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Joint Localization and Mapping through Millimeter Wave MIMO in 5G Systems

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Abstract—Millimeter wave signals with multiple transmit and receive antennas are considered as enabling technology for enhanced mobile broadband services in 5G systems. While this combination is mainly associated with achieving high data rates, it also offers huge potential for radio-based positioning. Recent studies showed that millimeter wave signals with multiple transmit and receive antennas are capable of jointly estimating the position and orientation of a mobile terminal while mapping the radio environment simultaneously. To this end, we present a message passing-based estimator which jointly estimates the position and orientation of the mobile terminal, as well as the location of reflectors or scatterers. We provide numerical examples showing that our estimator can provide considerably higher estimation accuracy compared to a state-of-the-art estimator. Our examples demonstrate that our message passing-based estimator neither requires the presence of a line-of-sight path nor prior knowledge regarding any of the parameters to be estimated.

I. INTRODUCTION

A. Motivation and State of the Art

In many conventional wireless networks, accurate radio-based positioning relies on the existence of a line-of-sight (LOS) path between the transmitter and the receiver. Based on the signaling and antenna apertures, position-related parameters can be derived from the received signal. Such parameters include the time-of-arrival (TOA), angle-of-arrival (AOA), angle-of-departure (AOD), and received signal strength (RSS). Based on the capabilities of the systems, one or more of these parameters can be determined and leveraged for position estimation. For instance, lateration uses the TOAs with respect to multiple transmitters in order to obtain an estimate of the position of the receiver [1], while angulation employs the AODs with respect to multiple transmitters to estimate the position of the receiver [2]. In contrast to many conventional systems, the millimeter wave (mmWave) multiple input multiple output (MIMO) physical (PHY) layer proposal in 5G enables the determination of a triplet of position-related parameters for every received multipath component. Due to the high temporal and spatial resolution of mmWave MIMO, the TOA, AOD, and AOA of every multipath component can be estimated [3]–[5]. Due to this these triplets of position-related parameters, every non-line-of-sight (NLOS) path can be leveraged for position and orientation estimation [6]. Even in the absence of LOS, accurate positioning using only a single transmitter becomes possible if at least three NLOS paths exist [6]. Note that harnessing NLOS paths for position estimation clearly marks a paradigm shift in the field of radio-based positioning, where NLOS paths were conventionally considered as useless if no prior information is available [7].

Recently, different estimators have been presented in the literature which employ NLOS paths for position estimation and mapping [4], [8]–[10]. In [4], a least-squares approach with extended invariance principle (EXIP) is used to recover the position and orientation of the receiver from the TOAs, AODs, and AOAs. This approach can be used in the presence and absence of LOS. However in the absence of LOS, the approach requires to solve a large number of parallel least-squares (LS) problems. In particular, a fine-grained grid of trial orientations is created and one LS problem has to be solved for every point on the grid. The residuals of all solved problems are cached and only the solution with the lowest overall residual is retained. The drawback of this approach is that generally a fine granularity of the trial values for the orientation is required to achieve accurate estimates. In [8], a Gibbs sampling-based approach is presented where an iterative sampling process is executed. The Gibbs sampler starts with an initial guess regarding the position and orientation of the mobile. Based on this guess, the positions of the reflectors or scatterers are determined and the initial guesses on the position and orientation are updated sequentially. This procedure is repeated numerous times. A selection of all samples is retained and used for position and orientation estimation of the mobile, as well as for the estimation of the reflectors or scatterers. However, the authors in [8] did not show that their proposed Gibbs sampler works in the case of OLOS, i.e. when the LOS component is missing. In [9], [10], a sequence of observations including path delays and acceleration data is used to sequentially estimate the position of a mobile terminal and map the radio environment. This simultaneous localization and mapping (SLAM) approach requires multiple observations at different time instances.

B. Contribution and Paper Organization

We present a novel message passing-based estimator that uses the concept of nonparametric belief propagation to determine estimates on the position and orientation of the mobile terminal, as well as estimates on the locations of reflectors or scatterers. We show that our message passing-based estimator provides accurate estimates in the OLOS scenario. Our main

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1We refer to the scenario where only NLOS components are received as obstructed line-of-sight (OLOS).
contributions are summarized as follows:

- We propose a novel message-passing based estimator that jointly estimates the position and orientation of a mobile terminal along with the locations of the scatterers or reflectors in the case of OLOS without assuming any prior knowledge.
- The proposed estimator is capable of performing accurate single-snapshot SLAM even in the absence of the LOS path.
- Our numerical examples show that, in most cases, the root-mean-square error (RMSE) of the proposed estimator is significantly lower compared to the least-squares approach from [4].

The rest of the paper is organized as follows. Section II discusses our system model. In section III, we review the theory regarding our novel message passing-based estimator, while section IV describes the particle-based implementation of the estimator. Section V contains numerical examples and section VI concludes the paper.

II. System Model

A. System Model

Fig. 1 depicts a scenario with $J = 3$ NLOS paths scenario. We consider a base station (transmitter) and a mobile terminal (receiver). The base station is located at the position $q^* = [q_x^*, q_y^*]^T$, while the mobile terminal is at $p^* = [p_x^*, p_y^*]^T$. The position and orientation of the base station are perfectly determined and known to the mobile terminal. Without loss of generality, we assume that the base station is at the origin and its array is aligned with the y-axis. The received signal comprises $J \geq 3$ NLOS components with associated points of incidence $s^*_t = [s_{x,j}^*, s_{y,j}^*]^T, \forall j$. Generally, the number of NLOS components in the mmWave band is small [11]. In addition, due to the high path loss in the mmWave band, NLOS components are assumed to originate from single bounce scattering or reflection only [12]–[14]. We assume that the receiver determines a triplet of estimates (TOA, AOD, and AOA) for every path as described in, e.g., [4]. We refer to these estimates as observations and collect them in the vector

$$\mathbf{z} = [\hat{d}_0, \hat{\theta}_{TX,0}, \hat{\theta}_{RX,0}, \ldots, \hat{d}_{J-1}, \hat{\theta}_{TX,J-1}, \hat{\theta}_{RX,J-1}]^T, \quad (1)$$

where $\hat{\tau}_j, \hat{d}_j = c \cdot \hat{\tau}_j, \hat{\theta}_{TX,j}, \hat{\theta}_{RX,j}$ denote the estimates on the TOA, distance, AOD, and AOA of the $j$th path, respectively, and $c$ is the speed of light. Note that, for synchronized transmitter and receiver, we can substitute TOA with the distance by considering the speed of light. The observations related to the $j$th NLOS path are given by

$$\hat{d}_j = d_j + e_d, \quad (2a)$$

$$\hat{\theta}_{TX,j} = \theta_{TX,j} + e_{\theta_{TX,j}} = \arctan\left(\frac{s_{y,j} - q_y}{s_{x,j} - q_x}\right) + e_{\theta_{TX,j}}, \quad (2b)$$

$$\hat{\theta}_{RX,j} = \theta_{RX,j} + e_{\theta_{RX,j}} = \arctan\left(\frac{s_{y,j} - p_y}{s_{x,j} - p_x}\right) - \alpha + e_{\theta_{RX,j}}, \quad (2c)$$

where $\arctan2$ is the four-quadrant inverse tangent and $e_d$, $e_{\theta_{TX,j}}$, $e_{\theta_{RX,j}}$, $\forall j$ can be modeled as Gaussian distributed with zero mean and known variances $\sigma^2_d$, $\sigma^2_{\theta_{TX,j}}$, $\sigma^2_{\theta_{RX,j}}$ and $\sigma^2_{\theta_{RX,j}}$ [8], respectively. This assumption was originally introduced in [8], where it was observed that the observation errors which resulted from the considered TOA, AOD, and AOA estimator follow a Gaussian distribution. The variances of the observation errors generally depend on the signal-to-noise-power-ratio (SNR), the bandwidth, the antennas arrays, as well as the actual estimation algorithm. For a given estimator, these values can be obtained via simulation and stored in tables for different SNRs. Finally, we assume that the position and orientation of the mobile terminal and the points of incidence are independent of each other.

The goal of the mobile terminal is to estimate its own position and orientation, as well as the points of incidence based on the observations $\mathbf{z}$ in (1). We summarize these parameters in the vector

$$\mathbf{\eta} = [\mathbf{p}^T, \alpha, s_{0,0}^T, \ldots, s_{J-1}^T]^T. \quad (3)$$

III. Message Passing for Joint Positioning, Orientation Estimation, and Mapping

This section contains the theory required for the proposed message passing-based estimator. First, we derive the fac-
torized a posteriori distribution (short: posterior) and the corresponding factor graph. Based on this factor graph, we briefly review the concept of belief propagation and discuss the initialization of the message passing algorithm.

A. Factorized A Posteriori Distribution

The joint a posteriori distribution is proportional to

\[ p(\eta|d) \propto p(d|\eta)p(\eta), \] (4)

where the joint likelihood function \( p(d|\eta) \) can be factorized based on the conditional independencies described in section II, i.e.

\[ p(d|\eta) = \prod_{j=0}^{J-1} p(\hat{d}_j|p, s_j, q) p(\hat{\theta}_{TX,j}|s_j, q) \]
\[ \times p(\hat{\theta}_{RX,j}|s_j, p, \alpha), \]

and the joint a priori distributions (short: priors) can be factorized as follows:

\[ p(\eta) = p(p)p(\alpha) \prod_{j=0}^{J-1} p(s_j). \] (5)

The factors related to the distance, AOD, and AOA of the \( j \)th NLOS path in (5) are given by

\[ p(\hat{d}_j|p, q, s_j) \propto e^{-(d_j - |q - s_j|)|s_j - p||^2/2\sigma^2_{d,j}}, \] (7a)
\[ p(\hat{\theta}_{TX,j}|s_j, q) \propto e^{-\hat{\theta}_{TX,j} - \text{atan2}(\frac{s_j - q}{s_j - p})^2/2\sigma^2_{\theta_{TX,j}}} \] (7b)
\[ p(\hat{\theta}_{RX,j}|s_j, p, \alpha) \propto e^{-\hat{\theta}_{RX,j} - \text{atan2}(\frac{s_j - q}{s_j - p} + \alpha)^2/2\sigma^2_{\theta_{RX,j}}}, \] (7c)

respectively. Note that due to the nonlinear factors in (7a)-(7c), the posterior distribution in (4) is also nonlinear. In addition, the posterior distribution has many local maxima. Hence it is difficult to obtain optimum estimates (e.g., maximum a posteriori (MAP) estimates) since numerical solvers will get stuck in these local extrema if the initial estimate is far away from the global optimum.

B. Factor Graph

We can visualize the factorized a posteriori distribution in a graphical way using the notion of factor graphs. For instance, the message from factor node \( \hat{d}_j \) to variable node \( s_j \) is computed as follows [15]

\[ \mu_{d_j \rightarrow s_j}(s_j) \propto \int p(\hat{d}_j|p, q, s_j) \times \mu_{p \rightarrow d_j}^{(l-1)}(p) \delta(q - q^*) dp dq, \] (8)

where the superscript \((l)\) refers to the iteration index, \( p(\hat{d}_j|p, q, s_j) \) is defined in (2a), \( \mu_{p \rightarrow d_j}^{(l-1)}(s_j) \) and \( \delta(q - q^*) \) are the incoming message from \( p \) and \( q \), respectively. Note that the integral in (8) cannot be solved in closed-form unless the position is perfectly determined, i.e. \( \mu_{p \rightarrow d_j}^{(l-1)}(s_j) = \delta(p - p^*) \).

For incoming messages of generic structure, we have to determine the marginals of \( p, \alpha, \) and \( s_j, \forall j \) via the points of incidence. We will use these observations in section III-D, to derive an initialization strategy.

C. Belief Propagation

In contrast to numerical solvers which try to find optimum estimates based on the high-dimensional joint posterior distribution (here \( \dim(\eta) = 3 + 2J \)), belief propagation determines the lower-dimensional marginal posterior distributions (short: marginals) (e.g., \( p(p|\hat{d}) \) with \( \dim(p) = 2 \approx \dim(\eta) \)) first. Estimates are obtained based on the marginals subsequently.

1) Message Filtering: Every factor node computes an outgoing message for every edge based on the function related to the factor node and all incoming messages, excluding the message from the edge for which the outgoing message is computed. For instance, the message from factor node \( d_j \) in Fig. 2 to the variable node \( s_j \) is computed as follows [15]

\[ \mu_{d_j \rightarrow s_j}(s_j) \propto \int p(\hat{d}_j|p, q, s_j) \times \mu_{p \rightarrow d_j}^{(l-1)}(p) \delta(q - q^*) dp dq. \] (8)

Fig. 2: Factor graph of the posterior distribution in (4). Messages are passed along the edges of the factor graph to iteratively determine the marginals of \( p, \alpha, \) and \( s_j, \forall j \).
2) Message Multiplication: Every variable node computes an outgoing message for every edge based on the product of the belief from the previous iteration and all incoming messages excluding the message from the edge for which the outgoing message is computed. For instance, the message from the variable node \( s_j \) to the factor node \( \theta_{RX,j} \) is given by

\[
\mu_{s_j \rightarrow \theta_{RX,j}}(s_j) = b_{s_j \rightarrow \theta_{RX,j}}^{(l-1)}(s_j) \mu_{\theta_{RX,j} \rightarrow s_j}^{(l)}(s_j) \mu_{d_j \rightarrow s_j}^{(l)}(s_j),
\]

where \( b_{s_j \rightarrow \theta_{RX,j}}^{(l-1)}(s_j) \) is the belief on \( s_j \) from the previous iteration, while \( \mu_{\theta_{RX,j} \rightarrow s_j}^{(l)}(s_j) \) and \( \mu_{d_j \rightarrow s_j}^{(l)}(s_j) \) are the incoming messages as depicted in Fig. 2.

The belief of the current iteration is computed as the product of all incoming messages and the previous belief. For the previous example,

\[
b_{s_j \rightarrow \theta_{RX,j}}^{(l)}(s_j) = b_{s_j \rightarrow \theta_{RX,j}}^{(l-1)}(s_j) \mu_{\theta_{RX,j} \rightarrow s_j}^{(l)}(s_j) \mu_{d_j \rightarrow s_j}^{(l)}(s_j).
\]

D. Initialization

Message passing algorithms are generally initialized by the leaf nodes of the graph [15]. Recall that we are considering the most general case, where we have no prior information regarding \( p, \alpha, \) and \( s_j \forall j \). Consequently, the base station node \( q \) is the only node with a non-uniform prior and belief propagation is initialized at this node. Recall that the base station’s position and orientation are perfectly known and, thus, a Dirac distribution \( \delta(q - q^*) \) is passed towards all connected nodes, where \( q^* \) is the true location of the base station. Note that in the upper part of the factor graph (dashed box in Fig. 2), message-flow is unidirectional, i.e. no messages are sent back to the base station since its position is perfectly determined. We choose the following sequence of messages for initialization: 1) \( \mu_{\theta_{TX,j} \rightarrow s_j}, \forall j \), 2) \( \mu_{s_j \rightarrow d_j} = \mu_{\theta_{TX,j} \rightarrow s_j}, \forall j \), 3) \( \mu_{d_j \rightarrow p}, \forall j \), 4) \( \mu_{p \rightarrow d_j}, \forall j \) and \( \mu_{p \rightarrow \theta_{RX,j}}, \forall j \), 5) \( \mu_{d_j \rightarrow s_j}, \forall j \), 6) \( \mu_{s_j \rightarrow \theta_{RX,j}}, \forall j \), 7) \( \mu_{\theta_{RX,j} \rightarrow \theta_{TX,j}}, \forall j \), 8) \( \mu_{\theta_{RX,j} \rightarrow p}, \forall j \) and \( \mu_{\theta_{RX,j} \rightarrow s_j}, \forall j \). After these sequences of messages, the factor nodes have incoming messages from all edges, and the beliefs are determined based on these messages. In all subsequent iterations, a so-called flooding schedule is used to update messages [16].

Remark: Note that the initialization strategy is not unique. We chose the aforementioned sequence of messages for initialization to reduce the uncertainty of the messages which are sent along the edges of the factor graph. For instance, \( \mu_{\theta_{TX,j} \rightarrow s_j} \) is basically a cone of infinite length originating at \( q^* \) with mean angle \( \theta_{TX,j} \). By incorporating the information regarding \( p \) invoked in step 4) (which is sent back to \( s_j \) via \( \mu_{d_j \rightarrow s_j} \), in step 5)), the message \( \mu_{s_j \rightarrow \theta_{TX,j}} \) remains a cone but with finite length which reduces the uncertainty considerably.

IV. PARTICLE-BASED MESSAGE COMPUTATION AND ESTIMATION

First, we briefly review the concept of importance sampling to approximate the continuous messages by sets of weighted samples (particles). Afterwards, we explain how the continuous messages in (8) and (9) are approximated by sets of particles. Finally, we explain how to obtain estimates of the parameters based on their beliefs. For notational convenience, we drop the iteration-superscript in this section.

A. Importance Sampling

To perform belief propagation, we have to have means to compute the outgoing messages. The filtering operation in (8) requires solving an integral which cannot be solved in closed-form in general. Since all messages can be interpreted as probability distributions, our goal is to draw samples from these distributions without computing these distributions explicitly. To that end, we employ importance sampling.

In importance sampling, we wish to obtain a set of samples \( x^{(k)}, k = 1, ..., N_s \) from \( p(x) \) which cannot be sampled directly. In our context \( p(x) \) is any outgoing message, e.g., \( \mu_{\theta_{RX,j} \rightarrow s_j} \). Therefore, we draw \( N_s \) samples \( x^{(k)} \) from a suitable proposal distribution \( q(x) \) and attach a weight \( w^{(k)} \) to every sample. The weight accounts for the mismatch between \( p(x) \) and \( q(x) \) [17]. The combination of a sample and its weight is referred to as a particle \( \{w^{(k)}, x^{(k)}\} \). The unnormalized weight is given by [17]

\[
\tilde{w}^{(k)} = \frac{p(x^{(k)})}{q(x^{(k)})}.
\]

For numerical stability, we normalize all weights such that \( w^{(k)} = \tilde{w}^{(k)}/\sum_k \tilde{w}^{(k)} \). The set of samples with their associated weights is called particle representation of \( p(x) \), denoted by \( R_{N_s}(p(x)) \). Finally, we resample the particle representation to stochastically discard particles with very low weights [17]. After resampling all samples have equal weight, i.e. \( 1/N_s \).

B. Particle-based Message Computation

1) Message Filtering: At any factor node, assume that all incoming messages are given as particle representations and we wish to obtain a particle representation of an outgoing message. For instance, we want to obtain the particle representation \( R_{N_s}(\mu_{d_j \rightarrow s_j}^{(k)}) \) of \( (k) \) the incoming message \( \mu_{d_j \rightarrow s_j}^{(k)} \) based on the particle representation of the incoming message \( \mu_{\theta_{RX,j} \rightarrow s_j}^{(k)} \). Given a set of samples \( \{s_i^{(k)}\}_{i=1}^{N_s} \) from the proposal distribution \( q(s) \), the unnormalized weights are computed according to

\[
\tilde{w}^{(k)}_{s_i} = \frac{w^{(n)}_{s_i} p(d_j^{(n)}, q^*, s_i^{(k)})}{q(s_i^{(k)})}.
\]

2) Message Multiplication: At any variable node, assume that all incoming messages are given as particle representations and we wish to obtain a particle representation of an outgoing message. For instance, we want to obtain the particle representation \( R_{N_s}(\mu_{s_j \rightarrow \theta_{RX,j}}^{(k)}) \) of the product in (9) based on particle representations of the incoming messages and the previous belief. Since the samples of the incoming messages and the previously belief are drawn randomly and from independent proposal distributions,
they will be distinct with probability one. Direct message multiplication is therefore not possible.

To enable multiplication, interpolated versions of these messages (so-called kernel density estimates) are determined [17]. In kernel density estimation, each particle is coated with a continuous kernel and the superposition of all \( N_s \) kernels yields the resulting density. For a set of particles \( \{ u(k), x(k) \} \) from the distribution \( p(x) \), a kernel density estimate \( \hat{p}(x) \) is given by
\[
\hat{p}(x) = \sum_{k=1}^{N_s} w(k) N(x; x(k), \sigma_{KDE}^2 I),
\]
where \( N(x; x(k), \sigma_{KDE}^2 I) \) denotes the Gaussian distribution with mean \( x(k) \) and covariance matrix \( \sigma_{KDE}^2 I \).

Using kernel density estimates of the incoming messages and the previous belief, the current belief can also be determined using importance sampling. In particular, we draw a set of samples \( \{ s_j \} \) for each particle and adjust the weights according to
\[
\hat{w}_j = \frac{\hat{b}_a(s_j) \hat{p}_{\theta TX, T} \rightarrow \theta_j(s_j) \hat{p}_{\theta RX, T} \rightarrow \theta_j(s_j)}{q(s_j)},
\]
where \( \hat{b}_a(s_j) \) is with high probability \( \approx 1 \). We use such observations to confine the area of interest and draw samples efficiently. Regarding the kernel width \( \sigma_{KDE} \), we use a set of heuristic values as will be explained in section V. In general, \( \sigma_{KDE} \) can be determined using kernel density estimation algorithms [17]. However, we found that many of such algorithms fail to determine appropriate kernel widths which lead to convergence of the message passing algorithm.

V. NUMERICAL EXAMPLES

To assess the performance of our estimator, we performed simulations to (i) determine the speed of convergence and investigate the impact of the number of samples and (ii) examine the effect of varying measurement noise. For that purpose, we consider a scenario with \( J = 3 \) NLOS paths, where the points of incidence are spatially correlated in the AoD-domain: \( \theta_1 = [20, 10]^T \) m, \( \theta_2 = [80, -10]^T \) m, and \( \theta_3 = [40, 0]^T \) m. The mobile terminal is located at \( \theta_m = [70, 0]^T \) m and rotated by \( \alpha = 45^\circ \). For position-related messages, we use the following iteration-dependent \( \sigma_{KDE} = (7-l)^T \) m, while we use \( \sigma_{KDE} = (6-l \cdot 0.6)^\circ \) for angle-related messages. As the performance metric, we consider the RMSE. We estimate the RMSE using 1000 Monte Carlo trials. We treat the error of the points of incidence jointly, i.e., \( \theta_a = [\theta_0^T, \ldots, \theta_J^T]^T = [(\theta_1^T, \ldots, \theta_J^T)]^T \). As performance benchmark, we consider the LS approach from [4]. Recall that numerous LS solvers work in parallel each of which uses a different trial value \( \alpha_{trial} \). For fair comparison, we choose a very fine grid of \( \Delta \alpha_{trial} = 0.57^\circ \). Hence we solve 629 LS problems in parallel.

A. Convergence and Number of Samples

Fig. 3 depicts the RMSE of the position (top) and orientation (bottom) estimates against the number of iterations for fixed measurement noise \( \sigma_{\theta TX, k} = \sigma_{\theta RX, k} = 1^\circ \) and \( \sigma_{\theta S} = 0.2 \) m. For comparison, we also depict the performance of the LS estimator (solid, red horizontal lines). In both cases, the RMSE reduces with the number of iterations. The largest reduction of the RMSE occurs in the first few iterations. Note that the decrease is not monotonic. Especially, the RMSE of \( \theta \) shows some oscillating behavior which results from the flooding schedule mentioned in section III-D. Other schedules have to be investigated in future works to mitigate the oscillation. In addition, we observe that the estimation accuracy increases with the number of samples which gives rise to a complexity-accuracy trade-off.

B. Varying Measurement Noise

Fig. 4 depicts the RMSE of the position, point of incidence, and orientation estimates considering increasing angular measurement noise \( \sigma_{\theta TX, k} = \sigma_{\theta RX, k} \uparrow \) and fixed \( \sigma_{\theta S} = 0.2 \) m. We compare the RMSE of our message passing-based estimator (after 6 iterations) to the RMSE of the LS approach in [4]. We observe that, for \( \sigma_{\theta TX, k} = \sigma_{\theta RX, k} > 2^\circ \), our proposed estimator provides significantly lower RMSE compared to the LS approach. Especially, points of incidence can be estimated more precisely. When \( \sigma_{\theta RX, k} = \sigma_{\theta RX, k} \uparrow \) is large the initial
estimates of the LS solver are far from the global minimum and the solver tends to converge to a local minimum leading to its poor performance in terms of RMSE (see Fig. 4).

VI. CONCLUSIONS

We proposed a novel message passing-based estimator for 5G millimeter wave MIMO systems which jointly estimates the position, orientation and the locations of scatterers or reflectors based on distance, angle-of-departure, and angle-of-arrival measurements. Our estimator determines the position and orientation of a mobile terminal accurately, while simultaneously generating a precise map of the radio environment. Even in the absence of the LOS component and without assuming prior knowledge on any of the parameters, the position, orientation, and the locations of scatterers or reflectors are estimated reliably. Our approach also provides a measure of uncertainty of the estimates since it approximates the marginal a posteriori distributions of the parameters. For large measurement noise, our proposed algorithm performs very well in terms of the estimation accuracy and outperforms the state-of-the-art approach.

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Fig. 3: RMSE of \( p \) and \( \alpha \) versus number of iterations - The RMSE of position and orientation estimates decreases with the number of iterations. Increasing the number of samples results in higher estimation accuracy.

Fig. 4: RMSE of \( p \), \( s \), and \( \alpha \) versus angular measurement noise - The RMSE of the LS estimates increases drastically with increasing \( \sigma_{\theta_{RX}} \) and \( \alpha \), while the RMSE of the NBP estimates remains almost constant.