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Distributed Two-Way Localization Bounds for 5G mmWave Systems

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Abstract—Recently, localization for 5G millimeter-wave communication systems has been shown to provide high-accuracy performance, with error being in the order of tens of centimeters. However, most of the literature assumes a high level of synchronization, which is not always the case practically. To address this matter, we investigate a distributed two-way localization protocol (DLP) that relieves the need for tight timing synchronization. We derive the position and orientation bounds, when localization is initiated and carried out by the base station. Our simulation results show that the performance of DLP is identical to that of the synchronized one-way localization. We thus conclude that the considered 5G localization is limited by the estimation of the angles rather than the delay. The results also imply that orientation estimation is more challenging than position estimation.

I. INTRODUCTION

With the high localization accuracy of 5G millimeter-wave (mmWave) communication systems, location-aided communication is becoming more attractive. The location information creates two kinds of opportunities unique to 5G mmWave, since it enables location-aware applications [1], [2], e.g., vehicular communication, and assisted living systems, while also supporting communication systems design and optimization [3]–[5] such as beamforming, pilot assignment, and resources allocation.

Due to the utilization of arrays with high number of antennas at the transmitter and the receiver, and the allocation of massive bandwidths, spatiotemporal localization with single base station (BS) can be seen as the ultimate localization strategy for 5G. With the high number of antennas, the directions of arrival (DOA) and departure (DOD) can be estimated with very low error [6], while the large bandwidth enables highly accurate estimation of the time of arrival (TOA) [7]. Subsequently, combining the spatial and temporal estimates, the user equipment (UE) location can be determined.

The accuracy of single-anchor localization for 5G mmWave systems has been studied recently by several papers in terms of position (PEB) and orientation error bounds (OEB). The UE PEB and OEB of 2D localization in 5G mmWave systems were investigated in [8] using uniform linear arrays. On the other hand, the PEB and OEB for mmWave 3D localization were derived with different approaches in [9] and [10] using arrays with arbitrary geometries. The results in [8]–[10] showed that the error performance of 5G mmWave localization is in the order of centimeters. However, one important, yet usually overlooked, requirement for localization is the synchronization of BS and UE. For example, [8] and [10] assume that the BS and UE are perfectly synchronized, while [9] assumes coarse synchronization, and includes a residual synchronization error in the model.

Motivated by two-way ranging that use the time-of-flight [11], in this paper, we focus on two-way localization (TWL). We study the PEB and OEB under line-of-sight (LOS) communication with a distributed TWL protocol (DLP) that accounts for timing bias between the clocks of the BS and UE. Higher order artifacts such as clock drift and skew are not addressed herein, but can be estimated using three- or multi-way ranging [11], [12]. Under DLP, the BS initiates the localization process by transmitting a known signal to a UE. Then, the UE estimates the TOA with reference to its local clock and transmits back another known signal, after a pre-agreed waiting interval. Subsequently, upon receiving the UE signal, the BS estimates the range between the two devices with reference to its local clock. Since this clock was initially used to transmit the first signal, full time synchronization between UE and BS is not needed. Eventually, localization is achieved at the BS, using the signal received back after the second transmission round.

Considering localization at BS only, we investigate the DLP for LOS 5G mmWave signals, as a means of alleviating the tight synchronization requirement of localization. Towards that, we consider the timing bias between the BS and UE as a nuisance parameter and derive the Fisher information matrices (FIM) of the position and orientation. Based on these FIMs, we evaluate the PEB and OEB numerically, and compare them to those of the traditional one-way localization (OWL) [10]. The results provided herein are part of an extensive study presented in [13], where both network-side and device-side localization are investigated for distributed and centralized TWL protocols.

II. CHANNEL MODEL AND BEAMFORMING

Consider uplink localization, whereby a BS, located at the origin of the 3D space with zero orientation angles, attempts to estimate the UE position, \( \mathbf{p} \triangleq [p_x, p_y, p_z]^T \), and orientation, \( \mathbf{o} \triangleq [\zeta_0, \chi_0]^T \). Similar to [10], we define \( \zeta_0 \) as the rotation angle around the \( z \)-axis, which yields new coordinate axes \( x', y' \) and \( z \), while \( \chi_0 \) is defined...
This is representative of practical applications characterized by two rotation angles, such as vehicular and robotic applications. Both BS and UE are equipped with antenna arrays of arbitrary but known geometries and communicate through a LOS. In this context, we assume that the NLOS parameters, if any, can be estimated as in [10]. However, unlike [10], we use only the DOA, DOD, and TOA of the LOS path to compute the PEB and OEB. Consequently, for clarity, we can write the signal model explicitly by including only the LOS2.

In the following, the parameters related to BS and UE are denoted by the subscripts “B” and “U”, respectively, while the superscripts “f” and “b” denote the parameters to the forward and backward transmissions, respectively.

1) Forward Channel: The forward signal, received at UE at time $t = \tau^f$, undergoes a channel given by

$$\mathbf{H}^f(\beta, \vartheta) \triangleq \mathbf{H}^f(\beta, \vartheta) \delta(t - \tau^f), \in \mathbb{C}^{N_B \times N_u}$$

where $\mathbf{H}^f(\beta, \vartheta) \triangleq \sqrt{N_B N_u} \mathbf{a}_\beta(\theta_U, \phi_U) \mathbf{a}^\dagger_{\vartheta}(\theta_B, \phi_B)$ is the channel part corresponding to the spatial channel parameters, such that $\beta$ is the complex path gain, $N_B$ and $N_u$ are the number of antennas at BS and UE, respectively, and $\vartheta \triangleq [\beta_B, \vartheta_B, \beta_U, \vartheta_U]^T$, (2)

and $(\theta_U, \phi_U)$ and $(\theta_B, \phi_B)$ are the forward DOAs and DODs. Finally, $\mathbf{a}_\beta$ and $\mathbf{a}_{\vartheta}$ are the array response vectors

$$\mathbf{a}_\beta(\theta_U, \phi_U) \triangleq \frac{1}{\sqrt{N_u}} e^{-j \Delta_B^T \mathbf{k}(\theta_U, \phi_U)}, \in \mathbb{C}^{N_u}$$

$$\mathbf{a}_{\vartheta}(\theta_B, \phi_B) \triangleq \frac{1}{\sqrt{N_B}} e^{-j \Delta_U^T \mathbf{k}(\theta_B, \phi_B)}, \in \mathbb{C}^{N_B}$$

where $\mathbf{k}(\theta, \phi) = \frac{2\pi}{\lambda} [\cos \phi \sin \theta, \sin \phi \sin \theta, \cos \theta]^T$ is the wavenumber vector, $\lambda$ is the wavelength, $\Delta_B \in \mathbb{C}^{3 \times N_u}$ is a matrix whose columns contain the 3D Cartesian coordinates of the array elements of BS in meters, and $\Delta_U \in \mathbb{C}^{3 \times N_B}$ is defined similarly for UE. For presentation purposes, we drop the angle parameters from the notation of $\mathbf{a}_{\vartheta}$ and $\mathbf{a}_\beta$.

The signal transmitted from BS is modeled by $\sqrt{E} \mathbf{F}_{B}(\tau^f, t)$, where $E$ is the transmitted energy per symbol, and $\mathbf{F}_{B} \triangleq [f_{B,1}, f_{B,2}, \ldots, f_{B,N_{bB}}]$ is the BS transmit beamforming matrix, $f_{B,b}, 1 \leq b \leq N_{bB}$ is the $b$th BS beam, and $N_{bB}$ is the number of transmit beams. The pilot signal $s_{B}(t) \triangleq [s_{B,1}(t), s_{B,2}(t), \ldots, s_{B,N_{bB}}(t)]^T$ has

$$s_{B,b}(t) = \sum_{\ell=0}^{N_s-1} a_{B,b,\ell}^*(t - \ell \tau_s), 1 \leq b \leq N_{bB},$$

where $a_{B,b,\ell}^*$ are known unit-energy pilot symbols transmitted over the $b$th beam from BS, and $p(t)$ is a unit-energy pulse with a power spectral density (PSD), denoted by $|P(f)|^2$. In (5), $N_s$ is the number of pilot symbols and $\tau_s$ is the symbol duration, leading to a total observation time of $T_o \approx N_s \tau_s$. Note that we keep the transmitted power fixed with $N_{bB}$ by setting $\mathbf{F}_{B}^H \mathbf{F}_{B} = 1$, and $s_{B}(t) \mathbf{F}_{B}^H(t) = \mathbf{I}_{N_{bB}}$, where $\mathbf{I}_{N_{bB}}$ denotes the matrix trace, and $\mathbf{I}_{N_{bB}}$ is the identity matrix.

Similarly, define the receive beamforming matrix at UE as $\mathbf{W}_{U} \triangleq [\mathbf{w}_{U,1}, \mathbf{w}_{U,2}, \ldots, \mathbf{w}_{U,N_{bU}}]$, where $\mathbf{w}_{U,k}, 1 \leq k \leq N_{bU}$ is a UE receive beam, and $N_{bU}$ is the number of receive beams.

2) Backward Channel: Channel from UE to BS is

$$\mathbf{H}^b(\beta, \vartheta) \triangleq \mathbf{H}^b(\beta, \vartheta) \delta(t - \tau^b), \in \mathbb{C}^{N_B \times N_U}$$

where $\mathbf{H}^b(\beta, \vartheta) \triangleq \sqrt{N_B N_U} \mathbf{a}_{B}(\theta_B, \phi_B) \mathbf{a}^\dagger_{\beta}(\theta_U, \phi_U)$, such that $\tau^b$ denotes the local TOA at BS, $(\theta_U, \phi_U)$ and $(\theta_B, \phi_B)$ are the backward DOAs and DODs at UE and BS, respectively. We assume that both transmissions occur within the coherence time so that the channel gain remains unchanged. In the backward transmission, UE transmits with a beamforming matrix, $\mathbf{F}_{U}$ containing $N_{bU}$ beams, while BS receives via a beamforming matrix, $\mathbf{W}_{B}$ containing $N_{bB}$ beams. Both $\mathbf{F}_{U}$ and $\mathbf{W}_{B}$ are defined similar to $\mathbf{W}_{U}$ and $\mathbf{F}_{B}$, respectively, but with possibly different beam directions.

Our objective is to derive the error bounds of estimating $\mathbf{p}$ and $\mathbf{o}$, from TOA, DOA, and DOD, obtained through DLP, in the presence of timing offset, $B$, and path gain, $\beta$, as nuisance parameters.

III. DISTRIBUTED TWO-WAY LOCALIZATION PROTOCOL

In our formulation, we assume that the UE has a clock bias with respect to the BS clock, denoted by $B$. We denote the propagation delay (nominal TOA) by $\tau = ||\mathbf{p}||/c$, where $c$ is the speed of light. See Fig. 2.

The forward transmission is initiated by the BS at time $t = 0$, and received at UE at local time

$$t = \tau^f + B + \tau.$$ (7)

Consequently, the observed signal after beamforming at the UE is given by

$$y_{U}(t) = \sqrt{E_0} \mathbf{W}^H_{U} \mathbf{H}^b(\beta, \vartheta) \mathbf{F}_{B} s_{B}(t - \tau^f) + \mathbf{n}_{U}(t).$$ (8)

Denoting the real and imaginary parts of $\mathbf{H}^b$ by $\mathbf{H}^b_R$ and $\mathbf{H}^b_I$, we find the FIM of $[\mathbf{H}^T, \mathbf{H}^b, \beta_R, \beta_I]_b^T$ based on $\mathbf{y}_{U}(t)$.

On the other hand, the backward transmission is initiated by the UE at time $t = t^b$, and received by BS at a local time

$$t = \tau^b = \tau^b + B - \tau.$$ (9)
After a pre-agreed delay $\tau^D$, measured from the time $y_U(t)$ is received, UE sends back a signal $s_U(t)$ at $t^b = t^f + \tau^D$.

Subsequently, BS receives the signal $y_B(t)$ at
\[ \tau^b = t^f + \tau^D + \tau - B = 2\tau + e^f + \tau^D. \] (10)

Thus, the observed signal after beamforming at BS is
\[ y_B(t) = \sqrt{E}W_B^H \mathbf{H}_B(\beta, \theta)F_{US}(t - \tau^b) + n_B(t) \] (11)

Based on $y_B(t)$, BS estimates $\hat{\tau}^b$ and eventually determines $p$, and $o$. Note that $B$ in the forward and backward transmissions cancel out, and need not be estimated at UE. Thus, based on $y_B(t)$, the FIM of $[\theta^T, \beta_R, \beta_I, \tau^b]^T$ is determined.

Denoting the equivalent FIMs (EFIMs) of $\tau^f$ and $\tau^b$ by $J_{\tau^f}$ and $J_{\tau^b}$, respectively, we introduce the following estimation error notation
\[ e^f \triangleq \hat{\tau}^f - \tau^f, \quad \text{and} \quad e^b \triangleq \hat{\tau}^b - \tau^b, \] (12)

such that
\[ \mathbb{E}\{(e^f)^2\} \geq J_{\tau^f}^{-1}, \quad \mathbb{E}\{(e^b)^2\} \geq J_{\tau^b}^{-1}. \] (13)

Finally, since the received signals are observed at the beamformer output, the noise terms in (8) and (11) are zero-mean additive spatially-correlated Gaussian noise. Therefore, the corresponding noise autocovariance matrices are $\mathbf{R}_{nu} = N_0\mathbf{W}_U^H\mathbf{W}_U$, and $\mathbf{R}_{nb} = N_0\mathbf{W}_B^H\mathbf{W}_B$ where $N_0$ is the noise PSD, which is assumed to be identical at BS and UE.

IV. Derivation of PEB and OEB for DLP

The PEB and OEB can be computed from the EFIM of position and orientation, $J_{\hat{\theta}, \hat{\phi}}$. 

\[ \text{OEB} \triangleq \sqrt{J_{\hat{\theta}, \hat{\phi}}_{1,1} + J_{\hat{\theta}, \hat{\phi}}_{2,2}}, \] (14)

\[ \text{PEB} \triangleq \sqrt{J_{\hat{\theta}, \hat{\phi}}_{3,3} + J_{\hat{\theta}, \hat{\phi}}_{4,4} + J_{\hat{\theta}, \hat{\phi}}_{5,5}}. \] (15)

Since $J_{\hat{\theta}, \hat{\phi}}$ is obtained by transforming the FIM of channel parameters, we start by computing this FIM. Then, we derive PEB and OEB using a parameter transformation procedure similar to [10].

1) FIM of Channel Parameters: In light of (6), (10) and (11), the vector of the unknowns under DLP is defined by
\[ \varphi_D \triangleq [\theta^T, \beta_R, \beta_I, \tau]^T. \] (16)

Consequently, the FIM of $\varphi_D$ is defined as
\[ J_{\varphi_D} \triangleq \begin{bmatrix} J_{\theta, \theta} & 0_6 \\ 0_6^T & J_{\tau, \tau} \end{bmatrix}, \] (17)

where,
\[ J_{\theta, \theta}^{b,b} = \begin{bmatrix} J_{\theta, \theta}^{b,b} & J_{\theta, \beta_R}^{b,b} \\ J_{\theta, \beta_R}^{b,b} & J_{\beta_R, \beta_R}^{b,b} \end{bmatrix}^T, \] (18)

is the FIM corresponding to the spatial part of $J_{\varphi_D}$. The value of $J_{\tau, \tau}$ as well as the entries of (18) are derived in the Appendix. Note that, as discussed in [10],

![Fig. 2. The timeline of the distributed TWL protocol](image-url)

the temporal and spatial parts in (17) are independent based on realistic mmWave assumptions: large number of transmit and receive antennas, large bandwidth and spatially sparse channel. Moreover, note that in (18), we used the fact that $J_{\beta_R, \beta_R}^{b,b} = J_{\beta_R, \beta_R}^b$.

While we can determine $J_{\tau, \tau}$ based on $y_U(t)$, the FIM of $[\theta^T, \beta_R, \beta_I, \tau^b]^T$ is based on $y_B(t)$. Hence, to obtain the FIM of $\varphi_D$ that includes $\tau$ rather than $\tau^b$, we apply the fact that the delays are independent of any other parameter [10]. Towards that, recall that $\tau^b = 2\tau + e^f + e^b + \tau^D$, and define
\[ \tau' \triangleq \frac{\tau^b - \tau^D}{2} = \tau + \frac{e^f + e^b}{2}. \] (19)

Consequently, using (13) yields
\[ \mathbb{E}\{(\tau' - \tau)^2\} \geq \frac{1}{4}(J_{\tau, \tau}^{-1} + J_{\tau, \tau}^{-1}) \] (20)

that is,
\[ J_{\tau, \tau} = 4(J_{\tau, \tau}^{-1} + J_{\tau, \tau}^{-1})^{-1}. \] (21)

2) FIM of Location Parameters: To obtain the FIM of the location parameters (position and orientation), we need the EFIM of $\theta$ and $\tau$. Since the temporal and spatial parts in (17) are independent, the EFIM of DOD and DOA is obtained from (18) by Schur’s complement
\[ J_{\theta, \theta}^{b,b} = J_{\theta, \theta}^b - \frac{1}{J_{\beta_R, \beta_R}^b} [J_{\theta, \beta_R}^b(J_{\beta_R, \beta_R}^b)^T]. \] (22)

Consequently, the EFIM of $\theta$ and $\tau$ is given by
\[ J_{\theta, \theta}^{s,s} = \begin{bmatrix} J_{\theta, \theta}^{s,s} & 0_4 \\ 0_4^T & J_{\tau, \tau} \end{bmatrix}. \] (23)

Applying a parameter transformation to (23), we obtain the EFIM of orientation and position
\[ J_{\hat{\theta}, \hat{\phi}}^{s,s} = \mathbf{Y} J_{\theta, \theta}^{s,s} \mathbf{Y}^T, \] (24)

where $\mathbf{Y} \triangleq \begin{bmatrix} \mathbf{Y}_s & \mathbf{Y}_r \end{bmatrix}$ is UL transformation matrix,
\[ \mathbf{Y} \triangleq \begin{bmatrix} \frac{\partial \theta}{\partial \varphi} & \frac{\partial \theta}{\partial \psi} & \frac{\partial \theta}{\partial \psi'} & \frac{\partial \theta}{\partial \psi''} \\ \frac{\partial \phi}{\partial \varphi} & \frac{\partial \phi}{\partial \psi} & \frac{\partial \phi}{\partial \psi'} & \frac{\partial \phi}{\partial \psi''} \end{bmatrix}, \] (25)

such that [10]
\[ \mathbf{Y}_s = \begin{bmatrix} 0 & 0 & \frac{p_r}{a^2} & \frac{p_r p_r''}{a^2} \\ 0 & 0 & p_r' \sin \chi_0 - \frac{p_r' p_r''}{a^2} \cos \chi_0 - \frac{\psi''}{a^2} \sin \chi_0 + \frac{\psi'''}{a^2} \\ -\frac{p_r}{a^2} & \frac{p_r p_r'}{a^2} & \frac{p_r}{a^2} & \frac{p_r p_r' p_r''}{a^2} \\ \frac{\psi'}{a^2} & \frac{\psi'}{a^2} & \frac{\psi'}{a^2} & \frac{\psi'}{a^2} \end{bmatrix}, \] (26)

\[ \mathbf{Y}_r = \begin{bmatrix} 0_4 & \frac{p_r}{a^2} \frac{p_r'}{a^2} \frac{p_r''}{a^2} \end{bmatrix}^T, \] (27)
where $g \triangleq p_y \cos \zeta_0 - p_x \sin \zeta_0$, $\mathbf{p}_\theta \triangleq [p_x p_z, p_y p_z, -a^2]^T$, $a \triangleq \sqrt{p_x^2 + p_y^2}$, $d' \triangleq \sqrt{p_x^2 + p_y^2}$, $[p'_x, p'_y, p'_z]^T \triangleq \mathbf{R} \mathbf{p}$, and $\mathbf{R} \triangleq [r_1, r_2, r_3] = \begin{bmatrix} \cos \zeta_0 & -\sin \zeta_0 \cos \chi_0 & -\sin \zeta_0 \sin \chi_0 \\ \sin \zeta_0 & \cos \zeta_0 \cos \chi_0 & \cos \zeta_0 \sin \chi_0 \\ 0 & -\sin \chi_0 & \cos \chi_0 \end{bmatrix}$.

Subsequently, for DLP, we can isolate the spatial and temporal parts and write,

$$J_{O,P}^{b} = J_{\tau}^{b} \mathbf{Y}_{\tau}^T + J_{\tau}^{b} \mathbf{Y}_{\tau}^T.$$

(27)

3) Performance Comparison of DLP with OWL: To compare DLP with OWL, recall that for OWL, $J_{O,P}^{b}$ has the same expression as (27), but with $J_{\tau}^{b} = J_{\tau}^{b}$. Therefore, in comparison with (21), DLP outperforms OWL when

$$J_{\tau}^{b} < 4 (J_{\tau}^{b} + J_{\tau}^{b})^{-1} = J_{\tau}^{b} \frac{4J_{\tau}^{b}}{J_{\tau}^{b} + J_{\tau}^{b}},$$

which leads to $J_{\tau}^{b} > \frac{1}{4} J_{\tau}^{b}$.

This means that, when the bandwidth is equal in both directions, the forward link should have at least one third the SNR of the backward link for DLP to outperform OWL. From Appendix A in [13], it can be seen that this mainly depends on the transmit and receive beamforming.

V. SIMULATION RESULTS AND DISCUSSION

In this section, we numerically investigate and compare the DLP and OWL. Since DLP involves forward and backward transmission, we select equal number of antennas at the BS and the UE to make a fair comparison. Towards that, we consider a BS and a UE both with $12 \times 12$ uniform rectangular antenna array communicating via a LOS. Moreover, we assume that the BS array is located in the $x$-$z$-plane centered about the 3D origin, thus has orientation of $[0^\circ, 0^\circ]$T. The UE is located in a diamond shape area defined by $(0, 0, 0)$, $(0, 25\sqrt{3}, 25)$, $(25\sqrt{3}, 0)$, $(0, 25\sqrt{3}, 25)$, and $(-25\sqrt{3}, -25)$. That is, the BS height is 10 meters.

We focus on two cases of orientation: $\mathbf{o} = [0^\circ, 0^\circ]^T$ and $\mathbf{o} = [15^\circ, 15^\circ]^T$. Finally, at a distance $d_0$, the channel gain is modeled as

$$\beta = \frac{\lambda}{4\pi d_0} \exp(j2\pi d_0),$$

(28)

We select $f = 38$ GHz, and $W = 125$ MHz, transmitted power $E_t/T_s = 0$ dBm, $N_0 = -170$ dBm/Hz, and $N_s = 64$ pilot symbols. We further assume an ideal sinc pulse-shaping filter with $W^2_{\text{eff}} = W^2/3$. Similar to [10], we adopt fixed directional beamforming with $N_{\text{bt}} = N_{\text{bt}} = 25$ such that

$$\mathbf{f}_{\text{B},b} = \frac{1}{\sqrt{N_{\text{bt}}}} a_{\text{B}}(\theta_{\text{B},b}, \phi_{\text{B},b}),$$

$$\mathbf{w}_{\text{B},b} = \frac{1}{\sqrt{N_{\text{bt}}}} a_{\text{B}}(\theta_{\text{B},b}, \phi_{\text{B},b}),$$

$$1 \leq b \leq N_{\text{bt}}.$$
to BS. This can result in a loss of beamforming gain that depends non-linearly on the UE location.

B. OEB with $0^\circ$ and $15^\circ$ UE Orientation

Considering OEB with $0^\circ$ and $15^\circ$ UE orientation in Fig. 4, it can be seen that DLP and OWL exhibit identical performance. Note that OEB depends on DOA and DOD, while the enhancement of DLP over OWL is in the temporal domain. Moreover, in comparison with the case of matched orientation, the system can still provide sub-meter PEB under $15^\circ$ mis-orientation, while providing significantly higher OEB. This means that orientation estimation is more challenging than position estimation.

C. Impact of the System Bandwidth on PEB

In Section V-A, we concluded that the system is limited by the estimation of the angles rather than the time delay. To investigate this further, we now look closer into the impact of the bandwidth. The results shown in Fig. 5 indicate that as the bandwidth increases, the PEB decreases before reaching a floor at around 100 MHz, which leads to the following observations.

Firstly, at the high bandwidths relevant in mmWave, the temporal information is very high compared to the spatial information, and the performance becomes fixed with $W$, leading the systems to be spatially-limited. Moreover, under mis-orientation, the accuracy of spatial information degrades, and the improved temporal information does not provide any benefit to the performance achieved at lower bandwidths. Furthermore, at lower bandwidths, the amount of temporal information decreases and becomes comparable to the spatial information. Therefore, the weight of the temporal information in the forward transmission becomes more significant, and the OWL and DLP diverge.

D. Impact of $N_B$ and $N_U$ on PEB

We now study the effect of the number of antennas at BS and UE on the PEB under DLP. Fig. 6 illustrates the effect of $N_U$ and $N_B$ on PEB. Note that the PEB curves with respect to $N_U$ are obtained with a fixed $N_B = 144$, and vice versa. It can be seen from Fig. 6 that a higher $N_U$ generally results in a worse performance. This is because with higher $N_U$, the UE beams become narrower, which requires more beams to cover the area.

Moreover, it can be deduced that a higher $N_B$ will slightly improve the PEB in general. Similar to the case in of $N_U$, it is understood that the PEB will generally increase when $N_B$ increases, albeit, at $N_B$ values well beyond those displayed in Fig. 6, and with a lesser magnitude than higher $N_U$. Therefore, adding more antennas at the BS will not reduce the localization performance, as the UE antennas potentially would, at least within the studied range of array size.

Finally, notice that Fig. 6 exhibits some non-monotonic trend. This is due to the nature of directional beamforming, whereby the beamforming gain depends on the user location, number of antennas, and beams directions as detailed in [14].

VI. CONCLUSIONS

Many papers on localization assume that the BS and UE are tightly synchronized. However, usually communication is not synchronized to a high-level useful for localization. Focusing on this issue, in this paper, we considered distributed localization protocol (DLP) and investigated the corresponding PEB and OEB. From the results of the numerical simulation, there was no enhancement observed for DLP over the traditional one-way localization in terms of PEB and OEB. That is, the localization was angle-limited rather than delay-limited. For future work, multipath propagation would be a relevant extension, since scatterers may differ in the uplink and downlink, depending on the beam directions.

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APPENDIX

DERIVATION OF THE ELEMENTS OF $J_{\varphi_D}$

From (18), we define

$$J_{\varphi_D}^b \triangleq \begin{bmatrix} J_{\theta U}^b \theta_{U} & J_{\phi U}^b \phi_{U} & J_{\theta U}^b \theta_{U} & J_{\phi U}^b \phi_{U} \end{bmatrix}$$  \tag{29}

and

$$(J_{\varphi_D}^b)^T \triangleq \begin{bmatrix} J_{\theta U}^b \theta_{U} & J_{\phi U}^b \phi_{U} & J_{\theta U}^b \theta_{U} & J_{\phi U}^b \phi_{U} \end{bmatrix}$$  \tag{30}

For the case of zero-mean additive correlated Gaussian noise, the FIM of $\varphi_D$ defined in (16), is given by [15]

$$J_{xy}^b \triangleq \frac{1}{N_0} \int_0^{T_o} \Re \left\{ \frac{\partial \mu^H(t)}{\partial x} (W^H_W W^H_U) \right\} \frac{\partial \mu(t)}{\partial y} dt, \tag{31}$$

where $x, y \in \{ \theta_U, \phi_U, \theta_R, \phi_R, \beta, \gamma, \tau \}$, and $\mu(t)$ is the mean of the observation vector in (11), and $T_o$ is assumed to be long enough to receive the entire pilot signal. That is,

$$\mu(t) = \sqrt{N_B N_U} E_t B W^H_U a B a H W^H_U s_U (t - \tau).$$  \tag{32}

Differentiating $\mu(t)$ w.r.t channel parameters and substituting in (31), while defining $P_A \triangleq A(A^H A)^{-1} A^H$, and $\gamma \triangleq N_B N_U N_E / N_0$, it can be shown that

$$J_{\theta U}^b \theta_{U} = \gamma | \beta |^2 \left( a B F_U F^H_U a_U \right) \left( k B^T P W_B k_B \right), \tag{33a}$$

$$J_{\phi U}^b \phi_{U} = \gamma | \beta |^2 \left( a B F_U F^H_U a_U \right) \left( p B^T P W_B k_B \right), \tag{33b}$$

$$J_{\theta U}^b \theta_{U} = \gamma | \beta |^2 \left( a B F_U F^H_U a_U \right) \left( k B^T P W_B k_B \right), \tag{33c}$$

$$J_{\phi U}^b \phi_{U} = \gamma | \beta |^2 \left( p B^T P W_B k_B \right) \left( a B^T P W_B a_B \right), \tag{33d}$$

$$J_{\beta R}^b \beta_{R} = \gamma \Re \left\{ | \beta |^2 \left( a B F_U F^H_U a_U \right) \left( k B^T P W_B k_B \right) \right\} \tag{33e}$$

$$J_{\gamma R}^b \gamma_{R} = -\gamma \Im \left\{ | \beta |^2 \left( a B F_U F^H_U a_U \right) \left( k B^T P W_B k_B \right) \right\} \tag{33f}$$

$$J_{\tau U}^b \tau_{U} = \gamma \Re \left\{ | \beta |^2 \left( k B^T F_U F^H_U a_U \right) \left( p B^T P W_B a_B \right) \right\} \tag{33g}$$

$$J_{\phi R}^b \phi_{R} = \gamma \Re \left\{ | \beta |^2 \left( p B^T F_U F^H_U a_U \right) \left( a B^T P W_B a_B \right) \right\} \tag{33h}$$

$$J_{\beta U}^b \beta_{U} = -\gamma \Im \left\{ | \beta |^2 \left( k B^T F_U F^H_U a_U \right) \left( p B^T P W_B a_B \right) \right\} \tag{33i}$$

$$J_{\gamma U}^b \gamma_{U} = -\gamma \Im \left\{ | \beta |^2 \left( p B^T F_U F^H_U a_U \right) \left( a B^T P W_B a_B \right) \right\} \tag{33j}$$

where $k_B = \frac{\partial}{\partial \beta_B} a_B$, $p_B = \frac{\partial}{\partial \phi_B} a_B$, such that $t \in \{ B, U \}$. To compute $J_{\varphi_D}$ in (21), we extend the results in [10] to

$$J_{r B} = \frac{1}{4\gamma | \beta |^2 \pi^2 W^H_U \| a B^H P W_B a_B \|^2}, \tag{34a}$$

$$J_{r U} = \frac{1}{4\gamma | \beta |^2 \pi^2 W^H_U \| a B^H P W_B a_B \|^2} \tag{34b}$$

where,

$$W^2_U = \int_{-W/2}^{W/2} f^2 |P(f)|^2 df.$$

REFERENCES


