

with parameters $\gamma = 0.01$ and $\epsilon = 0.01$. Furthermore, parameter C was selected by Eq. 2.

Similar feature selection strategy, as in Section 5, is used for this task. Time window position and the previous two-hour volume were treated as two basic features during the process. Time window position is the same as in Section 5 and the previous two-hour volume means the two-hour volume data before the rush hours to be predicted.

The performances of combining different scaling methods with SVR are presented in Table 2. For the volume prediction, applying SVR combined with a scaling method gives a huge improvement to the result compared with only using SVR. And again, it appears that Robust-scaling is particularly good for time series with more varying patterns. Note that the period of 1st October to 7th October is a big holiday period in China and it is widely known that the traffic volume is unusual during that period.

Table 2. Average MAPE from cross-validation experiments with features: time window position and previous two-hour volume. Training data are from 19/9 to 17/10. Test data are from 18/10 to 24/10.

Scaling method	validation result	prediction of test data
Robust-scaling	0.2710	0.1472
Standard-scaling	0.2717	0.1502
Min-Max-scaling, [0,1]	0.3467	0.1526
No scaling	1.0374	0.3128

Traffic volume may depend on many factors, including time of day, day of week, holiday, weather, etc. For this reason, an additional feature called special days to capture the holidays and weekends effect was added. Other features, extracted from the provided volume data, including the number of vehicles with ETC and the number of vehicles have vehicle model n ($n \in [0, 7]$), were also tested in our experiments (not shown here due to space). The predictive performance increases when we add special days to the feature set. The best performance (with average MAPE 0.2691 in validation phase and 0.1436 in prediction phase) is from an experiment where special days is included in the feature set, suggesting the feature special days is a very important feature for traffic volume prediction.

7 Generalisation

Based on the experimental results from the previous sections, we conclude that: (i) SVR with a scaling method performs better compared to without scaling; (ii) robust-scaling is especially good for time series with varying patterns; and (iii) Min-max-scaling is especially good for time series with similar patterns. These

conclusions could depend on the provided input data. Here, we want to test if the conclusions could be generalised if different traffic data set is used. Due to the lack of other traffic data set, we analyse the following question instead:

Do these conclusions still hold if some of the data had been missing?

If some of the data had been missing, we start from slightly different data. The basic idea to address this question is: randomly delete some values from the original data (pretend those values were missing) and repeat the same experiment with reduced input data. The procedure can be summarised as follows:

1. delete $p\%$ of the original data randomly.
2. fill in the originally missing data and the deleted data using Complementary and linear interpolation.
3. take the data after Step 2, for each of the three scaling methods, run the experiment with a fixed feature set and a fixed SVR-setting. For simplicity reason, we use the basic feature set (time window position and the previous two-hour travel time), RBF-kernel, and SVR parameters $\epsilon = 0.5, \gamma = 0.005$. The output from this step is a table similar to Table 1, but with changed values.
4. repeat Step 1 to Step 3 100 times.

Task 1 was investigated with five levels of deletion (10%, 20%, 30%, 40%, 50%). For brevity, only the results from 10% and 50% are reported here (Fig. 2).

The results from Task 1 (Fig. 2) show that the performance of no scaling (black) is noticeably worst compared to that of the other methods for both validation (solid lines) and prediction (dashed lines). For validation, the performances of Robust-scaling (solid red) and Standard-scaling (solid blue) are very similar, while Min-max-scaling (solid green) is slightly better than the other scaling methods. For prediction, the performances of Robust-scaling (dashed red) and Standard-scaling (dashed blue) deteriorate more than Min-max-scaling (dashed green) as more data are deleted. A possible explanation of this is that as more data are deleted, the more outliers disappear and are replaced with smoother values (since we use complementary and linear interpolation to fill in the deleted data). This suggests that Min-max-scaling is especially good for time series with similar patterns.

A modified generalisation procedure was applied for Task 2, with the same five levels of deletion. The modifications include: In Step 2, only linear interpolation is used to fill in the originally missing data and the deleted data; In Step 3, use time window position and the previous two-hour volume as feature set and set SVR parameters $\epsilon = 0.01, \gamma = 0.01$.

The results from Task 2 (Fig. 3) show that in all cases the performance of no scaling (black) is worst compared to that of the other methods for both validation (solid lines) and prediction (dashed lines). The performances of Robust (red) and Standard-scaling (blue) are very similar in both validation and prediction. Unlike the results of generalisation from Task 1, the validation performance of Min-max-scaling (solid green) deteriorates more than the other scaling methods

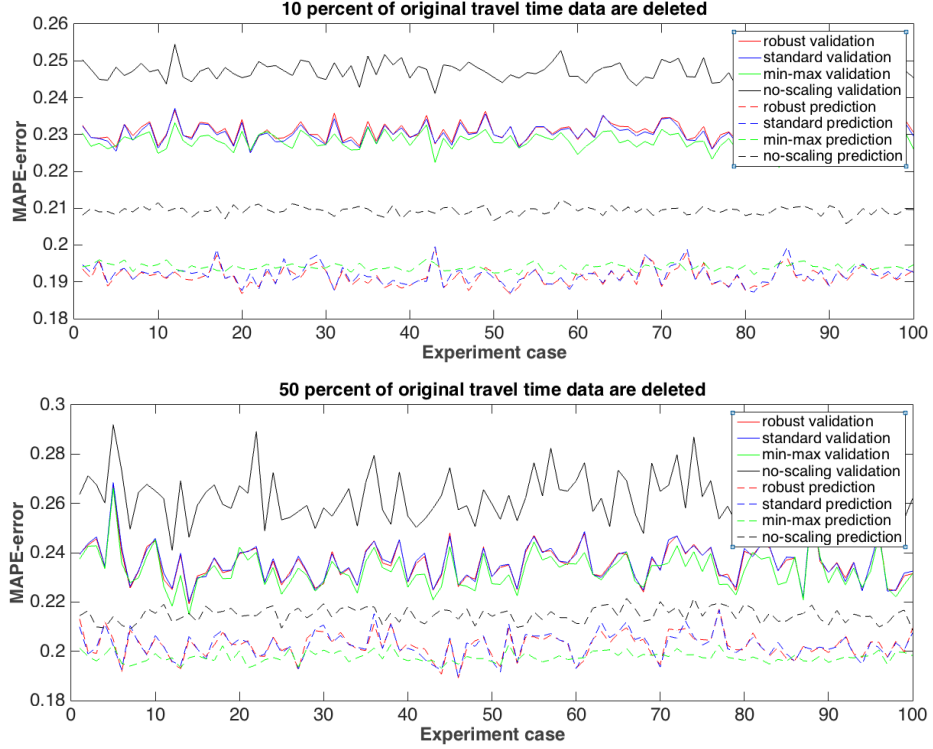


Fig. 2. Validation and prediction error for 100 experiments with 10% (top) and 50% (bottom) deleted data for the generalisation of Task 1 (travel time prediction).

as more data are deleted. For prediction, the performances of all three scaling methods are very similar. A possible explanation for this is that the original pattern (varying pattern) of volume data are mostly preserved after deletion and filling in process.

Based on the results of this section, the conclusions (i) and (iii) still hold. Regarding conclusion (ii), it seems that, for the data with varying pattern, the Robust and Standard-scaling perform very similar and slightly better than Min-max-scaling.

8 Conclusion

This paper demonstrated the application of SVR with scaling methods for travel time and tollgate volume predictions in rush hours. The impact of using three different scaling methods (Robust-scaling, Standard-scaling, and Min-Max-scaling) with SVR-predictor was investigated. Furthermore, experiments to test if the conclusions from Sections 5 and 6 still hold if reduced data is used as input were conducted. Our results suggested that SVR combined with a scaling method

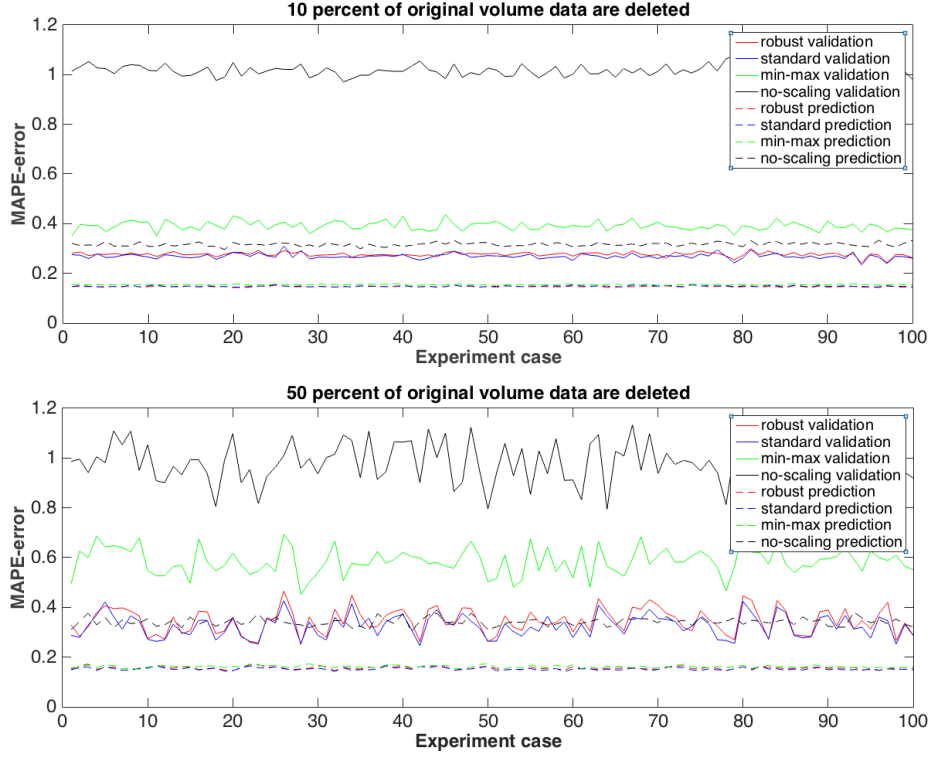


Fig. 3. Validation and prediction error for 100 experiments with 10% (top) and 50% (bottom) deleted data for the generalisation of Task 2 (volume prediction).

provides a more accurate prediction than without scaling, especially for volume prediction task. Min-Max-scaling was found to be particularly good for time series with more similar patterns. The performances of Robust-scaling and Standard-scaling were found to be pretty similar, and they seemed to perform slightly better than Min-max-scaling for time series with varying patterns.

Features that capture different travel time/volume influencing factors were analysed in the experiments. Although adding the features tollgate volume and adjacent tollgate volume has been found to increase the performance in some of our experiments for travel time prediction, but it is not always the case. The feature special days was found to be useful for volume prediction. Weather-related features were not found to be that useful in our experiments.

When our model was applied to Task 1, the mean absolute percentage error of the travel time prediction is around 0.19, which differs by only 0.02 from the best result obtained by other contestants (this is a competition task, the best prediction result was announced). Similarly, when our model was applied to Task 2, the mean absolute percentage error of the volume prediction is around 0.144, which differs by only 0.03 from the best result. We conclude that SVR

combined with a scaling method can still provide a reasonable performance for travel time and traffic volume predictions, even when the training data contains many outliers (like holiday data) and no deep analysis of the data was applied.

Acknowledgments. S. acknowledges strategic funding support from Chalmers Area of Advance Transport while writing this paper.

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