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Cost-optimal energy management of hybrid electric vehicles using fuel cell/battery health-aware predictive control

Xiaosong Hu, Senior Member, IEEE, Changfu Zou, Member, IEEE, Xiaolin Tang, Teng Liu, Member, IEEE, Lin Hu

Abstract—Energy management is an enabling technology for increasing the economy of fuel cell/battery hybrid electric vehicles. Existing efforts mostly focus on optimization of a certain control objective (e.g., hydrogen consumption), without sufficiently considering the implications for on-board power sources degradation. To address this deficiency, this article proposes a cost-optimal, predictive energy management strategy, with an explicit consciousness of degradation of both fuel cell and battery systems. Specifically, we contribute two main points to the relevant literature, with the purpose of distinguishing our study from existing ones. First, a model predictive control framework, for the first time, is established to minimize the total running cost of a fuel cell/battery hybrid electric bus, inclusive of hydrogen cost and costs caused by fuel cell and battery degradation. The efficacy of this framework is evaluated, accounting for various sizes of prediction horizon and prediction uncertainties. Second, the effects of driving and pricing scenarios on the optimized vehicular economy are explored.

Index Terms—Batteries, energy management, fuel cell, hybrid electric vehicle, predictive control, sustainable transport

I. INTRODUCTION

A. Motivation and Challenges

Increasingly severe fuel consumption and environmental pollution have been strongly pushing the academia and automotive sector to actively develop and deploy fuel cell hybrid electric vehicles (FCHEVs) [1]–[4]. FCHEVs diversify energy sources of mobility, enabling a good synergy of transportation and renewables [5]. The fuel cell-battery-motor coupling featured by FCHEVs is, however, quite complicated and directly influences overall vehicular performance [6], constituting the first challenge for system-level energy management. Unlike internal combustion engines (ICEs), the lifetime of the two electrochemical power sources (fuel cell and battery systems) is highly vulnerable to their operating conditions. This causes another challenge of how to coordinate the two energy units such that the vehicular total cost of ownership can be reduced. To address the two main challenges, we propose a look-ahead health-conscious energy management strategy to maximize the economy of an FCHEV.

B. Literature Review

Energy management of FCHEVs and ICE-included hybrid electric vehicles (HEVs) is certainly a vast field of research [7]–[9]. A large number of strategies have been proposed in the literature, which can be roughly divided into two categories, i.e., rule-based and optimization-based approaches. Each type has its own advantages and disadvantages.

Rule-based energy management is centered on heuristic rules governing the vehicle operating modes [10]. These rules are invariably derived from engineering experiences, as simple functions of battery and/or engine states. For example, when the battery State-of-Charge (SOC) exceeds a higher bound, the pure electric mode is adopted; when the battery SOC is lower than a lower bound, the ICE mode is operated. Common rule-based power management strategies include thermostat control [11], fuzzy logic [12], etc. Salient upsides of this type of method are simplicity, ease of real-time implementation, and strong resilience against driving patterns. For these reasons, rule-based methods are predominantly being used in HEVs in the current market. Nonetheless, the effects of these rules are typically far away from the optimality of vehicle design/control objectives, incenting alternatives to seek noticeable improvements.

Optimization-based energy management strategies have been actively developed in order to achieve better vehicular performance [9]. The overarching goal of this type of method is to optimize a predefined criterion, like fuel consumption, subject to a set of operational constraints, given a hybrid powertrain model [13]. Sometimes, multiple objectives are considered to investigate tradeoffs of different concerns [14]–[16]. As a globally optimal benchmark, dynamic programming (DP) was often exploited to develop a theoretically optimum energy management strategy and evaluate other algorithms...
prediction horizon and prediction uncertainties. Second, the work are carefully examined, considering different sizes of The performance and computational efficiency of this frame-
work was modified by means of a DP-refined rule-based controller in the inner loop [36], [37]. Due to the convexity, CP can guarantee a globally optimal solution with exceptionally fast calculation. The model simplification and convexification somewhat de-
grade the optimality, in contrast to DP. Typically, noncausal DP and CP can only be implemented offline, as driving cycles must be known beforehand. To explore the possibility of online optimized energy management, causal optimization methods, e.g., equivalent consumption minimization strategy (ECMS) [23], [24], Pontryagin’s Minimum Principle (PMP) [25], [26], and model predictive control (MPC) [27], [28], were adopted. These controllers with appropriate design and tuning always produce a satisfactory performance in energy consumption, operating cost, or the total cost of vehicle ownership.

A vast majority of existing studies on FCHEVs energy management merely consider how to minimize hydrogen consumption, without involving performance degradation of fuel cell/energy storage systems. The economy potential of FCHEVs is insufficiently assessed. A few papers attempted to establish power management strategies cognizant of the tradeoff between fuel cell health and hydrogen economy. For example, fuel efficiency, cost, and life-cycle carbon emissions of an FCHEV were optimized via the genetic algorithm in [29]. Fuel cell lifetime was governed by imposing constraints on fuel cell output power in ECMS [30], PMP [31], and CP [14] energy management controllers. A stochastic DP controller to minimize the summation of hydrogen and fuel cell costs was introduced in [32], [33] as well. However, these studies did not take energy storage degradation into consid-
eration. A battery health-aware power management strategy of an FCHEV equipped with hybrid energy storage was constructed via CP in [34], where the impact of fuel cell health was neglected. Xu et al. [35] incorporated both fuel cell and battery degradation models into a bi-loop framework for offline component sizing and DP-based energy management of an FCHEV. To reduce the computational burden, such a framework was modified by means of a DP-refined rule-based controller in the inner loop [36], [37].

C. Main Contributions

To the best knowledge of the authors, no efforts have been made to develop an FCHEV energy management strategy perceptive of the lifetime of both fuel cell and battery systems in a cost-optimal, predictive manner. In order to bridge such a research gap, this article presents two original contributions that distinguish our work from existing schemes. First, we devise an MPC framework, for the first time, to minimize the expenditure of an FCHEV, inclusive of hydrogen cost and costs associated with fuel cell and battery degradation. The performance and computational efficiency of this framework are carefully examined, considering different sizes of prediction horizon and prediction uncertainties. Second, the

The rest of the paper proceeds as follows. The FCHEV powertrain model is detailed in Section II. Section III introduces the MPC energy management framework. The control results under various driving cycles are given in Section IV. The implication of power-source pricing is discussed in Section V followed by conclusions summarized in Section VI.

II. FCHEV POWERTRAIN MODEL

Here, we consider a fuel cell hybrid bus powertrain, as sketched in Fig. 1. The widely-used quasi-static modeling method is leveraged to model the powertrain for a time-
efficient, accurate simulation [38], [39].

A. Configuration and Power Balance

An electric motor drives the bus with a hybrid power source composed of a proton-exchange-membrane fuel cell system (PEMFCS) and a lithium-ion battery system. A DC-DC converter is adopted at the side of the PEMFCS to regulate its current flow into the DC bus, while the battery system is passively connected. The specifications of the principle powertrain components are listed in Table I. The overall power balance equation is described by

\[ T_{em}(k)w_{em}(k) + P_{em,loss}(k) + P_{au}(k) = P_{bat}(k) + P_{fcs}(k)\eta_{dc}. (1) \]

where \( T_{em} \) and \( w_{em} \) are the motor torque and speed, respectively; \( P_{em,loss} \) is the motor loss as a function of \( T_{em} \) and \( w_{em} \); \( P_{bat} \) and \( P_{fcs} \) are the battery terminal power and the PEMFCS output power, respectively; \( \eta_{dc} \) is the averaged efficiency of the DC-DC converter; \( P_{au} \) is the power of auxiliaries that is assumed to be constant; \( k \) is the time index.

B. Motor Model

A permanent magnet synchronous motor is used to propel the bus and do regenerative braking. The efficiency and loss data of the motor taken from [20] are plotted in Fig. 2. The

Fig. 1: Configuration of the fuel cell hybrid electric bus.
### TABLE I. MAIN VEHICLE PARAMETERS.

<table>
<thead>
<tr>
<th>Component</th>
<th>Specifications</th>
</tr>
</thead>
<tbody>
<tr>
<td>PEMFCS</td>
<td>A 1000-cell stack</td>
</tr>
<tr>
<td></td>
<td>Power rating: 100 kW</td>
</tr>
<tr>
<td>Battery system</td>
<td>A 2000-cell pack</td>
</tr>
<tr>
<td></td>
<td>Energy capacity: 15.18 kWh</td>
</tr>
<tr>
<td>Motor</td>
<td>Maximum power: 220kW</td>
</tr>
<tr>
<td></td>
<td>Maximum speed: 3000rpm</td>
</tr>
<tr>
<td>DC-DC converter</td>
<td>Averaged efficiency: 96%</td>
</tr>
<tr>
<td>Final drive</td>
<td>Gear ratio: 4.7</td>
</tr>
<tr>
<td>Vehicle</td>
<td>Chassis mass: 13476kg</td>
</tr>
<tr>
<td></td>
<td>Auxiliary power: 7.0kW</td>
</tr>
</tbody>
</table>

*a* Adopted from [20]; *b* Adopted from [14]; *c* Adapted from [20].

Motor torque and speed meet the vehicular power demand as follows:

\[
w_{em}(k) = \frac{\lambda v(k)}{r} \quad (2a)
\]

\[
T_{em}(k) = \max(T_v(k), T_{em,\text{min}}(k)) \quad (2b)
\]

where \(v, \lambda,\) and \(r\) are the vehicle speed, final drive gear ratio, and wheel radius, respectively; \(T_{em,\text{min}}\) is the minimum negative torque during regenerative braking; \(T_v\) is the torque request on the shaft between the motor and the final drive, which can be readily derived by the vehicular longitudinal dynamics (the derivation is detailed in Appendix of [22]). In this study, the motor is sized enough to satisfy the propelling torque request of the bus. When the braking torque request exceeds \(T_{em,\text{min}}\), the conventional frictional braking is activated as a supplement.

### C. PEMFCS Model

1) **Hydrogen Consumption Model:** We herein consider a 1000-cell PEMFCS with a power rating of 100 kW for an electric bus, same as the fuel cell system used in [40], whose configuration is sketched in Fig. 3. Its main elements include a fuel cell stack and four auxiliary subsystems, i.e., hydrogen circuit, air circuit, water circuit, and coolant circuit [14], [22]. These auxiliaries consume a portion of the electricity generated by the stack to ensure a normal operation of the PEMFCS. A detailed description about how these subsystems work can be found in [41]. The quasi-static hydrogen consumption model, characterizing the relationship between the hydrogen power \(P_h\) and the PEMFCS output power \(P_{fcs}\), is a scaled version of FC\_ANL50H2 in ADVISOR [42], as indicated in Fig. 4.

2) **Health Model:** Performance degradation is an entrenched issue in electrochemical power sources. How to model the PEMFCS health evolution plays an important role in the economy-targeted power management of the bus. As recognized in electrochemistry community, a multitude of tangible and intangible factors impact membrane electrode assembly (MEA) degradation, resulting in a great challenge of establishing such a model. As introduced in [33], MEA performance degradation mainly originates from the following aspects.

a) **Catalyst layer degradation** [33]: electrochemical active surface area (ECASA) reduction occurs, owing to agglomeration, sintering together, and detachment of platinum particles [33], [43], oxidation of carbon support caused by fuel starvation at high or transient loading [44]–[47], production of surface oxides at very low loading [48]. It can be seen that the PEMFCS operating condition has a substantial influence on ECASA reduction. Extremum loads are very detrimental to the catalyst layer.

b) **Membrane degradation** [33]: fuel impurity, mechanical stress, and thermal stress lead to membrane degradation [44]–[46]. The former two are related to contaminants and congenital or assembly defects, respectively [44], [45]. They
are thus typically irrelevant to PEMFCS loading. However, thermal stress is dependent on the PEMFCS output power. Extensive heat at extremum loads may reduce the membrane protonic conductivity and incur membrane-drying-caused gas permeability [33], [44], [45].

c) Gas diffusion layer (GDL) degradation [33]: it has some overlapping aging mechanisms with the catalyst support. For example, fuel starvation at high or transient loading induces oxidation of carbon that is often exacerbated at high temperatures [33], [44], [45]. In addition, increased humidity at high loads may cause flooding [44], [49].

According to the foregoing descriptions [33], [44]–[49], the main MEA degradation mechanisms with respect to PEMFCS loading are summarized in Fig. 5. Since vehicular applications are invariably subject to drastically dynamic loading, it is of particular significance and practicality to carefully govern the PEMFCS loading (i.e., output power) to alleviate its performance degradation and increase the overall vehicular economy. It has been demonstrated in [32], [33], [40] that on/off loading has a predominately negative impact on the lifetime of PEMFCS, especially in heavy-duty vehicular applications. Therefore, as manipulated in [14], [22], [34], the bus PEMFCS is herein always on. We adopt a similar approach to [33], [40], so as to account for the effects of other loads. When the PEMFC output power $P_{fcs}$ is equal to or larger than 80% of the power rating, the voltage degradation rate per hour at high load is portrayed by $\gamma_{high}$; when the PEMFC output power $P_{fcs}$ is lower than 20% of the power rating, the voltage degradation rate per hour at low load is denoted by $\gamma_{low}$; the voltage degradation rate per kW during transient load change is depicted by $\gamma_{chg}$. The values of these rates used in this work are listed in Table I. As treated in [33], these sources of degradation are assumed to be mostly independent, and thus their effects can be summed up to embody the total voltage degradation.

D. Battery Model

1) Electrical Model: A 2000-cell lithium iron phosphate battery pack with the nominal energy capacity of 15.18 kWh is employed as the energy storage unit of the hybrid powertrain, whose configuration is illustrated in Fig. 6. Each battery cell is emulated by the internal resistance model as follows:

$$V_{cell}(k) = u(k) - i(k)R$$

(3)

where $V_{cell}$, $u$, $i$, and $R$ represent the terminal voltage, open-circuit voltage, current, and internal resistance of battery cell, respectively. Note that the open-circuit voltage $u$ is a monotonically increasing function of cell SOC, which is often provided by the manufacturer (see [50] for A123’s ANR26650m1 used here). Given the terminal cell power $P_{cell}(k) = V_{cell}(k)i(k)$ and (3), we can obtain the following current equation:

$$i(k) = \frac{u(k) - \sqrt{u^2(k) - 4RP_{cell}(k)}}{2R}$$

(4)

where $P_{cell}(k) = \frac{P_{soc}(k)}{I_{max}} = \frac{P_{soc}(k)}{t_{s}} = \frac{P_{soc}(k)}{2000}$. And then the SOC dynamics can be delineated by

$$soc(k+1) = soc(k) - \frac{i(k)\Delta t}{Q}$$

(5)

where $soc$, $Q$, and $\Delta t$ are the cell SOC, the nominal cell capacity, and the sampling interval, respectively. The following electrical constraints must be fulfilled when operating the hybrid powertrain:

$$i_{min} \leq i(k) \leq i_{max}$$

(6a)

$$soc_{min} \leq soc(k) \leq soc_{max}$$

(6b)

$$soc(0) = soc_0$$

(6c)

where $i_{min}$ and $i_{max}$ are the cell current bounds (maximum charge/discharge current); $soc_{min}$ and $soc_{max}$ are the SOC bounds, and $soc_0$ is the initial SOC.

2) Health Model: A semi-empirical battery aging model developed in [51] is adopted in this paper to simulate the capacity loss of the battery cell. This model was already widely used for vehicular energy management [52], battery charging control [53], power-source sizing [54], [55],

![Fig. 4: Hydrogen consumption model of the PEMFCS.](image)

![Fig. 5: Main MEA degradation mechanisms with respect to PEMFCS loading.](image)

TABLE II. PEMFCS DEGRADATION RATE (CELL LEVEL).

<table>
<thead>
<tr>
<th>Load</th>
<th>Degradation rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>High load</td>
<td>10.00 $\mu$V/h</td>
</tr>
<tr>
<td>Low load</td>
<td>8.662 $\mu$V/h</td>
</tr>
<tr>
<td>Load change</td>
<td>0.04185 $\mu$V/kWh</td>
</tr>
</tbody>
</table>

$^a$Adopted from [40]; $^b$Adapted from [33] and [40].
TABLE III. PRE-EXponential FACTOR AS A FUNCTION OF THE C-Rate [51].

<table>
<thead>
<tr>
<th>C-rate</th>
<th>0.5</th>
<th>2</th>
<th>6</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>M</td>
<td>31630</td>
<td>21681</td>
<td>12934</td>
<td>15512</td>
</tr>
</tbody>
</table>

The cell capacity loss is characterized by the following equation [51]:

\[
\Delta Q = M(c) \exp \left( \frac{-E_a(c)}{R_c T_c} A(c)^z \right)
\]

(7)

where \(\Delta Q\) is the percentage of capacity loss in [%], \(c\) is the C-rate, and \(M\) is the pre-exponential factor as a function of the C-rate, as indicated in Table III. The ideal gas constant is \(R_c\) (8.31 J/mol-K), \(T_c\) is the lumped battery temperature in [K], and \(A\) is the discharged ampere-hour (Ah) throughput. The activation energy \(E_a\) in [J/mol] and the power-law factor \(z\) are determined by [51]

\[
E_a(c) = 31700 - 370.3c \quad (8a)
\]

\[
z = 0.55. \quad (8b)
\]

When using [8] and Table III, 1C \((c = 1)\) corresponds to 2A [51], where a de-rated 2Ah was used to ease experimentation. 20\% capacity loss is considered as the end-of-life (EOL) of an automotive battery, and the total discharged Ah throughput \(A_{tol}\) is, therefore, acquired by

\[
A_{tol}(c, T_c) = \left[ \frac{20}{M(c) \exp \left( \frac{-E_a(c)}{R_c T_c} A(c)^z \right)} \right]^{1/z}. \quad (9)
\]

Then, the number of cycles until the battery EOL, \(N\), is attained by [52]

\[
N(c, T_c) = \frac{3600 A_{tol}(c, T_c)}{Q}. \quad (10)
\]

As a result, the State-of-Health (SOH) is defined below [52]:

\[
soh(t) = 1 - \frac{\int_0^t |i(\tau)| d\tau}{2N(c, T_c)Q}. \quad (11)
\]

The corresponding dynamic SOH model is thereby established as [52]

\[
soh(k + 1) = soh(k) - \frac{|i(k)| \Delta t}{2N(c, T_c)Q}. \quad (12)
\]

TABLE IV. MAIN ELECTRICAL SPECIFICATIONS OF THE BATTERY CELL.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>%Internal resistance</td>
<td>0.01 Ohm</td>
</tr>
<tr>
<td>%Nominal capacity</td>
<td>8280 As</td>
</tr>
<tr>
<td>%Maximal charge current</td>
<td>-35 A</td>
</tr>
<tr>
<td>%Maximal discharge current</td>
<td>70 A</td>
</tr>
<tr>
<td>%Maximal SOC</td>
<td>75%</td>
</tr>
<tr>
<td>%Minimal SOC</td>
<td>55%</td>
</tr>
<tr>
<td>%Initial SOC</td>
<td>65%</td>
</tr>
<tr>
<td>%Maximal SOH</td>
<td>100%</td>
</tr>
<tr>
<td>%Minimal SOH</td>
<td>0%</td>
</tr>
<tr>
<td>%Initial SOH</td>
<td>100%</td>
</tr>
</tbody>
</table>

\(a\) Adopted from [50]; \(b\) Adopted from [52].

Based on the SOH model, the values of \(N\) and SOH decline rate at various temperatures and C-rates can be easily calculated (e.g., see Fig. 15 in [53] with a C-rate with respect to the nominal capacity of 2.3 Ah). The following health constraints must be fulfilled when operating the hybrid powertrain:

\[
soh_{\text{min}} \leq soh(k) \leq soh_{\text{max}} \quad (13a)
\]

\[
soh(0) = soh_0 \quad (13b)
\]

where \(soh_{\text{min}}\) and \(soh_{\text{max}}\) are the SOH bounds, and \(soh_0\) is the initial SOH. The main electrical and SOH specifications of the battery are listed in Table IV.

III. MPC ENERGY MANAGEMENT FRAMEWORK

In this section, we mathematically formalize the predictive, cost-optimal power management strategy in an MPC framework.

A. Objective function

To minimize the total running cost of the bus over each prediction horizon, the objective function \(J\) includes four terms, which is defined by

\[
J_j = C_{h,j} + C_{fcs,j} + C_{bat,j} + D_{soc,j}, \quad j = 0, 1, 2 \ldots \quad (14)
\]

where

1) \(C_{h,j}\) is the hydrogen cost over the prediction horizon \(j\), i.e.,

\[
C_{h,j} = \sum_{m=j}^{j+T_h-1} \beta_h P_h(m) \Delta t, \quad j = 0, 1, 2 \ldots \quad (15)
\]

with \(T_h\) being the size of prediction/control horizon and \(\beta_h\) the hydrogen price per Joule.

2) The PEMFCs degradation cost \(C_{fcs,j}\) is computed by

\[
C_{fcs,j} = C_{\text{low},j} + C_{\text{high},j} + C_{\text{chg},j}, \quad j = 0, 1, 2 \ldots \quad (16)
\]

where \(C_{\text{low},j}\) is the degradation cost caused by low load, which is calculated by

\[
C_{\text{low},j} = \frac{\gamma_{\text{low}} P_{\text{low},j} M_{fcs}}{V_{fcs,cal}}, \quad j = 0, 1, 2 \ldots \quad (17)
\]
with $T_{low,j}$ being the duration of low load in hour over the prediction horizon $j$, $V_{fcs,ed}$ the voltage drop until the PEMFCS EOL (i.e., 10% voltage decrease of fuel cell at rated current [40]), and $M_{fcs}$ the PEMFCS cost, i.e., $M_{fcs} = 100\beta_{fcs}$ where $\beta_{fcs}$ is the PEMFCS price per kW. Moreover, $C_{high,j}$ is the degradation cost caused by high load, as defined by

$$C_{high,j} = \frac{\gamma_{high} T_{high,j} M_{fcs}}{V_{fcs,ed}}, \quad j = 0, 1, 2 \ldots$$  \hspace{1cm} (18)

with $T_{high,j}$ being the duration of high load in hour over the prediction horizon $j$. Then, $C_{chg,j}$ is the degradation cost caused by load change, which is derived by

$$C_{chg,j} = \frac{\gamma_{chg} M_{fcs} \sum_{m=j}^{j+T_h-2} |P_{fcs}(m+1) - P_{fcs}(m)|}{1000n_{fcs} V_{fcs,ed}}$$  \hspace{1cm} (19)

with $D_p$ being a large, positive constant.

### B. Constraints

Equations (1) and (2) enable us to only choose the PEMFCS output power $P_{fcs}$, as the optimization variable to reduce computational burden (the battery power $P_{bat}$ can be invariably represented as a function of $P_{fcs}$). And then, the constraints of the optimal control problem consist of $\{3, 4, 12, 13\}$, which can be described as functions of $P_{fcs}$, as well as the physical bounds on $P_{fcs}$.

$$P_{fcs, min} \leq P_{fcs}(k) \leq P_{fcs, max}$$  \hspace{1cm} (22)

with $P_{fcs, min}$ and $P_{fcs, max}$ equal to 0 and 100000, respectively.

### C. Framework formulation

Given the objective function and constraints above, the cost minimization problem over the prediction/control horizon at the time step $j$ can be mathematically framed as follows:

$$\min_{P_{fcs}(k), k=j+1, \ldots, j+T_h-1} J_j = C_{h,j} + C_{fcs,j}$$  \hspace{1cm} (23a)

s.t. $\forall k \in \{j, \ldots, j+T_h-1\}, q \in \{j+1, \ldots, j+T_h\}$,

$$soc(k+1) = soc(k) - \frac{i(k) \Delta t}{Q}$$  \hspace{1cm} (23b)

$$i_{min} \leq i(k) \leq i_{max}$$  \hspace{1cm} (23c)

$$soc_{min} \leq soc(q) \leq soc_{max}$$  \hspace{1cm} (23d)

$$soc(0) = soc_0$$  \hspace{1cm} (23e)

### IV. RESULTS AND DISCUSSIONS

In this section, we present optimization results via running the aforementioned MPC energy management framework. The baseline prices of the hydrogen, PEMFCS, and battery unit are given in Table V. As an example, the standard Manhattan bus cycle (MBC) from [22] is herein considered (see Fig. 7).

**Table V. Baseline Prices of the Hydrogen, PEMFCS, and Battery Unit.**

<table>
<thead>
<tr>
<th>Price</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydrogen</td>
<td>4.00 $/kg</td>
</tr>
<tr>
<td>PEMFCS</td>
<td>93.00 $/kW</td>
</tr>
<tr>
<td>Battery</td>
<td>178.41 $/kWh</td>
</tr>
</tbody>
</table>

*Adopted from [60], bAdopted from [61] with medium-volume manufacturing of 10000 units/year; cAdopted from [62].

Note that the current $i$ in (23) is only an expression of $P_{fcs}$, with the consideration of (1), (2) and (4). We harness sequential quadratic programming (SQP) algorithm to solve the optimal control problem (23), as this algorithm has been corroborated to work well in a spectrum of MPC engineering applications [57]–[59]. For the solution over the current horizon $[P_{fcs}(j), \ldots, P_{fcs}(j+T_h-1)]$, only the first element $P_{fcs}(j)$ is applied to the hybrid powertrain to evolve the system dynamics, while the remaining elements are discarded. Such a manipulation is repeated at the next time step $k+1$ and is called the receding-horizon principle.

**Fig. 7: MBC driving cycle [22]:** (a) speed and slope, (b) acceleration, (c) speed distribution, and (d) acceleration distribution.
shown in Fig. 8. The total running cost in MBC is approximately $1.5390, to which the hydrogen cost of $1.0331 contributes most. The PEMFCS degradation cost of about $0.3941 constitutes the second large expense, to which three sources, i.e., high load, low load, and load change, contribute. Clearly, the contribution of low load to the PEMFCS degradation is dominant. The battery degradation cost of $0.1118 is smallest, compared to those of hydrogen and PEMFCS degradation.

The optimized power split between the PEMFCS and the battery pack is depicted in Fig. 9 and the corresponding motor electric power is presented in Fig. 10. It is clear that the PEMFCS largely operates at low load to mitigate its degradation, with the aid of battery power variances. The associated trajectories of battery SOC and SOH are illustrated in Fig. 11. It can be found that the proposed MPC energy management solution works well to ensure the battery charge sustenance. The battery SOH decline is slight, less than 0.005%.

**B. Horizon effect**

In this subsection, we investigate how the size of the prediction/control horizon affects the optimization accuracy and computational burden. As shown in Fig. 12, the total running cost reduces, as the horizon size increases. The computational burden, however, becomes increasingly heavy, particularly when the size exceeds 10s. Therefore, the choice of the horizon size needs a balance between the optimality and computational efficiency for a specific case study. For example, as for low-cost energy controllers with limited computational capability, it is probably sensible to pick a relatively small horizon size, e.g., less than 5s, to assure real-time implementability. On the contrary, in the case of a computationally powerful controller, we most possibly prioritize the optimality over the computational load, so as to seek a large horizon size, e.g., greater than 9s.

**C. Effect of prediction uncertainty**

In the above discussion, we assume that the bus velocity trajectory in the prediction horizon is exactly known. This assumption is highly judicious, as bus routes are typically fixed, especially in city transit applications. With the development of vehicle-to-vehicle (V2V) and vehicle-to-infrastructure (V2I) communication, highly credible velocity predictors are expected even in the context of varying, complex routes. Vehicular velocity forecasting itself is a vast area of intensive studies, leading to a diversity of prediction methods. Please, for example, refer to [63], [64] for more related details. Since the main contributions and focus of this endeavor do not lie in velocity prediction, we straightforwardly evaluate how
potential prediction uncertainty influences the optimal cost by adding artificial Gaussian prediction errors of different standard deviations to the MBC data. To maintain physical viability, the contaminated negative velocity is set to zero. Take a prediction/control horizon $T_h = 5$ as an example. The associated result is illustrated in Fig. 13. It is clear that the optimized cost increases with augmented prediction error. When the standard deviation of the error equals to 1, the total cost virtually doubles, in contrast to the benchmark with perfect velocity. Hence, it is of great importance to obtain sufficiently precise velocity evolution, from a perspective of saving vehicular running cost.

It is worth mentioning that, in the case of imperfect velocity forecasting, as the prediction horizon increases, the prediction uncertainty most probably increases. Such an error increase may somewhat offset the optimality gain obtained by increasing the prediction horizon. As such, the performance improvement of the predictive controller resulting from the horizon increase may saturate. As a result, we cannot arbitrarily augment the prediction horizon, which should be decided by a nontrivial, comprehensive consideration of the prediction uncertainty, optimality gain, and computational load.

V. DRIVING AND PRICING IMPACT

In this section, the influence of driving and pricing scenarios on the optimization outcome is elucidated.

A. Driving Impact

In addition to MBC, we consider another two bus cycles, i.e., the standard city suburban cycle (CSC) and a realistic Gothenburg city cycle with slope knowledge (see Figs. 8 and 9 of [22]). In this way, how the driving pattern affects the optimal cost can be unveiled. Given $T_h = 5$, the total costs under the three driving cycles in $$/km are compared in Fig. 14. It is evident that the harshest MBC induces the highest expense, i.e., about $0.44/km. In MBC, the prime mover, PEMFCS, experiences the most dynamic loads, giving rise to higher hydrogen cost and PEMFCS degradation. In the other extremum, the smoothest CSC leads to the lowest expense, i.e., about $0.28/km (36.4% reduction versus MBC). In CSC, the hydrogen cost, PEMFCS cost, and battery cost are all lowest in the three cycles. The total expense in the Gothenburg cycle is in between MBC and CSC, i.e., $0.34/km (22.7% reduction versus MBC). In this cycle, the battery degradation is, however, largest, because the hilly driving requires more frequent utilization of the battery system.

B. Pricing Impact

We examine the pricing impact on the optimization result, through considering price evolutions of hydrogen, PEMFCS, and battery in the most recent three years (from 2017 to 2019). Table V is used as the baseline prices in 2017. The annual price increase of hydrogen is assumed to be 20%, due to increasingly serious energy shortage. The PEMFCS price decrease is from [61] (about 5% annually), while that of the battery is from [62] (about 11% annually), due to economies of scale and growing maturity of design/manufacturing technologies. The price evolutions are shown in Fig. 15.

The optimization results are plotted in Fig. 16. It is pronounced that the optimal cost gradually increases from 2017 to 2019. For example, in MBC, the increases in 2018 and 2019 reach 11.27% and 26.02%, respectively, with respect to the
impact the optimization results are investigated. Furthermore, how driving and pricing scenarios are assessed. The effectiveness and computational efficiency of this strategy are validated via numerous simulation campaigns, and the effects of prediction horizon and prediction uncertainties are assessed. The key findings include the following five points:

1) The proposed method presents an alternative idea for developing cost-optimal energy management strategies of fuel cell/battery hybrid electric vehicles.
2) How to pick an appropriate horizon size entails a trade-off between the optimality and computational efficiency, according to controller properties. As the horizon size becomes larger, the total running cost reduces, whereas the computational load increases.
3) Velocity prediction uncertainties thwart the reduction of total running cost. When the standard deviation of uncertainty equals to 1, the total cost of the bus increases by nearly 100%.
4) Driving patterns significantly influences the optimized cost. The highest expense, i.e., about $0.44/km, occurs in the harshest MBC. As the driving becomes smoother, we can accomplish 22.7% and 36.4% cost reductions in the Gothenburg and CSC cycles, respectively.
5) The potential price changes of hydrogen, PEMFCS, and battery will increase the optimized cost, due to predominantly augmented hydrogen cost. In MBC, the cost increases in 2018 and 2019 are 11.27% and 26.02%, respectively, versus the baseline case in 2017. The cost decreases of PEMFCS and battery degradation are very slight.

VI. CONCLUSIONS

This paper devises a cost-optimal, predictive energy management strategy for hybrid powertrains, which is cognizant of the lifetime of both fuel cell and battery systems. In the strategy, the total running expense of a PEMFC/battery hybrid electric bus, inclusive of hydrogen cost and costs of fuel cell and battery degradation, is minimized in an MPC setting. The effectiveness and computational efficiency of this strategy are validated via numerous simulation campaigns, and the effects of prediction horizon and prediction uncertainties are assessed. Furthermore, how driving and pricing scenarios impact the optimization results are investigated.

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