (with  $v_{\text{orb}}(r)$  the orbital speed at radius  $r$ ), we request points to be at least one spatial resolution element inside of the line in the  $pv$  diagram defining a thin ring at 50 au (see Figure 2). For points with a larger  $|v|$ , we can be sure that no contamination from the outer disk is present. We also exclude points with a predicted emission below 10% of the model peak to avoid considering regions of the data cube where only weak emission is expected anyway. We can then measure the flux in this region of the data cube, with the error estimated with a method analogous to what is described in Appendix A. Defining a detection threshold of  $3\sigma$ , we do not detect significant emission. We derive an upper limit on the C density by adjusting the model such that the probability for a nondetection, i.e., measuring a flux below the detection threshold, would only be 1% if the model was correct. Assuming Gaussian noise, the probability of a model with flux  $F_{\text{mod}}$  to

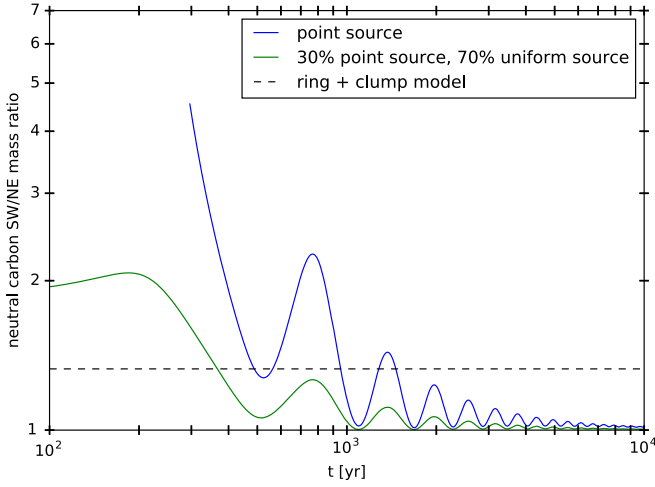
remain undetected is given by  $\frac{1}{2} \left[ 1 + \text{erf} \left( \frac{n\sigma - F_{\text{mod}}}{\sqrt{3}\sigma} \right) \right]$ , with  $\sigma$  the error on the flux and  $n = 3$  in our case. The upper limit model has a midplane  $\text{C}^+$  number density of  $\sim 600 \text{ cm}^{-3}$  at 30 au, while  $\sim 100 \text{ cm}^{-3}$  is necessary to brake the metals (Fernández et al. 2006). Thus, the data are consistent with enough carbon being present in the inner disk to brake metals. However, to get better constraints, we also look at the C II observations from *Herschel*/HIFI by Cataldi et al. (2014). We measure the flux in the wings of the C II spectrum corresponding to radial velocities between  $v_{\text{orb}}(50 \text{ au})$  and  $v_{\text{orb}}(10 \text{ au})$ . Error bars are calculated by calculating the flux in spectral regions of the same size without line emission and taking the standard deviation. We first determine the errors on the flux in the left wing and right wing individually and then add them in quadrature to obtain the error on the total measured flux. No significant (larger than  $3\sigma$ ) flux is detected in either the H or V beam of the data. Thus, we adjust the model such that the combined probability to remain undetected in the ALMA C I and the HIFI C II (H and V beam) data is only 1% (including the ALMA data has a negligible effect, as the HIFI data are more constraining). This model has a midplane  $\text{C}^+$  density at 30 au of  $\sim 380 \text{ cm}^{-3}$ . We conclude that the currently available data are consistent with carbon being present inside of 50 au at a level that is sufficient to brake metals. We suggest that this gas in the inner region was not produced in the same event as the gas seen at larger distances. If it was, we would expect a full accretion disk, which is not supported by the data (see also Cataldi et al. 2014). Instead, it might be the leftover from a previous gas-producing event.

#### 5.5. Origin of the Observed C Asymmetry

A key result from our new ALMA data is that C shows the same asymmetry as CO: a clump on the SW side of the disk. This is surprising since one would expect C to spread in azimuth within a few orbits even though C production might happen preferably at the CO clump. This is in contrast to CO, which has a lifetime shorter than an orbital period and thus remains asymmetric. Here we discuss possible solutions to this puzzle.

##### 5.5.1. Recent Event

Perhaps the simplest explanation for the observed C asymmetry is that C production at the clump location started so recently that there was not yet enough time for azimuthal spreading (respectively symmetrization). We expect the timescale for azimuthal symmetrization to be on the order of a few orbits (at 85 au, the orbital period is  $\sim 600$  a). We investigate the symmetrization with a 1D toy model, where the only dimension is the azimuthal angle  $\phi$ . To start, we assume that all C is produced in a single point at azimuth  $\phi_0$ , at a distance of 85 au, with a rate equal to the CO destruction rate calculated in Section 5.3. In reality, only 30% of the CO emission is found in the clump (Dent et al. 2014). This setup thus maximizes the asymmetry, so the derived symmetrization timescale can be considered an upper limit. We then write the following simple equations describing the temporal evolution of the neutral and ionized carbon densities under the influence of C production,



**Figure 13.** Temporal evolution of the NE/SW ratio of the neutral carbon mass in our toy model. Two scenarios are considered: production from a point source (blue line), providing an upper limit on the symmetrization timescale, and a scenario with initial conditions similar to what we observe today (green line). The dashed line denotes the mass ratio of our best-fit “ring+clump” model.

ionization, recombination, and orbital motion:

$$\frac{\partial \rho_0}{\partial t} = \delta(\phi - \phi_0) \Lambda_{\text{CO}} \frac{m_{\text{C}}}{m_{\text{CO}}} + \rho_+ n_e \gamma - \rho_0 \Gamma - \omega \frac{\partial \rho_0}{\partial \phi} \quad (5)$$

$$\frac{\partial \rho_+}{\partial t} = -\rho_+ n_e \gamma + \rho_0 \Gamma - \omega \frac{\partial \rho_+}{\partial \phi}, \quad (6)$$

where  $\rho_0$  and  $\rho_+$  are the azimuthal densities (in  $\text{kg rad}^{-1}$ ) of neutral and ionized C, respectively,  $\Lambda_{\text{CO}}$  is the CO destruction rate (in  $\text{kg s}^{-1}$ ),  $m_{\text{C}}$  and  $m_{\text{CO}}$  are atomic and molecular masses, respectively,  $n_e$  is the electron density,  $\gamma$  is the recombination coefficient,  $\Gamma$  is the ionization rate, and  $\omega$  is the angular velocity at 85 au. For the electron density, we assume that all electrons come from the ionization of C and that the typical volume extends over  $\Delta r = 70$  au in the radial direction (best-fit “ring” model; Section 4.2.1) and over  $\Delta z = 2H$  (with  $H$  the scale height; see Equation (2)) in the vertical direction (the model remains one-dimensional; we only assume a certain volume to get a value for the electron density). This means that  $n_e = \rho_+ / (m_{\text{C}} + r \Delta r \Delta z)$ , where  $m_{\text{C}}^+$  is the mass of a  $\text{C}^+$  ion. Then, Equations (5) and (6) are used to compute the change of the azimuthal densities at each time step. Figure 13 shows how the SW/NE mass ratio of neutral carbon evolves with time. The wavy pattern is due to the orbital motion of the gas. The local minima correspond to the times when the first gas produced by the point source leaves the NE side and enters the SW side. After  $\sim 10^3$  a, the ratio falls below the value of our best-fit “ring + clump” model.

We can also use this model to estimate the time it will take to symmetrize the C from the state that we observe today if there is no mechanism that prevents symmetrization. For example, assuming that only 30% of the C production occurs at the clump, with the other 70% uniformly distributed at all azimuths (this corresponds to adding a production term independent of  $\phi$  to Equation (5)), we get the green curve shown in Figure 13. As expected, the symmetrization occurs faster—within  $\sim 10^3$  a, the SW/NE mass ratio falls below 1.1.

A caveat to this toy model is the possibility that the gas production is not constant over time. Also, for more robust constraints, detailed hydrodynamical calculations would be necessary.

The upper limit on the symmetrization timescale is below the lower bound of the timescale range over which C production occurred, as derived from the C mass (Section 5.3). Thus, it appears unlikely that the asymmetry can be explained by invoking a very recent event.

In summary, the estimated lifetime ( $\sim 5000$  a) of the carbon-rich gas disk should be long enough to spread out the azimuthal asymmetry, but not long enough to diffuse the disk radially via viscous spreading.

### 5.5.2. Resonance Trapping by Planet

Matrà et al. (2017a) argued that the asymmetry in  $\beta$  Pic, and perhaps in a number of other debris disks, is the result of planetesimals being trapped into mean-motion resonances (MMRs) by a (migrating) planet. For  $\beta$  Pic, our resolved C I observation excludes this possibility.

For planetesimals in resonance with a planet there would be an enhancement in particle density at some special azimuth relative to the planet. In the case of 2:1 MMR, such a resonance island lies  $90^\circ$  behind and ahead of the azimuth of the perturbing planet. As collisions are more frequent in the denser region, it is expected, in this scenario, that CO, which essentially traces recent collisions because of its short lifetime, is enhanced near the island and therefore asymmetric. However, as the planet revolves in its orbit, the resonance island sweeps through all azimuths. Integrated over many periods, the resonance island does not linger particularly long around a special azimuth. So if we look at a tracer gas that is the integrated production of CO over many periods, as the carbon gas is (produced over  $\sim 5000$  a, i.e.,  $\sim 10$  orbits), we expect it to be evenly spread out in the orbit. The observed asymmetry in C thus cannot be explained by its parent planetesimals being trapped into a planet MMR.

Can carbon gas also be trapped into an MMR? In contrast to dust grains, gas cannot be trapped into an MMR. One can show that the resonance width, even when forced by a highly eccentric Jovian planet, is narrower than the vertical scale height of the gas ( $\sim$  a few au). As the vertical scale height corresponds to the sound speed travel time over an orbit, gas pressure can, in an orbital period, easily disperse the gas azimuthally and radially over an extent wider than the resonance width. It is difficult for the weak planetary perturbation to restrain them.

In Section 4.2.3 we showed that an eccentric gas distribution is qualitatively able to reproduce the carbon observations. Thus, in the following sections, we discuss how such an eccentric disk could arise.

### 5.5.3. Initially Eccentric Disk

If the parent planetesimal disk is eccentric because it has been left in that state by some unknown initial condition, the debris disk will initially be asymmetric. Such a disk, if precessed rigidly, can retain its initial configuration over a time much longer than the sound-crossing time. However, over the lifetime of the system (20 Ma), differential precession should have disturbed this initial imprint. Ignoring the presence of other planets and only considering the quadrupole precessional

effect of  $\beta$  Pic b (Lagrange et al. 2009), the timescale for order unity change in the relative precession angle is (Murray & Dermott 2000)

$$t_{\text{smear}} \sim \frac{M_*}{M_p} \left( \frac{a}{a_p} \right)^2 \left( \frac{2\Delta a}{a} \right)^{-1} P_{\text{orb}} \sim 14 \text{ Ma}, \quad (7)$$

where we evaluate the expression using  $M_p = 13 M_{\text{Jup}}$  (Morzinski et al. 2015) for the planet mass and  $a_p = 9 \text{ au}$  (Wang et al. 2016) for its semimajor axis with the ring at  $a \sim 85 \text{ au}$  and with a fiducial radial width of  $\Delta a \sim 20 \text{ au}$  (consistent with that in Table 2). So even without an additional planet, an initially eccentric disk is expected to be largely smeared out.

#### 5.5.4. Eccentric Disk Secularly Forced by a Planet

Secular perturbation from a planet cannot be responsible for producing the eccentric gas disk that we observe. The age of the C gas ( $\sim 5000 \text{ a}$ ) is shorter than any reasonable secular timescale ( $\geq P_{\text{orb}}/\mu$ , where  $\mu$  is the mass ratio of planet to star). So any eccentricity in the gas disk will have to be inherited from their planetesimal parent bodies. But if so, what could possibly have started the parent bodies' grind-down a mere 5000 a ago, if they have lived in such states for a secular timescale? But let us ignore this issue here and proceed to consider the geometry.

In the hypothetical case of long-lived parent bodies forced to a relatively low eccentricity, more particles will be found near apoapsis where they move the slowest (the so-called ‘‘apocenter’’ glow; Pan et al. 2016), while collisions are more likely to occur near the pericenter where the particle streamlines are more densely spaced and their relative velocities are higher. Collisions near the pericenter occur at a higher relative velocity, allowing smaller debris (which are more populous and have a larger collisional surface area) to break apart a given fragment. Matrà et al. (2017b) suggest that the mass-loss rate is enhanced at either periapsis or apoapsis depending on the proper eccentricity and strength of the planetesimals. From preliminary numerical simulations, we favor an enhancement at periapsis (more detailed simulations will be presented in a forthcoming paper). As a result, we expect CO (which reflects the instantaneous collisional mass-loss rate) to be concentrated in periapsis (the SW side, as is observed), while both the submillimeter emission and the carbon line fluxes should be determined mostly by particle trajectories and should peak at apoapsis, contrary to the observations (the observed CI periapsis-to-apoapsis flux ratio is  $1.2 \pm 0.2$ ; see Section 3.1). This argument is easy to understand if one thinks of the CI gas as exact analog of the small dust grains, which are also integrated products of previous collisions. Small grains will shine more brightly in apocenter because there are more of them there—unless their eccentricities are so large that the fall-off of stellar flux at apocenter is more important than the number excess (see our discussion below).

At higher eccentricities, the apocenter is much further than the pericenter, and the drop-off in stellar flux, particle volume density, and gas temperature could compensate for the above trajectory effect and reduce the apocenter glow. Colder submillimeter particles have reduced emissivity. The lower gas temperature and volume density also mean that the carbon gas is less excited, leading to reduced line fluxes. This effect is more severe when the orbits have an intrinsic spread in

eccentricity, leading to a spread in apocenter distances and further reducing the dust and gas volume densities in those locations. Carbon ionization fraction, on the other hand, may also be affected by the lower ionizing flux and the smaller recombination rate.

So to explain the observed same-sided asymmetry in different tracers, we will require a medium to high eccentricity ( $e \gtrsim 0.3$ , Table 2) and preferably a large spread in eccentricities (discussed below). For a secularly forced ring, the forced eccentricity  $e \sim 5/4(a_p/a_{\text{ring}})e_p$ , where  $e_p$  is the eccentricity of the planet (Murray & Dermott 2000). A planet with considerable eccentricity is then required, which may itself decimate the planetesimal belt by dynamical ejection.

Another argument against the planet hypothesis comes from the range of eccentricities required to explain the observations. For a disk with a 20% spread in semimajor axis ( $\Delta a \sim 20 \text{ au}$  if  $a = 85 \text{ au}$ ), we expect a 20% spread in the forced eccentricities. This is too small to help explain the same-side asymmetry, and it is also smaller than indicated by our best-fit solution.

In conclusion, it seems that the hypothesis that there is an underlying highly eccentric planetesimal belt, forced secularly by a planet, is unlikely to explain our observations.

#### 5.5.5. Giant Impact

Jackson et al. (2014) proposed a scenario where a giant impact between two comparably massed bodies produces a wide spread of debris that have a range of eccentricities but a similar alignment. This is qualitatively plausible to explain the observations (but see Matrà et al. 2017a, for a counterargument regarding the radial width). If such an event occurred in the recent past, it provides an interesting explanation for our deduced carbon production timescale. However, such an event seems exceedingly improbable, as we will show with an order-of-magnitude estimate of the event rate.

Consider  $N$  bodies with radius  $R$ , in a belt of semimajor axis  $a$  and width  $\Delta a$ , performing vertical epi-cycles around the midplane. Viewed by each one of these bodies, the other bodies present a certain optical depth of  $\tau_{\perp} = (N4\pi R^2)/(2\pi a\Delta a)$ , or a mean collision time of  $P_{\text{orb}}/\tau_{\perp}$ . Summed over  $N$  bodies, this implies a mean event time of

$$t_{\text{coll}} \sim P_{\text{orb}} \frac{2\pi a\Delta a}{N^2 \times 4\pi R^2} \sim 3 \times 10^9 \text{ years} \times \left( \frac{a}{80 \text{ au}} \right) \left( \frac{\Delta a}{20 \text{ au}} \right) \left( \frac{N}{1000} \right)^{-2} \left( \frac{R}{2000 \text{ km}} \right)^{-2}, \quad (8)$$

where we assume that there is no gravitational focusing among these low-mass objects, reasonable if their velocity dispersion lies much beyond their surface escape velocities. The scaled value  $R = 2000 \text{ km}$  is appropriate to explain the total gas/dust mass observed, and  $\Delta a = 20 \text{ au}$  is inspired by the best fit in Table 2. The value  $N = 1000$  is a placeholder. So, to produce an event as recent as 5000 a ago, one would require  $N \sim 10^5$ , or an absurdly high total mass of  $\sim 500 M_{\oplus}$ . This argument makes giant impacts exceedingly implausible at this location in the disk. Another difficulty with such a scenario is that giant impacts tend to be completely accretionary at low relative speeds, and even at speeds beyond the surface escape, only a small fraction of mass can be unbound and released into the circumstellar environment (Agnor & Asphaug 2004).

### 5.5.6. Tidal Disruption

Here we briefly propose an alternative scenario to produce the observed disk. A more detailed calculation will be presented in an upcoming paper. Consider that the outer disk contains a number of Neptune-like planets ( $N_N \sim$  a few). They have a surface escape velocity of  $v_{\text{esc}} \sim 23 \text{ km s}^{-1}$ . Let us also assume that there are  $N$  bodies similar in mass to the Moon ( $\sim 0.01 M_{\oplus}$ ) or Mars ( $\sim 0.1 M_{\oplus}$ ) and moving in space with a relatively low dispersion velocity,  $\sigma \ll v_{\text{esc}}$ . There is little gravitational focusing among these bodies, but strong focusing by the Neptunes. The timescale for a physical collision with a Neptune is

$$t_{\text{coll}} \sim P_{\text{orb}} \frac{2\pi a \Delta a}{NN_N \times \pi R_N^2} \left( \frac{\sigma}{v_{\text{esc}}} \right)^2 \sim 3 \times 10^7 \text{ years} \\ \times \left( \frac{a}{80 \text{ au}} \right) \left( \frac{\Delta a}{20 \text{ au}} \right) \left( \frac{N}{1000} \right)^{-1} \\ \left( \frac{\sigma}{1 \text{ km s}^{-1}} \right)^2 \left( \frac{v_{\text{esc}}}{23 \text{ km s}^{-1}} \right)^{-2}, \quad (9)$$

where we chose  $N_N = 5$ . This is somewhat arbitrary, but the abundance of cold Neptunes is already suggested by microlensing studies, which claim that their abundance rate per star (mostly M dwarfs) is 52% (Cassan et al. 2012). This timescale is becoming astrophysically interesting. But a physical collision with a Neptune will not produce a debris disk around the star. Instead, we focus on encounters that are close enough that the body is tidally disrupted. This means an encounter distance of  $\sim 2R_N$  and encounter time  $t_{\text{disruption}} \sim t_{\text{coll}}/2 \sim 10 \text{ Ma}$  (at  $2R_N$ , while the geometric cross section goes up by a factor of 4, the gravitational focusing factor,  $(\sigma/v_{\text{esc}})^2$ , evaluated at  $R = 2R_N$  goes down by a factor of 2). So there could have been a few tidal disruption events over the lifetime of  $\beta$  Pic, if there are thousands of moons floating around and if these moons retain low enough dispersion velocities to experience strong gravitational focusing by Neptune. This is still well above the 5000 a event time we infer and still presents a tension.

The end product of the tidal disruption shares many similarities with that from a giant impact. First, the debris will be ejected on a variety of orbits, bringing about a large spread in eccentricity. The semimajor axis will also have a spread. All debris will return to the disruption site, making this location a region of frequent collisions. The size of the disruption site, however, is larger than that in giant impact. As the debris flies away from Neptune, its stellar-centric orbit is altered by Neptune's gravity while it is still within Neptune's Hill sphere. As a result, unlike the narrow nozzle of the size of the impactor radius in the case of giant impacts, here the nozzle has a typical spread of order the planet's Hill radius, which reduces the peak collision rate. However, Matrà et al. (2017a) measured a radial extent of the CO clump of at least 100 au, which is clearly larger than the planet's Hill sphere. More detailed modeling is needed to see whether a tidal disruption event can produce such a radially broad clump. Also, the clump in the deprojection of Matrà et al. (2017a) might appear more extended than it is in reality because the intrinsic velocity dispersion of the gas and the finite velocity resolution of the instrument degrade the resolution of the deprojection in the  $y$ -direction. In addition, the deprojection is carried out assuming velocities corresponding to circular orbits. Thus, if the orbits are eccentric in reality, the

deprojection will be distorted and not correspond to the actual gas distribution.

The event in  $\beta$  Pic is recent and must also be relatively short-lived, assuming that we are not observing it at a special time. The duration of a tidal disruption flare will depend not only on the above-discussed collisional geometry but also on the distribution of the largest fragments (that remain or reform) after the disruption event. Both of these effects need to be studied in detail. In addition, a short lifetime will also ensure that debris products from previous events do not interfere with the current event. If not, the asymmetry would be washed out by previous debris that likely have a different asymmetry, and we would observe the radially diffused accretion disk from gas produced in previous events.

In summary, our observation disfavors a few proposed scenarios (planet MMR trapping, giant impact, secular forcing). Instead, we propose that the bright, asymmetric debris disk in  $\beta$  Pic could be the result of a recent tidal disruption of a Moon-to Mars-sized object by a Neptune-like planet. Using the C mass derived in Section 4.1 and assuming that the disrupted body has had a CO mass fraction of 10%, its total mass would indeed be  $\gtrsim 3 M_{\text{Moon}}$  (lower limit because not all carbon might have been released yet).

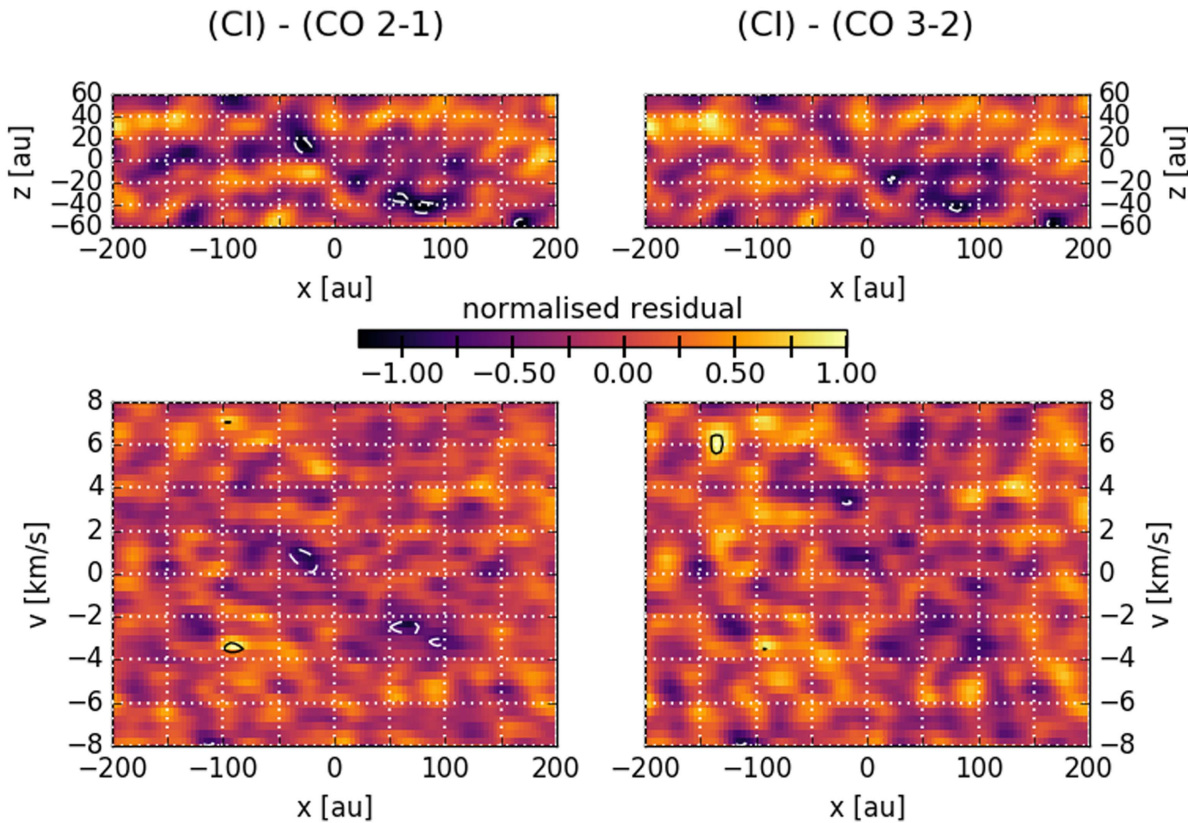
### 5.6. Comparison with the CO Emission

Since C and CO have similar horizontal emission profiles (see Figure 3), the question arises how similar the spatial and spectral distributions of the emission really are. To answer this question, we first interpolate the CO data cube onto the coordinates of the C I data cube. Then, we use convolution to adjust the spatio-spectral resolution of the data cubes. Finally, we normalize the data cubes and subtract. Figure 14 shows the moment 0 and  $p\nu$  diagram of the residual cube for the CO 2–1 and 3–2 transitions (Matrà et al. 2017a). The CO emission seems similar to the C I emission, with few residuals above  $3\sigma$  seen. With the data at hand, we are thus not able to detect clear differences in the emission distribution. Note that there is significant difference in the distribution of CO 2–1 versus CO 3–2 emission (Matrà et al. 2017a).

### 5.7. Comparison to the Spatial Distribution of Metals

Brandeker et al. (2004) and Nilsson et al. (2012) found that Na and Fe have an NE/SW asymmetry reminiscent of what we see for C and CO (compare Figure 3 of this work to Figure 3 in Brandeker et al. 2004). Na and Fe also show a tilt similar to what is seen for C and CO. The radial distribution is quite different, however, with the density being higher closer to the star instead of peaking at 85 au. The asymmetry is seen in both the inner and outer parts of the disk; concerning the inner distribution of Na and Fe, the emission is traced inward to the observational limit of 13 au in the NE, while to the SW the density peak appears to be located much farther out, beyond 50 au. In the outer parts of the disk, Na and Fe can be seen all the way to the limit of the observation at the projected distance of 330 au in the NE, while the disk seems truncated in the SW at 150–200 au.

A possible scenario is that the origin of CO (and thus C and O as its dissociation products) is different from the origin of the metals observed in the optical (Na, Fe, Ca, Ni, Ti, and Cr; Brandeker et al. 2004). While CO likely comes from the disruption of CO-rich cometary bodies at 85 au, the metals



**Figure 14.** Residual moment 0 and  $pv$  diagram when subtracting the peak-scaled CO from the C I data cube. The spectro-spatial resolution has been adjusted prior to subtraction. Contours are drawn at intervals of  $3\sigma$ . The residual data cube was integrated over  $\pm 6 \text{ km s}^{-1}$  for the moment 0 and  $\pm 30 \text{ au}$  for the  $pv$  diagram, respectively.

observed in the optical could be produced by the so-called falling evaporating bodies (e.g., Vidal-Madjar et al. 2017) close to the star and then diffused outward by the stellar radiation pressure. As the presence of  $\text{C}^+$  would act as a braking agent (Fernández et al. 2006), its spatial distribution would naturally become imprinted on the spatial distribution of the metals. The spatial distribution of Na and Fe is therefore consistent with  $\text{C}^+$  being in an eccentric distribution resulting from a tidal disruption event, as outlined in Sections 4.2.3 and 5.5.6. With the SW clump at 85 au being at the convergence point for a family of eccentric orbits, the C would be more concentrated to the clump location in the SW, while being much more radially distributed in the NE, in agreement with the observed Na and Fe distributions.

## 6. Summary and Conclusions

In this paper, we present resolved ALMA band 8 observations of C I emission toward the  $\beta$  Pic debris disk. Our work can be summarized as follows:

1. Using a simple 1D model that calculates the ionization balance and non-LTE level populations, we estimate the total C mass to be between  $5 \times 10^{-4}$  and  $3.1 \times 10^{-3} M_{\oplus}$ . Assuming that C is produced from the photodissociation of CO at a constant rate and that C is not removed from the system, this mass implies that gas production started only  $\sim 5000$  a ago.
2. Surprisingly, C I shows the same asymmetry as seen for CO: a clump on the SW side of the disk. By modeling the spatial distribution of the C gas, we find that a satisfactory

fit to the C I and archival C II data can be found by assuming that the gas consists of a ring between 50 and 120 au with a superimposed clump at the same location as the CO clump. A model assuming eccentric orbits of the gas with a flat eccentricity distribution between 0 and 0.3 also reasonably fits the data.

3. The C I data are not consistent with the accretion disk predicted by Kral et al. (2016). If C gas production indeed started only  $\sim 5000$  a ago, not enough time has passed for gas to have spread viscously into an accretion disk.
4. The short timescale since gas production started argues against a giant-impact origin of the C/CO/dust clump, because giant impacts are rare. It is unlikely that we observe the results of such an event so shortly after it occurred. However, while the production timescale of  $\sim 5000$  a is short compared to the age of the system, it is long enough to allow azimuthal spreading of the gas. Thus, a scenario where the C asymmetry is due to a lack of time for azimuthal spreading is disfavored.
5. The fact that C shows the same asymmetry as CO (a clump in the SW) argues against a scenario where the clump is due to planetesimals trapped in a resonance with an outward-migrating planet. Indeed, in such a scenario, the clump orbits with the planet, i.e., the gas production should be symmetric on an orbital timescale.
6. In order to explain the simultaneous C and CO asymmetry, we propose that the planetesimal and gas disk of  $\beta$  Pic is eccentric and might have originated from a recent tidal disruption event. This could potentially also

explain the asymmetry observed in Na I and Fe I by Brandeker et al. (2004).

A detailed study of the tidal disruption mechanism will be presented in a forthcoming paper. Follow-up observations of the C I line at higher S/N and spectro-spatial resolution can be used to confirm or reject our hypothesis of an eccentric disk due to a tidal disruption event.

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*Facilities:* ALMA, Herschel (PACS, HIFI).

*Software:* astropy (Astropy Collaboration et al. 2013), CASA (McMullin et al. 2007), emcee (Foreman-Mackey et al. 2013), LIME (Brinch & Hogerheijde 2010), Matplotlib (Hunter 2007), NumPy (van der Walt et al. 2011), pythonradex (<https://github.com/gica3618/pythonradex>), SciPy (<http://www.scipy.org>).

## Appendix A Details of the Error Calculation

In this appendix we describe how the errors quoted in Sections 3.1 and 3.3 are derived.

The total line emission was measured by integrating the data cube within  $\pm 6 \text{ km s}^{-1}$  in the spectral dimension and over the rectangular box shown in Figure 1 in the spatial dimension. Having measured the noise in the data cube, a naive way to estimate the error  $\sigma_F$  on the total flux would be to write  $\sigma_F = \sqrt{n} \sigma d\Omega dv$ , with  $n$  the number of data points over which the integration extends,  $\sigma$  the noise in the data cube, and  $d\Omega$  and  $dv$  the extent in solid angle and velocity, respectively, of a single data point. However, since neighboring data points are correlated, this approach is not valid. Instead, we consider the flux of a number of volumes with the same size as the volume used to measure the total flux, placed in regions of the data cube without emission. Taking the standard deviation of these flux samples, we obtain an estimate of the error. The volumes are placed such that they are sufficiently distant from each other to be considered independent. Since no primary beam correction has been applied, the noise can be assumed uniform over the data cube.

For the continuum, the above procedure yields too few flux samples. Thus, we reduce the size of the flux samples in the  $x$ -direction to get more samples. Then, we set  $\sigma_F = \sigma_s \sqrt{N}$ , where

$\sigma_s$  is the standard deviation of the flux samples and  $N$  is the number of flux samples that fit into the region for which the flux is measured. Again, the flux samples are placed sufficiently distant from each other to be considered independent.

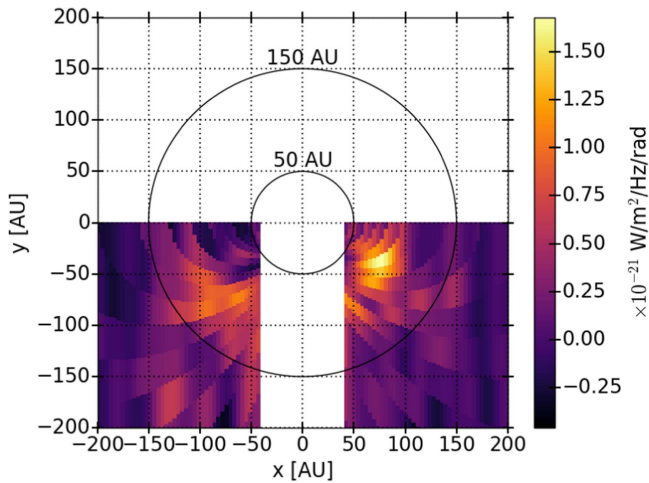
For the emission profile along the disk (Figures 1 and 3, right panels), we consider sample “volumes” that extend only one pixel in the  $x$ -direction. In the case of the profile derived from the restricted region in  $pv$  space (Figure 3), the size of the region over which we integrate depends on  $x$ . Thus, we take flux samples for each  $x$  individually. For this profile, the error thus depends on  $x$ .

## Appendix B Measurement of the Line Broadening Parameter

The line broadening parameter  $b$  (defined as  $b = \text{FWHM}/(2\sqrt{\ln 2})$ , where FWHM is the full width at half maximum of the line) parameterizes the line broadening due to effects other than the orbital motion of the gas (e.g., thermal broadening or turbulence). We can use the ALMA observations of C and CO to measure  $b$  by considering a vertical cut in the  $pv$  diagram (Figure 2) going through  $x = 0$ , i.e., considering the line of sight toward the star. For circular orbits, all gas along this line of sight is centered at the same radial velocity (namely,  $0 \text{ km s}^{-1}$ ), allowing a measurement of  $b$ . However, if orbits are eccentric, the line of sight toward the star can contain additional broadening due to orbital motion. Furthermore, the finite spatial resolution of the instrument will blur material with nonzero radial velocity into the line of sight toward the star. Thus, our derived value of  $b$  should be considered an upper limit.

We consider the  $pv$  diagrams of C I (this work), CO 2–1, and CO 3–2 (Matrà et al. 2017a) and for each of them fit a Gaussian to the vertical cut through  $x = 0$ , yielding three independent measurements of  $b = \sqrt{b_{\text{fit}}^2 - b_{\text{inst}}^2}$ , where  $b_{\text{fit}}$  is the broadening parameter of the fitted Gaussian and  $b_{\text{inst}}$  is the broadening due to the spectral response function of the instrument.<sup>21</sup> We estimate errors using emcee, a python implementation of an affine invariant Markov chain Monte Carlo sampler (Foreman-Mackey et al. 2013). The likelihood was defined via a  $\chi^2$  measure analogous to Equations (1) and (2) of Booth et al. (2017). In particular, we also use a noise correlation ratio, defined in our case as the square root of the number of spectral pixels per spectral resolution element. We consider invariant uninformative priors, imposing only that the peak of the Gaussian and the broadening parameter are positive. We use 100 walkers with  $10^4$  steps. This yields the following results for  $b$ :  $0.66 \pm 0.11 \text{ km s}^{-1}$  (C I),  $0.56 \pm 0.04 \text{ km s}^{-1}$  (CO 2–1), and  $0.56 \pm 0.05 \text{ km s}^{-1}$  (CO 3–2). Combining these measurements as a weighted mean yields  $b = 0.57 \pm 0.03 \text{ km s}^{-1}$ . This value may be compared to previous measurements of  $b$ . Jolly et al. (1998) measured  $0.8 \pm 0.05 \text{ km s}^{-1}$  from CO absorption (they also measured a high  $b$  value of  $4.2 \text{ km s}^{-1}$  from C I absorption, potentially caused by modeling difficulties because the line is saturated). Roberge et al. (2000) obtained  $1.3 \pm 0.5 \text{ km s}^{-1}$  from C I absorption and  $1.3 \pm 0.1 \text{ km s}^{-1}$  from CO absorption. Cataldi et al. (2014) and Nilsson et al. (2012) previously adopted  $1.5 \text{ km s}^{-1}$  for their models based on measurements of Ca II K absorption (Crawford et al. 1994). The  $b$  value derived from the

<sup>21</sup> See ALMA Cycle 6 Technical Handbook, Section 5.5.2 (Spectral Setup), <https://almascience.nao.ac.jp/documents-and-tools/cycle6/alma-technical-handbook>.



**Figure 15.** Same as Figure 4, but in the same units as the  $pv$  diagram, i.e., without multiplying the deprojection by the Jacobian shown in Equation (10).

ALMA data seems thus generally lower than in previous publications.

### Appendix C Details of the Deprojection Procedure

The  $pv$  diagram can be used to get a deprojected view of the emission in the  $(x, y)$  plane. As is discussed in Appendix C of Matr  et al. (2017a), a radius  $r = (GM_*x^2/v^2)^{1/3}$  can be assigned to points  $(x, v)$  of the  $pv$  diagram for an edge-on disk and circular Keplerian orbits. From this, we can find the position along the line of sight  $y = \pm\sqrt{r^2 - x^2}$ . Note that for some points  $(x, v)$  of the  $pv$  diagram, the term under the square root becomes negative. This simply means that for the given  $x$  the radial velocity  $v$  cannot be reached anywhere along the line of sight, i.e., we have  $|v| > v_{\text{max}}$ , where  $v_{\text{max}}$  is the orbital velocity of the orbit with  $r = x$ . One has to choose how to distribute the flux from a given  $pv$  point among the two possible  $y$  points (in front of and behind the sky plane).

In practice, it is easiest to take an inverse approach. First, we decide to place all flux in front of the sky plane (i.e., we only consider  $y < 0$ ). Then, for a given point  $(x, y)$ , we calculate  $r = \sqrt{x^2 + y^2}$ . From this,  $v = -\sqrt{\frac{GM_*}{r}} \frac{x}{r}$ , where the minus sign accounts for the known rotation sense of the  $\beta$  Pic disk. We then look up the flux at  $(x, v)$  in the  $pv$  diagram and assign it to the point  $(x, y)$  in the deprojection.

In order to get a deprojection with a straightforward interpretation in terms of the distribution of the flux, it is also necessary to transform the flux units from  $\text{W m}^{-2} \text{Hz}^{-1} \text{rad}^{-1}$  (as in the  $pv$  diagram; see Figure 2) to  $\text{W m}^{-2} \text{sr}^{-1}$ . To do this, it is helpful to see the deprojection as a coordinate transformation from  $(x, v)$  to  $(x, y)$ . The Jacobian determinant of this transformation (for  $y = -\sqrt{r^2 - x^2}$  as in Figure 4) reads

$$J = \frac{3}{2} \sqrt{GM_*} xy (x^2 + y^2)^{-7/4}. \quad (10)$$

The flux read from the  $pv$  diagram is then multiplied by  $|J|$  and an additional constant factor  $\frac{\nu_0}{c}d$  (with  $\nu_0$  the central frequency of the line and  $d$  the distance between the observer and  $\beta$  Pic).

If the flux units of the deprojection are not transformed (as, e.g., in Matr  et al. 2017a), an interpretation of the deprojection is not straightforward because the flux in a certain area of the

deprojection does not equal the integral over  $x$  and  $y$  over this area. Figure 15 shows the deprojection without multiplication by the Jacobian (i.e., in the same units as the  $pv$  diagram). Comparing to Figure 4, it becomes apparent that a deprojection without transformed units might lead to visual misinterpretation, for example, about the relative amount of flux at large radii (say, beyond 150 au). Indeed, from Equation (10), we see that the Jacobian gets smaller at large radii.

### Appendix D Approximate Calculation of the SE

We solve the SE under the simplifying assumption that the photon escape fraction is high, i.e., we neglect (de)excitation by emitted line photons and assume that the background radiation field (CMB, stellar field, and dust continuum) is not attenuated by the gas. In this section, we justify these assumptions.

The SE equation for an atomic level  $i$  can be written as

$$\sum_{j \neq i} (x_j(A_{ji} + C_{ji} + \bar{J}B_{ji}) - x_i(A_{ij} + C_{ij} + \bar{J}B_{ij})) = 0, \quad (11)$$

where  $x_j$  is the fractional population of level  $j$ ,  $C_{ij} = K_{ij}n_e$  is the collisional (de)excitation rate (with  $K_{ij}$  the collisional rate coefficient and  $n_e$  the electron density),  $\bar{J}$  is the frequency-integrated mean intensity, and  $A_{ij}$  and  $B_{ij}$  are the Einstein coefficients (where we set  $A_{ij} = 0$  if  $i < j$ ). If we can show that  $A_{ji} + C_{ji} \gg \bar{J}B_{ji}$  (for any  $i, j$ ), then we have demonstrated that background radiation and line photons are not important to solve the SE.

The frequency-integrated mean intensity is the sum of the line emission and background radiation at each point of the disk:  $\bar{J} = \bar{J}_{\text{line}} + \bar{J}_{\text{backg}}$ . To get insight into the individual contribution of the two components, we consider them separately. First, we calculate  $R_{\text{backg}} = \bar{J}_{\text{backg}}B_{ji}/(A_{ji} + C_{ji})$  for all transitions and all locations (except where the gas density is below 5% of the peak density) for the best-fitting models described in Sections 4.2.1–4.2.3. We find that  $R_{\text{backg}} < 0.02$  for C I and  $R_{\text{backg}} < 0.001$  for C II. Thus, although we included background radiation in our calculation, it is actually negligible. We double-check by recomputing the models without background radiation and find that the results indeed do not change.

Next, we consider (de)excitation by line emission and compute  $R_{\text{line}}$ . To this end, we compute, for every location (again, except where the gas density is below 5% of the peak density), the number of line photons arriving from the other grid points, neglecting optical depth and the velocity field (the velocity field could red/blueshift photons from other grid points out of the transition). We are thus calculating an upper limit on  $\bar{J}_{\text{line}}$ . We find that  $R_{\text{line}} < 0.4$  for C I and  $R_{\text{line}} < 0.03$  for C II. Thus, a more sophisticated model should include the full radiative transfer for C I, but neglecting the line photons is a decent approximation given the quality of our data, since it considerably simplifies the calculation of the models.

As an additional test, we used the LIME code version 1.9.1 (Brinch & Hogerheijde 2010) to calculate the full non-LTE radiative transfer (neglecting background radiation except for the CMB) for our best-fit models from Sections 4.2.1–4.2.3. We find that the total flux computed by LIME differs at most by a factor of 1.2 for both C I and C II.

## Appendix E

### Gas Density for Eccentric Orbits

In this section, we derive the gas surface density of the model with eccentric orbits presented in Section 4.2.3. We assume that all orbits have a common pericenter and that the distribution of eccentricities is known and given by  $P(e)$ . We search the probability  $P(r, \theta)$  (which we assume is proportional to the surface density) to find a particle at radius  $r$  and true anomaly  $\theta$ . We first consider  $P(e, \theta) = P(e)P(\theta|e)$ . In our model, a given eccentricity  $e$  corresponds to a single orbit (because all orbits have a common pericenter). Thus,  $P(\theta|e)$  is interpreted as the probability to find a particle at true anomaly  $\theta$  along the orbit with eccentricity  $e$ . The time a particle spends at a given  $\theta$  is inversely proportional to the orbital velocity. Thus, we have

$$P(\theta|e) = \frac{C(e)}{|v(e, \theta)|}, \quad (12)$$

where the normalization constant  $C(e) = \left( \int \frac{1}{|v(e, \theta')|} d\theta' \right)^{-1}$ . The orbital velocity is given by

$$v(e, \theta) = \sqrt{\mu \frac{1 + 2e \cos \theta + e^2}{q(1 + e)}}, \quad (13)$$

where  $\mu = GM_*$  and  $q$  is the fixed pericenter distance. Next, we consider the transformation from  $(e, \theta)$  to  $(r, \theta)$  where




$$r = \frac{q(1 + e)}{1 + e \cos \theta}. \quad (14)$$

The transformation is bijective, except for  $\theta = 0$ . Therefore, we can write

$$P(r, \theta) = P(e, \theta)|J|, \quad (15)$$

with  $J$  the Jacobian determinant of the transformation, given by  $J = \frac{\partial e}{\partial r}$ , which can be calculated from Equation (14). At  $\theta = 0$ , the density  $P(r, \theta)$  diverges. In practice, this is easily handled by simply not sampling the singularity on the numerical grid.

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