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## PAPER

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# First-principles microkinetic study of methane and hydrogen sulfide catalytic conversion to methanethiol/dimethyl sulfide on Mo<sub>6</sub>S<sub>8</sub> clusters: activity/selectivity of different promoters†

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A large fraction of the global natural gas reserves is in the form of sour gas, *i.e.* contains hydrogen sulfide (H<sub>2</sub>S) and carbon dioxide (CO<sub>2</sub>), and needs to be sweetened before utilization. The traditional amine-based separation process is energy-intensive, thereby lowering the value of the sour gas. Thus, there is a need to find alternative processes to remove, *e.g.*, hydrogen sulfide. Mo<sub>6</sub>S<sub>8</sub> clusters are promising candidates for transforming methane (CH<sub>4</sub>) and hydrogen sulfide into methanethiol (CH<sub>3</sub>SH) and dimethyl sulfide (CH<sub>3</sub>SCH<sub>3</sub>), which are high-value sulfur-containing products that can be further used in the chemical industry. Here first-principles microkinetics is used to investigate the activity and selectivity of bare and promoted (K, Ni, Cl) Mo<sub>6</sub>S<sub>8</sub>. The results show that methanethiol is produced *via* two different pathways (direct and stepwise), while dimethyl sulfide is formed *via* a competing pathway in the stepwise formation of methanethiol. Moreover, there is an increase in activity and a decrease in selectivity when adding an electropositive promoter (K), whereas the reverse behaviour is observed when adding an electronegative promoter (Cl). When adding Ni there is also a decrease in activity and an increase in selectivity; however, Ni is acting as an electron donor. The results provide insights and guidance as to what catalyst formulation is preferred for the removal of hydrogen sulfide in sour gas.

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## 1 Introduction

Rational design of catalysts to obtain new or improved catalyst formulations with a highly selective conversion of hydrocarbon gas, such as methane (CH<sub>4</sub>), is of utmost importance in solving seminal petroleum industry processing problems. These problems include everything from energy carrier generation (*e.g.*, steam reforming and water gas shift on the supported Ni and CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalysts, respectively),<sup>1</sup> obtaining feedstock for a variety of commodity chemicals (*e.g.*, olefin metathesis of ethylene and 2-butene to produce propylene on supported metal oxide catalysts)<sup>2,3</sup> and environmental remediation of refinery tail gases

(*e.g.*, H<sub>2</sub>S oxidation on Al<sub>2</sub>O<sub>3</sub> or TiO<sub>2</sub> in the Claus process).<sup>4</sup> Yet, many fundamental aspects governing hydrocarbon catalyst conversion and selectivity are still not resolved because the underlying complex selectivity descriptors are still lacking.<sup>5</sup> Of particular interest is understanding the structure–selectivity relationships in metal oxide and metal sulfide catalysts for sour natural gas catalytic conversion.<sup>6</sup> Sour gas – mainly CO<sub>2</sub> and H<sub>2</sub>S – molecules are invariably present in natural gas and present significant challenges for conventional oxide-based catalysts including catalyst degradation and loss of activity. The Society of Petroleum Engineers (SPE) estimates that about 40% of the world's total accessible natural gas reserves are acidic, containing large concentrations of CO<sub>2</sub> and H<sub>2</sub>S, with over 10% H<sub>2</sub>S totaling up to 350 Tcf.<sup>7</sup> The concentrations of acidic gases can range up to 90% by volume and this sub-quality natural gas accounts for ~30% of U.S. natural gas resources<sup>8</sup> with the consequence that most of the gas is not utilized.<sup>9</sup> A conventional approach to sweeten natural gas includes *a priori* removal of these gases using alkanolamines, with the two most common being monoethanolamine (MEA) and diethanolamine (DEA), *via* solvent recycling and adsorption/desorption processes. Typically, the energy consumed during the amine regeneration step is 3.65 MJ kg<sup>−1</sup> CO<sub>2</sub>,<sup>10–12</sup> which significantly increases the cost of natural gas.

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† Electronic supplementary information (ESI) available: A zip file with all structures and figures of the reaction mechanism for the K-, Ni-, and Cl-promoted clusters, a free energy landscape, a comparison of the TOF for all clusters, tables with kinetic information, the steady-state coverages, the effect of the diffusion barrier on the TOF and selectivity, a degree of rate control analysis for all clusters, and the projected crystal orbital Hamiltonian populations. See DOI: 10.1039/c9cy00375d



A conceptually new approach recently emerged to catalytically transform both hydrocarbon and sour gas molecules into valuable products simultaneously *via* reactive separation.<sup>6</sup> In particular, hydrogen sulfide methane reforming<sup>13</sup> has been proposed at temperatures above 1000 °C with considerable amounts of carbonyl sulfide (COS) being formed. While H<sub>2</sub>S poisons conventional catalysts for steam reforming,<sup>14</sup> the overall process is thermodynamically limited and a series of supported catalysts have been utilized for this reaction, including metal oxides (Pt/Al<sub>2</sub>O<sub>3</sub>,<sup>15</sup> Mo,Cr/ZrO<sub>2</sub>-SBA15 (ref. 16), Mo,Cr/ZrO<sub>2</sub>-La<sub>2</sub>O<sub>3</sub> (ref. 16) and Fe<sub>2</sub>O<sub>3</sub>/γ-Al<sub>2</sub>O<sub>3</sub> (ref. 17)) and metal sulfides (MoS<sub>2</sub>,Cr<sub>2</sub>S<sub>3</sub> and Ce<sub>2</sub>S<sub>3</sub>).<sup>18–20</sup> The Langmuir–Hinshelwood–Hougen–Watson (LHHW) reaction mechanism on MoS<sub>2</sub> catalysts was proposed with the rate-determining step (RDS) being the reaction among the adsorbed species (CH<sub>3</sub><sup>\*</sup>, H<sub>2</sub>S<sup>\*</sup> and S<sup>\*</sup>) on the catalyst surface with the participation of three catalytic sites.<sup>19</sup> These catalysts have been used instead of thermal decomposition taking place at high (>70% for both CH<sub>4</sub> and H<sub>2</sub>S) conversion above 1250 °C.<sup>21</sup> In turn, CS<sub>2</sub> and COS have been shown to selectively react to form CH<sub>3</sub>SH on Ni-, K-, and Co-promoted MoS<sub>2</sub>/SiO<sub>2</sub>, providing indirect routes of acidic gas processing to CH<sub>3</sub>SH.<sup>22–25</sup> On the other hand, CH<sub>3</sub>SH, which is isostructural with CH<sub>3</sub>OH,<sup>26</sup> can be further converted into higher hydrocarbons. Chang and Silvestri<sup>27</sup> utilized H-ZSM-5 at 480 °C to convert CH<sub>3</sub>SH into a mixture of hydrocarbons and H<sub>2</sub>S with 7.0% selectivity towards C<sub>2</sub> and C<sub>3</sub> olefins with a significant amount of the carbon feed converted to dimethyl sulfide (DMS). Butter *et al.*<sup>28</sup> claimed overall 96.1% conversion of CH<sub>3</sub>SH with significant amounts of CH<sub>4</sub> generated at 258 °C on Al-exchanged H-ZSM-5. Similarly, Mashkina *et al.*<sup>29</sup> identified the presence of CH<sub>4</sub> when CH<sub>3</sub>SH was reacted on various acid catalysts between 350 and 400 °C, while at lower temperatures DMS was the only product observed. In general, large amounts of CH<sub>4</sub>, DMS and coke were observed in addition to the BTX (benzene, toluene, xylene) products formed.<sup>30–32</sup> Insights from density functional theory (DFT) calculations have suggested less favorable free energy reactive pathways for CH<sub>3</sub>SH as compared with CH<sub>3</sub>OH for the same acidity catalysts due to the differences in charge transfer between the organic species and the zeolite framework.<sup>33–35</sup> DMS, on the other hand, was shown to yield 15.4% C<sub>2</sub>H<sub>4</sub> in the product stream using WO<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub>, with CH<sub>4</sub> and C<sub>3</sub>H<sub>6</sub> comprising the rest at 380 °C and 32% conversion.<sup>36</sup> Hence, obtaining partially activated CH<sub>4</sub> analogues, such as CH<sub>3</sub>SH and CH<sub>3</sub>SCH<sub>3</sub>, to be converted to higher olefins as opposed to a complete reforming from sour gas streams is of direct interest.

In this work, we utilize DFT to investigate the activity and selectivity of bare and promoted Mo<sub>6</sub>S<sub>8</sub> clusters toward methanethiol (CH<sub>3</sub>SH) and DMS (CH<sub>3</sub>SCH<sub>3</sub>) using first-principles microkinetics. Earlier studies have shown that the stable and highly symmetric Mo<sub>6</sub>S<sub>8</sub> cluster has many promising properties, *e.g.* large CO binding energy<sup>37</sup> and large dipole moment<sup>38</sup> and a number of other optical

and reactive properties.<sup>39–43</sup> We expand our previous work<sup>44</sup> by adding diffusion steps in a phenomenological manner in the reaction mechanism in order to consider multiple reaction pathways and thereby selectivity. We utilize bare and K-, Cl- or Ni-promoted Mo<sub>6</sub>S<sub>8</sub> clusters as a versatile and tunable H<sub>2</sub>S-tolerant catalyst material.<sup>37,39,40,44,45</sup>

## 2 Computational details

### 2.1 Electronic structure calculations

Periodic DFT calculations were performed as implemented in the VASP code.<sup>46–49</sup> The projector augmented wave (PAW) method of Blöchl,<sup>50</sup> as adapted by Kresse and Joubert,<sup>51</sup> was used to describe the effective interaction between the valence electrons and the core. The exchange-correlation energy was described by the spin-polarized version of the PBE.<sup>52</sup> The Brillouin zone was sampled using the *Γ*-point only. The Kohn–Sham equations have been solved self-consistently in a plane-wave basis set with a cutoff of 400 eV. The convergence criterion for the electronic self-consistency cycle, measured by the change in the total energy between successive iterations, was set to 10<sup>−6</sup> eV. The electronic structures of the different clusters were analyzed and are shown in Fig. S10† using the crystal orbital Hamiltonian populations projected on the nearest neighbour orbitals using the LOBSTER software.<sup>53–56</sup>

### 2.2 Structural optimization calculations

Transition states have been identified using the DIMER method,<sup>57</sup> as improved by Heyden *et al.*<sup>58</sup> The atomic positions were considered relaxed if all forces acting on the atoms were less than 0.005 eV Å<sup>−1</sup>. Transition states were proven to be first-order saddle points of the potential energy surface using vibrational analysis. The intrinsic reaction coordinates (IRCs)<sup>59,60</sup> for the forward and backward reaction steps were identified using the damped velocity Verlet algorithm.<sup>61</sup> The structures corresponding to potential energy minima along the IRC were further relaxed using a conjugate-gradient algorithm in order to satisfy the same optimization criterion as for transition states. Vibrational analysis was performed to ensure that the relaxed structures correspond to true potential energy minima. This procedure guarantees that reactant and product states are linked through one single transition state. Optimized structures are provided in the ESI† (Fig. S1–S3).

### 2.3 Microkinetic modelling

The reaction kinetics were investigated using energies and vibrational frequencies as calculated from DFT. The rate constants for the reaction between reaction intermediates were



expressed using the conventional transition state theory (TST),<sup>62</sup>

$$k_{\text{TST}} = \frac{k_{\text{B}}T}{h} \frac{Z^\ddagger}{Z} \exp\left(-\frac{\Delta E}{k_{\text{B}}T}\right) = \frac{k_{\text{B}}T}{h} \exp\left(-\frac{\Delta G}{k_{\text{B}}T}\right), \quad (1)$$

where  $Z^\ddagger$  and  $Z$  are the internal partition functions of the transition state and initial state, respectively,  $\Delta E$  is the zero-point corrected energy difference, and  $\Delta G$  is the free energy difference. The free energy differences were evaluated using the Atomic Simulation Environment software package (ASE v3.15.0).<sup>63,64</sup>

Adsorption of CH<sub>4</sub>, H<sub>2</sub>S, CH<sub>3</sub>SH, H<sub>2</sub>, and DMS was considered to be direct with rate constants expressed as

$$k_{\text{ads}} = \frac{A_{\text{s}}}{(2\pi mk_{\text{B}}T)^{1/2}}, \quad (2)$$

where  $A_{\text{s}}$  is the area of the site, and the desorption is defined through the equilibrium

$$K_{\text{eq}} = \frac{k_{\text{ads}}}{k_{\text{des}}} = \exp\left(-\frac{G_{\text{ads}}}{k_{\text{B}}T}\right), \quad (3)$$

where the energy of adsorption of species A (CH<sub>4</sub>, H<sub>2</sub>S, CH<sub>3</sub>SH, H<sub>2</sub>, or DMS) is calculated as

$$E_{\text{ads}} = E_{\text{A}^*} - (E_{\text{*}} + E_{\text{A(g)}}) \quad (4)$$

The CH<sub>4</sub>:H<sub>2</sub>S pressure ratio was kept at 1:12 in the kinetic calculations in order to simulate conditions necessary to avoid coke formation.<sup>16</sup>

In addition to the transition state (TS) steps and the barrierless adsorption/desorption (ads/des) steps, we also considered the diffusion steps between different clusters (diffusion) in a parametric way. From practical consideration this was done by introducing a low barrier (0.05 eV) and treating diffusion using TST.

Here we will assume a Langmuir–Hinshelwood reaction mechanism<sup>62</sup> over a double site, using a double site notation [A\*,B\*], symbolizing adsorption on a –S–Mo– site with A adsorbed on S and B on Mo; all reaction steps are described in Table 1. We ignore the possibility of an Eley–Rideal mechanism<sup>62</sup> since Eley–Rideal is usually less probable<sup>62,65</sup> as compared to Langmuir–Hinshelwood. In addition, we do not include a Mars–Van Krevelen mechanism<sup>62</sup> since under industrial reaction conditions sulfur is in excess and the cost of creating a sulfur vacancy (Mo<sub>6</sub>S<sub>7</sub>) is calculated to be 2.4 eV, while the energy cost of adding one sulfur to Mo<sub>6</sub>S<sub>8</sub> is 0.2 eV (here the reference state for sulfur is H<sub>2</sub>S–H<sub>2</sub>), which indicates that a reaction mechanism including Mo<sub>6</sub>S<sub>7</sub> clusters is unlikely. The inclusion of Eley–Rideal and Mars–Van Krevelen mechanisms is a future challenge that is beyond the scope of this study.

**Table 1** All reactions used in the microkinetic model using the double site notation [A\*,B\*], for adsorption on a –S–Mo– site with A adsorbed on S and B on Mo. The right column indicates how the reaction was treated

Reaction	Type
H <sub>2</sub> S(g) + [*,*] ⇌ [*,H <sub>2</sub> S*]	Ads/des
[*,H <sub>2</sub> S*] ⇌ [H*,SH*]	TS
[H*,SH*] + [*,*] ⇌ [H*,*] + [*,SH*]	Diffusion
CH <sub>4</sub> (g) + [*,*] ⇌ [*,CH <sub>4</sub> ]	Ads/des
[*,CH <sub>4</sub> ] ⇌ [H*,CH <sub>3</sub> ]	TS
[H*,CH <sub>3</sub> ] + [*,*] ⇌ [H*,*] + [CH <sub>3</sub> *,*]	Diffusion
[H*,*] + [H*,*] ⇌ [H*,H*]	Diffusion
[H*,H*] ⇌ [*,H <sub>2</sub> ]	TS
[*,H <sub>2</sub> ] ⇌ [*,*] + H <sub>2</sub> (g)	Ads/des
[CH <sub>3</sub> *,*] + [*,SH*] ⇌ [CH <sub>3</sub> *,SH*] + [*,*]	Diffusion
[CH <sub>3</sub> *,SH*] ⇌ [*,CH <sub>3</sub> SH*]	TS
[*,CH <sub>3</sub> SH*] ⇌ [*,*] + CH <sub>3</sub> SH(g)	Ads/des
[*,SH*] ⇌ [H*,S*]	TS
[S*,H*] + [*,*] ⇌ [*,S*] + [H*,*]	Diffusion
[CH <sub>3</sub> *,*] + [*,S*] ⇌ [CH <sub>3</sub> *,S*] + [*,*]	Diffusion
[CH <sub>3</sub> *,S*] ⇌ [*,CH <sub>3</sub> S*]	TS
[H*,*] + [CH <sub>3</sub> S*,*] ⇌ [H*,CH <sub>3</sub> S*] + [*,*]	Diffusion
[H*,CH <sub>3</sub> S*] ⇌ [*,CH <sub>3</sub> SH*]	TS
[CH <sub>3</sub> S*,*] + [CH <sub>3</sub> *,*] ⇌ [CH <sub>3</sub> *,CH <sub>3</sub> S*] + [*,*]	Diffusion
[CH <sub>3</sub> *,CH <sub>3</sub> S*] ⇌ [*,CH <sub>3</sub> SCH <sub>3</sub> ]	TS
[*,CH <sub>3</sub> SCH <sub>3</sub> ] ⇌ [*,*] + CH <sub>3</sub> SCH <sub>3</sub> (g)	Ads/des

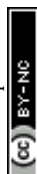
Selectivity between DMS and methanethiol is defined as the ratio between the TOF of DMS and the sum of the direct and stepwise TOF of methanethiol.

The ensuing non-linear differential equations were integrated numerically using the SciPy Python package, which relies on the ODEPACK Fortran library.<sup>66,67</sup>

### 3 Results and discussion

The calculated formation energies of the reactions CH<sub>4</sub> + H<sub>2</sub>S → CH<sub>3</sub>SH + H<sub>2</sub> and 2CH<sub>4</sub> + H<sub>2</sub>S → CH<sub>3</sub>SCH<sub>3</sub> + 2H<sub>2</sub> are –0.84 eV and –1.57 eV, respectively. This is in fair agreement with the experimental formation energies,<sup>68</sup> which are –0.75 eV and –1.37 eV, respectively.

The bare Mo<sub>6</sub>S<sub>8</sub> cluster forms a face-capped octahedral cluster where the Mo atoms sits in octahedral positions and the S atoms occupy the face of the octahedron. The Mo–Mo and Mo–S distances are 2.62 Å and 2.44 Å, respectively. There is a charge transfer from the molybdenum atoms to the more





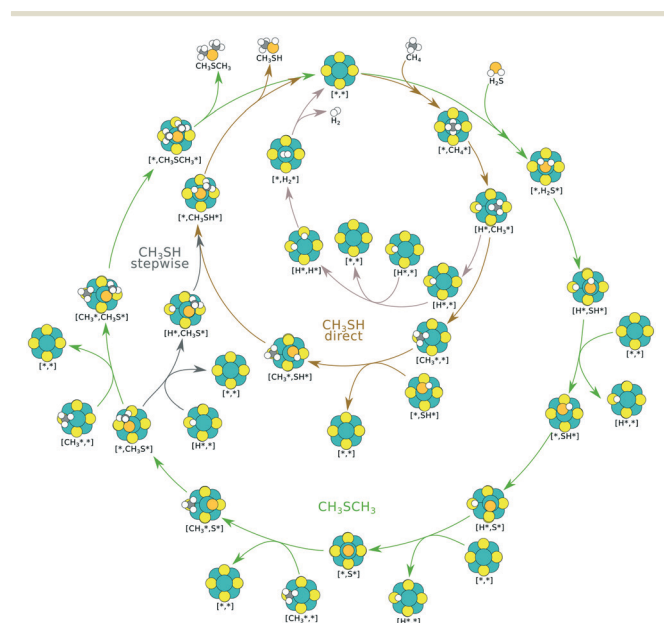
electronegative sulfur atoms. A Bader analysis<sup>69–72</sup> shows a 0.7–0.8 excess of electrons per atom on the sulfur atoms, while the molybdenum atoms lose close to one whole electron per atom.

The promoters (K, Ni, and Cl) affect the structural and electronic properties of the  $\text{Mo}_6\text{S}_8$  cluster in different ways. K adsorbs in a bridge position between two S atoms, with a bond distance of 3.00 Å, but there is no noticeable distortion in the  $\text{Mo}_6\text{S}_8$  cluster owing to the adsorption. However, K acts as an electron donor, and *via* a Bader charge analysis we observe an additional charge of 0.2 and 0.1 electrons per atom to the sulfur and molybdenum atoms close to the adsorption site. Ni also adsorbs in the bridge position (bond distance of 2.15 Å) between two sulfur atoms. However, there are noticeable structural changes in the cluster; in particular, the sulfur atoms adjust so that the Ni promoter gains access to the two underlying molybdenum atoms. The Ni–Mo distances (2.43 Å and 2.60 Å) are not symmetric. However, according to the Bader charge analysis, Ni transfers 0.2 electrons almost symmetrically between the two coordinating molybdenum atoms. In marked difference with the other promoters, Cl coordinates to one molybdenum atom (bond distance 2.33 Å). There is a charge transfer to Cl (0.4 electrons) which comes from the molybdenum atom (0.2 electrons) coordinated to Cl and symmetrically from all sulfur atoms in the cluster.

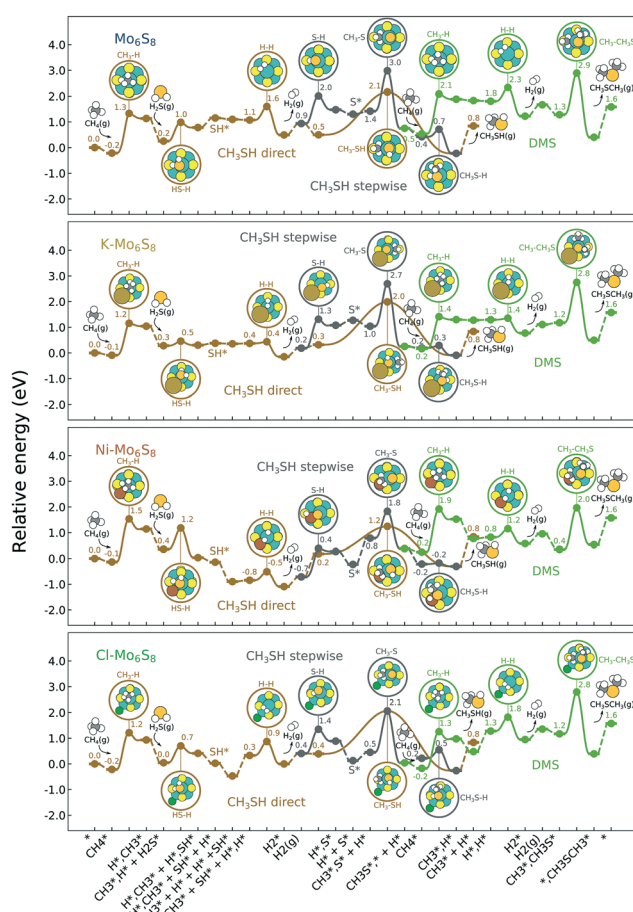
The proposed reaction mechanism of  $\text{CH}_4$  and  $\text{H}_2\text{S}$  conversion to methanethiol and DMS is shown in Fig. 1 for the bare cluster (see Fig. S1–S3† for K-, Ni-, and Cl-promoted clusters). The reaction mechanism can be divided into three

parts: (i) activation of reactants ( $\text{CH}_4$  and  $\text{H}_2\text{S}$ ), (ii) formation of methanethiol where two different pathways are considered (one direct route,  $\text{SH}^* + \text{CH}_3^*$ , and one associative route that involves atomic  $\text{S}^*$ ), and finally (iii) coupling of  $\text{CH}_3\text{S}^*$  and  $\text{CH}_3^*$  to DMS. The stepwise methanethiol and DMS pathway has one common reaction intermediate, namely  $\text{CH}_3\text{S}^*$  adsorbed on the Mo site. Depending on which reaction intermediate, either hydrogen or methyl, occupies the accompanying sulfur site, methanethiol or DMS will be formed. There is also a number of diffusion steps included in the reaction mechanism, which are important as this allows relevant reaction intermediates to pair up according to the dual site notation shown in Fig. 1.

The reaction energy landscape of  $\text{CH}_4$  and  $\text{H}_2\text{S}$  conversion to methanethiol and dimethyl sulfide is shown in Fig. 2, where all energies are referenced to the empty cluster with



**Fig. 1** Proposed reaction mechanism for the conversion of  $\text{CH}_4$  and  $\text{H}_2$  to methanethiol and DMS. The production of methanethiol occurs along two different pathways (direct and stepwise), while the production of DMS is a competing path in the stepwise reaction. Color code: hydrogen, white; carbon, black; sulfur, yellow ( $\text{Mo}_6\text{S}_8$ ) or orange (adsorbed); and molybdenum, green.



**Fig. 2** Reaction energy landscape for the conversion of  $\text{CH}_4$  and  $\text{H}_2\text{S}$  to methanethiol and DMS. The production of methanethiol occurs along two different pathways (direct and stepwise), while the production of DMS is another path of the stepwise reaction. Energy (eV) with gas-phase  $\text{H}_2\text{S}$  and  $\text{CH}_4$  as reference is shown for the most important steps. The insets show the transition states for all the clusters and also the adsorption site of the different promoters and intermediates. All energies are referenced to the empty cluster with  $\text{CH}_4$  and  $\text{H}_2\text{S}$  in the gas phase. Color code: hydrogen, white; carbon, black; sulfur, yellow ( $\text{Mo}_6\text{S}_8$ ) or orange (adsorbed); molybdenum, green; potassium, brown; nickel, red; and chlorine, dark green.



CH<sub>4</sub> and H<sub>2</sub>S in the gas phase. The free energy landscape at 1400 K is shown in Fig. S4† and the rate constants and free energy barriers are listed in Tables S1–S4.† The activation of CH<sub>4</sub> on the bare and promoted Mo<sub>6</sub>S<sub>8</sub> cluster occurs through a weak physisorption state with an adsorption energy of −0.21 eV, −0.09 eV, −0.13 eV and −0.21 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively. From that state the C–H bond that coordinates to the cluster becomes activated and finally reaches a transition state with an energy of 1.32 eV (Mo<sub>6</sub>S<sub>8</sub>), 1.16 eV (K–Mo<sub>6</sub>S<sub>8</sub>), 1.53 eV (Ni–Mo<sub>6</sub>S<sub>8</sub>) and 1.22 eV (Cl–Mo<sub>6</sub>S<sub>8</sub>). The C–H bond distance at the transition state ranges between 1.73 Å and 1.91 Å, where the bond distance correlates with the transition state energy. The dissociative state [H\*, CH<sub>3</sub>\*] is endothermic with respect to the physisorbed state, with comparable energies (1.34 eV and 1.28 eV) for the bare and Ni–Mo<sub>6</sub>S<sub>8</sub>, while K–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub> are slightly less destabilized (1.13 eV and 1.15 eV).

On the other hand, the activation of H<sub>2</sub>S occurs through a rather strong chemisorption state with an adsorption energy of −0.88 eV, −0.76 eV, −0.78 eV and −0.89 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively. The transition state involves the activation of one of the H–S bonds. K–Mo<sub>6</sub>S<sub>8</sub> has the lowest barrier (0.18 eV), followed by Cl–Mo<sub>6</sub>S<sub>8</sub> (0.66 eV), Mo<sub>6</sub>S<sub>8</sub> (0.73 eV) and finally Ni–Mo<sub>6</sub>S<sub>8</sub> (0.82 eV). The dissociation is endothermic on Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub> with an energy of 0.53 eV and 0.37 eV, respectively. This is very different as compared to Ni–Mo<sub>6</sub>S<sub>8</sub> where the dissociation is exothermic with an energy of −0.32 eV. On K–Mo<sub>6</sub>S<sub>8</sub> the reaction is endothermic but with an energy of only 0.02 eV.

The next part involves the diffusion of hydrogen away from the sulfur part of the dual site. In the reaction energy landscape the separation of SH\* and H\* to two separate dual sites is shown first. Here it is clear that for the bare Mo<sub>6</sub>S<sub>8</sub> this process is strongly endothermic (0.47 eV), while for the Cl- and Ni-promoted clusters this process is exothermic with −0.39 eV and −0.18 eV, respectively. On K–Mo<sub>6</sub>S<sub>8</sub> the separation is slightly endothermic (0.07 eV). Similar results are found for the separation of CH<sub>3</sub>\* and H\* to two separate dual sites, where the reaction energy is 0.03 eV, −0.02 eV, −0.76 eV and −0.50 eV for Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively. However, the diffusion of H\* to the same dual site ([H\*, H\*]) displays a reverse trend where on the bare Mo<sub>6</sub>S<sub>8</sub> this process is exothermic (−0.11 eV), while the same process is endothermic on K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub> with an energy of 0.02 eV, 0.05 eV and 0.80 eV, respectively. The two H\* can associate and form H<sub>2</sub>\* on the molybdenum part of the dual site with a reaction barrier of 0.52 eV (Mo<sub>6</sub>S<sub>8</sub>), 0.06 eV (K–Mo<sub>6</sub>S<sub>8</sub>), 0.33 eV (Ni–Mo<sub>6</sub>S<sub>8</sub>) and 0.54 eV (Cl–Mo<sub>6</sub>S<sub>8</sub>). The formation of H<sub>2</sub>\* is endothermic irrespective of whether the cluster is promoted or not.

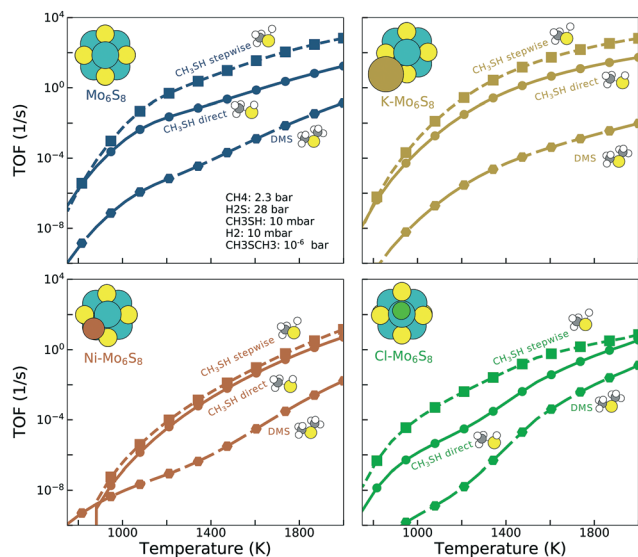
The direct pathway to methanethiol involves diffusion of CH<sub>3</sub>\* and SH\* to the same dual site. In the case of Mo<sub>6</sub>S<sub>8</sub> this step is exothermic with −0.53 eV, and −0.01 eV on Cl–Mo<sub>6</sub>S<sub>8</sub>, while for the K- and Ni-promoted clusters the diffusion is endothermic, 0.13 eV and 0.90 eV on K–Mo<sub>6</sub>S<sub>8</sub> and Ni–Mo<sub>6</sub>S<sub>8</sub>,

respectively. The next step in the formation of methanethiol occurs through a transition state that involves the formation of an S–C bond. The bond distance is calculated to be 2.53 Å, 2.60 Å, 2.52 Å, 2.61 Å with an energy barrier of 1.65 eV, 1.67 eV, 1.06 eV and 1.68 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively.

Besides the direct pathway there is also the possibility to further decompose SH\* into elementary S\*. The barrier of the transition state is 1.08 eV, 1.13 eV, 1.10 eV and 0.94 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively. The S–H bond distance at the transition state ranges between 1.74 Å and 2.76 Å and the different bond distances correlate with the transition state energy. The dissociation of SH\* is endothermic on all clusters. The diffusion of H\* from the same dual site is endothermic, with the exception of K–Mo<sub>6</sub>S<sub>8</sub> where this process is endothermic with 0.19 eV. The reverse behaviour in energy is observed for the diffusion of CH<sub>3</sub>\* to the sulfur part of the dual site occupied by S\*. The reaction between S\* and methyl occurs through a rather high energy barrier of 1.54 eV, 1.66 eV, 1.05 eV and 1.61 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively. The S–C bond distance at the transition state ranges between 2.53 Å and 2.60 Å. The formation of CH<sub>3</sub>S\* is exothermic on all clusters. Depending on which species diffuse to the empty sulfur site, the methylthiol can react to form methanethiol (stepwise pathway) or dimethyl sulfide. In the case of diffusion of H\* the reaction pathway is the same as the direct pathway but with an additional diffusion step, while in the case of diffusion of methyl the reaction can proceed to form dimethyl sulfide. In the reaction energy landscape (Fig. 2), to form dimethyl sulfide two additional steps (methane dissociation and hydrogen desorption) are necessary to keep the reaction stoichiometry. However, these are the same as described earlier. The diffusion of CH<sub>3</sub>\* to the same dual site as that of CH<sub>3</sub>S\* is exothermic, with the exception of K–Mo<sub>6</sub>S<sub>8</sub> where the reaction is slightly endothermic (0.07 eV). The barrier at the transition state is high (1.60 eV, 1.57 eV, 1.61 eV and 1.62 eV on Mo<sub>6</sub>S<sub>8</sub>, K–Mo<sub>6</sub>S<sub>8</sub>, Ni–Mo<sub>6</sub>S<sub>8</sub> and Cl–Mo<sub>6</sub>S<sub>8</sub>, respectively) and there is only a small change due to the addition of promoters. The formation is exothermic with the exception of Ni–Mo<sub>6</sub>S<sub>8</sub>. This is also reflected in the lower adsorption energy of dimethyl sulfide on Ni–Mo<sub>6</sub>S<sub>8</sub> (−1.04 eV) as compared to the other clusters, namely −1.18 eV (Mo<sub>6</sub>S<sub>8</sub>), −1.08 eV (K–Mo<sub>6</sub>S<sub>8</sub>) and −1.18 eV (Cl–Mo<sub>6</sub>S<sub>8</sub>).

The turnover frequencies (TOFs) (Fig. 3) under industrially relevant conditions for forming methanethiol and DMS are calculated in a microkinetic model based on the reaction mechanism shown in Fig. 1 and the energy landscape shown in Fig. 2. It is clear that the formation of methanethiol occurs mainly through the stepwise mechanism. The direct pathway becomes more important at lower temperature but consequently with a rather low TOF. It is also clear that the TOF for DMS is always low as compared to the TOF for methanethiol, the exception being Ni–Mo<sub>6</sub>S<sub>8</sub> at low temperatures (~900 K). K–Mo<sub>6</sub>S<sub>8</sub> displays a higher activity for methanethiol formation as compared to bare Mo<sub>6</sub>S<sub>8</sub> at temperatures higher than



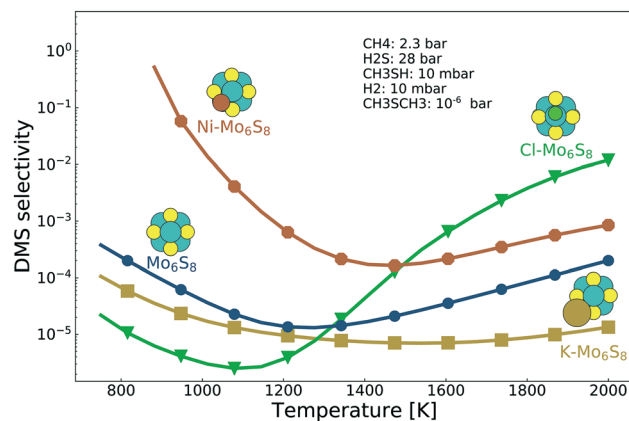


**Fig. 3** The turnover frequency as a function of temperature for the direct (dashed line and square point) and stepwise (solid line and circles) formation of methanethiol and DMS (dashed line and circles) for the bare  $\text{Mo}_6\text{S}_8$  (blue),  $\text{K-Mo}_6\text{S}_8$  (yellow),  $\text{Ni-Mo}_6\text{S}_8$  (red) and  $\text{Cl-Mo}_6\text{S}_8$  (green).

1200 K (see Fig. S5†); however, the production of DMS is lower over the whole temperature range. The reason behind the crossover in activity can be seen in the coverage of the active sites (Fig. S6†) where the number of free sites becomes larger on  $\text{K-Mo}_6\text{S}_8$  as compared to that on  $\text{Mo}_6\text{S}_8$  at 1300 K. This in turn is due to the weaker adsorption energy of  $\text{S}^*$  on  $\text{K-Mo}_6\text{S}_8$  as compared to  $\text{Mo}_6\text{S}_8$ .  $\text{Ni-Mo}_6\text{S}_8$  and  $\text{Cl-Mo}_6\text{S}_8$  are less active with respect to both methanethiol and DMS and also here the reason can be found in the coverage of the active site, as both clusters bind  $\text{S}^*$  too strongly (Fig. S6†), which thereby poisons the active site and prevents the reaction from proceeding. It is possible that the high coverage of  $\text{S}^*$  will lead to higher S-containing clusters, *i.e.*,  $\text{Mo}_6\text{S}_x$ ,  $x > 8$ ; however, this remains as a challenge for future investigation.

In contrast to a recent study<sup>44</sup> of the formation of methanethiol on bare and promoted  $\text{Mo}_6\text{S}_8$ , diffusion is included in the reaction mechanism but it is treated parametrically with an energy barrier of 0.05 eV. The sensitivity of the actual diffusion barrier is evaluated by changing the barrier to 0.005 eV and 0.5 eV. The effect on the TOF and the selectivity (see Fig. S7 and S8†) is only minor, which indicates that the exact height of the diffusion barrier is not important, although the addition of the diffusion step is crucial for the reaction mechanisms. A degree of rate control analysis (shown in Fig. S9†) confirms that the diffusion steps are crucial for the reactions to happen.

Selectivity between methanethiol and DMS is an important property when deciding the catalyst formulation. The selectivity between DMS and methanethiol, calculated as the ratio between the TOF for DMS and the TOF for methanethiol, is shown in Fig. 4. It is clear from the results that what benefit the K-promoted cluster has in activity is the reverse in selec-



**Fig. 4** The selectivity between methanethiol and DMS as a function of temperature for the bare  $\text{Mo}_6\text{S}_8$  (blue),  $\text{K-Mo}_6\text{S}_8$  (yellow),  $\text{Ni-Mo}_6\text{S}_8$  (red) and  $\text{Cl-Mo}_6\text{S}_8$  (green).

tivity. In contrast, the Ni-promoted and Cl-promoted clusters display higher selectivity as compared to the bare  $\text{Mo}_6\text{S}_8$ . There is a noticeable difference between the two promoted clusters as  $\text{Ni-Mo}_6\text{S}_8$  is several orders of magnitude higher in selectivity at low temperature, while  $\text{Cl-Mo}_6\text{S}_8$  surpasses the bare  $\text{Mo}_6\text{S}_8$  in selectivity first at a temperature of 1400 K (in fact,  $\text{Cl-Mo}_6\text{S}_8$  even surpasses  $\text{Ni-Mo}_6\text{S}_8$  at a temperature of 1500 K). The improved selectivity is closely connected with the poisoning effect of  $\text{S}^*$  (Fig. S6†).

## 4 Conclusions

The activity and selectivity of  $\text{CH}_4$  and  $\text{H}_2\text{S}$  to methanethiol and DMS are investigated by first-principles calculations using a microkinetic model. The proposed reaction mechanism includes a dual site (sulfur and molybdenum) and phenomenological diffusion between the dual sites. The reaction landscape involves several transition states and in particular there are two different pathways to form methanethiol (direct and stepwise). The stepwise pathway is part of the pathway to form DMS, which has adsorbed sulfur as a reaction intermediate.

The promoters fall into two categories; either the activity of the main product, methanethiol, is increased ( $\text{K-Mo}_6\text{S}_8$ ) or there is a loss in activity but with a gain in selectivity ( $\text{Ni-Mo}_6\text{S}_8$  and  $\text{Cl-Mo}_6\text{S}_8$ ). In the case of K and Cl, the effect is due to the electron-donor and electron-acceptor properties of the promoters. In the case of Ni the underlying reason is not as clear. Ni acts as an electron donor but still stabilizes the reaction intermediates to the extent that the dual site becomes poisoned. The results presented here highlight the balance between activity and selectivity when using promoters on  $\text{Mo}_6\text{S}_8$  clusters and can thus guide future catalyst formulation.

## Conflicts of interest

There are no conflicts to declare.





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