



Towards phonon routing: controlling propagating acoustic waves in the quantum regime

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Ekström, M., Aref, T., Josefsson Ask, A. et al (2019)

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New Journal of Physics, 21(12)

<http://dx.doi.org/10.1088/1367-2630/ab5ca5>

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PAPER

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OPEN ACCESS

RECEIVED

11 September 2019

REVISED

20 November 2019

ACCEPTED FOR PUBLICATION

28 November 2019

PUBLISHED

12 December 2019

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We explore routing of propagating phonons in analogy with previous experiments on photons. Surface acoustic waves (SAWs) in the microwave regime are scattered by a superconducting transmon qubit. The transmon can be tuned on or off resonance with the incident SAW field using an external magnetic field or the Autler–Townes effect, and thus the reflection and transmission of the SAW field can be controlled in time. We observe 80% extinction in the transmission of the low power continuous signal and a 40 ns rise time of the router. The slow propagation speed of SAWs on solid surfaces allows for in-flight manipulations of the propagating phonons. The ability to route short, 100 ns, pulses enables new functionality, for instance to catch an acoustic phonon between two qubits and then release it in a controlled direction.

1. Introduction

Quantum ElectroDynamics (QED) is a common platform to investigate strong coupling between light and matter, where both cavity and waveguide based systems have shown functionality in terms of quantum information processing [1–5]. In waveguide QED based on superconducting circuits, a single atom in an open system interacts with a weak resonant propagating field such that the scattered and the incident fields interfere destructively, giving rise to extinction of the forward propagating field. In early experiments on atoms and molecules demonstrating this effect, the extinction did not exceed 12% [6, 7] due to the spatial mode mismatch between the incident and scattered field of the single atom in three-dimensional space. By confining the propagating fields in a one-dimensional open transmission line and using artificial atoms based on superconducting circuits, extinctions well above 90% [8, 9] were demonstrated using flux qubits, and above 99% extinction was achieved [10] with transmon qubits [11]. It was also shown that the scattered and forward propagating fields could be controlled in time using fast microwave pulses to Autler–Townes split the energy levels of the artificial atom and in that way tune the artificial atom out of resonance with the propagating photons. This was used to create a single-photon router with a maximum on-off ratio of 99% and 10 ns operation time [10].

The fast speed of propagating photons in quantum optics experiments can be a limiting factor for some application such as in-flight manipulation. Surface acoustic waves (SAWs), on the other hand, offer clear advantages in this respect due to their much slower propagation speed. In this paper, we propose and demonstrate in-flight manipulation of SAWs at the single-phonon level, where the manipulation is done using a superconducting transmon qubit coupled to SAWs.

A number of experiments with SAWs in the quantum regime have been performed. For instance, phonon assisted tunneling of SAW-irradiated quantum dots has been demonstrated [12, 13], and on-chip transport of electrons propelled by SAWs has been shown [14–16]. The interaction between SAWs and a superconducting qubit at the quantum level was suggested [17] and shown [18] by Gustafsson *et al.* This was achieved by placing a transmon qubit on a piezoelectric substrate and interfacing it with a SAW transducer. In later experiments, SAW

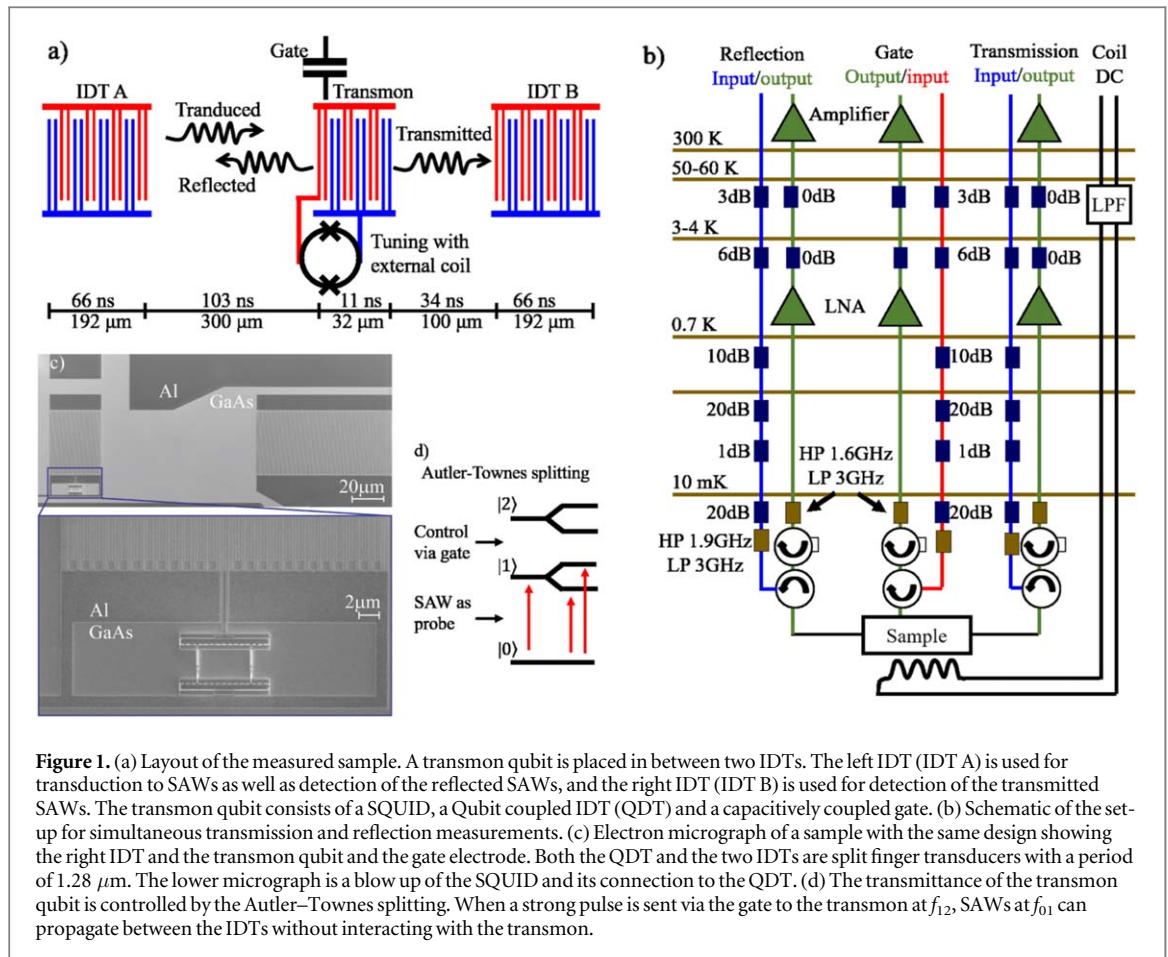


Figure 1. (a) Layout of the measured sample. A transmon qubit is placed in between two IDTs. The left IDT (IDT A) is used for transduction to SAWs as well as detection of the reflected SAWs, and the right IDT (IDT B) is used for detection of the transmitted SAWs. The transmon qubit consists of a SQUID, a Qubit coupled IDT (QDT) and a capacitively coupled gate. (b) Schematic of the set-up for simultaneous transmission and reflection measurements. (c) Electron micrograph of a sample with the same design showing the right IDT and the transmon qubit and the gate electrode. Both the QDT and the two IDTs are split finger transducers with a period of $1.28 \mu\text{m}$. The lower micrograph is a blow up of the SQUID and its connection to the QDT. (d) The transmittance of the transmon qubit is controlled by the Autler–Townes splitting. When a strong pulse is sent via the gate to the transmon at f_{12} , SAWs at f_{01} can propagate between the IDTs without interacting with the transmon.

resonators coupled to superconducting qubits have been demonstrated and strong coupling has been shown [19–22]. Furthermore, bulk acoustic waves have been used to study atom–phonon interaction [23]. SAWs might also provide a solution to connect distant qubits, acting as a quantum bus in quantum computers [24]. These acoustic systems open up for new possibilities to reach interesting regimes that are not feasible with other systems, due to the slow speed of the SAWs and the possibility for strong coupling to artificial atoms. For instance, the concept of giant artificial atoms leads to new physics and non-Markovian effects [25–29].

SAWs are mechanical waves that can propagate along the surface of any solid. They can be converted to and from electric microwave signals using interdigital transducers (IDTs) [30] on piezoelectric substrates. In this work we have chosen gallium arsenide (GaAs) as the substrate. The IDT is an array of electrodes with alternating polarity, and when an ac-voltage is applied across the IDT, SAWs are generated traveling in both directions from the IDT. The spacing of the electrodes sets the center frequency of the IDT (f_I) and the number of unit cells ($N_{p,I}$) determines the bandwidth by $BW_I = 0.9f_I/N_{p,I}$.

An artificial atom interacting with SAWs can be designed using an IDT as a shunt capacitance for a superconducting quantum interference device (SQUID) to form a transmon qubit [11]. This IDT will be referred to as the QDT (Qubit coupled IDT). Around the center frequency of the QDT, f_Q , the transmon couples to SAWs with a coupling strength $\Gamma_{ac} = 0.5f_Q K^2 N_{p,Q}$, where K^2 is the electromechanical coupling coefficient set by the substrate material and $N_{p,Q}$ is the number of unit cells in the QDT [18, 31].

2. Methods

Our device consists of a transmon qubit, with a QDT as the shunting capacitance, positioned asymmetrically between two IDTs, see figures 1(a), (c). The QDT as well as the IDTs are designed to couple to SAWs at 2.26 GHz. The IDTs act as transducers converting microwave signals between the electromagnetic and acoustic domains. To reduce internal mechanical reflections both the IDTs and the QDT have split electrodes, where one period (unit cell) consists of two electrodes connected to the top bus bar and two to the bottom bus bar (figures 1(a), (c)) [32–34]. Pertinent parameters are shown in table 1.

An optimized IDT should be impedance matched to 50Ω , which can be achieved by varying the electrode overlap W and $N_{p,I}$ [33, 34]. However, impedance matching on GaAs requires a very large $N_{p,I}$ (approximately 450),

Table 1. Table of material parameters, design and measured/extracted values for the measured sample. The dielectric constant, ϵ_∞ , the sound velocity, v_0 , and electromechanical coupling constant, K^2 are given by the material which is GaAs. The parameters that are set by design are: IDT A to transmon distance, $d_{Q,A}$, IDT B to transmon distance, $d_{Q,B}$, number of finger pairs of the IDT, $N_{p,I}$, and the QDT, $N_{p,Q}$, bandwidth of the IDT, BW_I , and the QDT, BW_Q , finger overlap (IDT/QDT width), W , and SQUID area A_{SQ} . The measured or extracted parameters are, maximum transmon frequency, $f_{01,max}$, IDT/QDT frequency, $f_{I/Q}$, Josephson coupling energy at zero flux $E_{J,0}$, Charging energy, E_C , E_J/E_C ratio, acoustic coupling, Γ_{ac} , and SAW wavelength, λ_0 .

Parameter	Material			Design							Measured							
	ϵ_∞	v_0	K^2	$d_{Q,A}$	$d_{Q,B}$	$N_{p,I}$	$N_{p,Q}$	BW_I	BW_Q	W	A_{SQ}	$f_{01,max}$	$f_I = f_Q$	$E_{J,0}$	E_C	E_J/E_C	Γ_{ac}	λ_0
Value	12.0	2864	0.07	300	100	150	25	14	81	40	16.5	3.19	2.264	10.7	129	83	21	1265
Unit		$m\ s^{-1}$	%	μm	μm			MHz	MHz	μm	μm^2	GHz	GHz	GHz	MHz		MHz	nm

and would result in a very small bandwidth of the IDTs. As a compromise, we have used $N_{p,I} = 150$ to get a sufficient bandwidth of 14 MHz, while achieving a reasonably good conversion efficiency. In principle it would be possible to add an impedance matching network to improve the conversion [33, 34], but this not been done here. To obtain the IDT/QDT center frequency, the electrodes have an equal spacing and width of $\lambda/8 = 158$ nm. The electrode structure was made using electron beam lithography and a liftoff process with 27 nm thick aluminum capped by 3 nm of palladium. The transducers were connected to ground planes (5/85/10 nm of Ti/Au/Pd) and the SQUID was deposited last using two-angle evaporation of 40/60 nm aluminum at $\pm 23^\circ$.

The acoustic transmission of the transmon qubit could be controlled in two different ways, which both operate by changing the energy level structure of the transmon such that the frequency of the 0–1 transition, f_{01} , is detuned with respect to the QDT frequency f_Q . The detuning is defined as $f_{01} - f_Q$ and the maximum transition frequency of the transmon is $f_{01,max} \approx (\sqrt{8E_J E_C} - E_C)/h \approx 3.19$ GHz [11]. (i) Using the magnetic flux from an external magnetic coil, the energy levels of the transmon can be tuned over a wide range, this tuning is relatively slow. (ii) The transmon can be driven by applying a microwave tone to the gate electrode and in particular the energy levels can be Rabi dressed creating an Autler–Townes splitting, see figure 1(d). The detuning achieved in this way is limited, but sufficiently large to detune the transmon from the SAW frequency. This type of control can also be very fast.

The device was measured using the set-up shown in figure 1(b). When the SAWs are generated by IDT A, the SAWs propagate with the amplitude ϕ_R^+ towards the transmon. At the transmon the SAWs are reflected (ϕ_L^-) back towards IDT A or transmitted (ϕ_R^-) towards IDT B, where the reflected and transmitted SAWs are measured simultaneously. Here, the indices L/R refer to left and right respectively. The reflection coefficient of the transmon is then given by $r = \phi_L^-/\phi_L^+$ and the transmission coefficient by $t = \phi_R^-/\phi_L^+$. The coefficients t and r are related by $t = r + 1$.

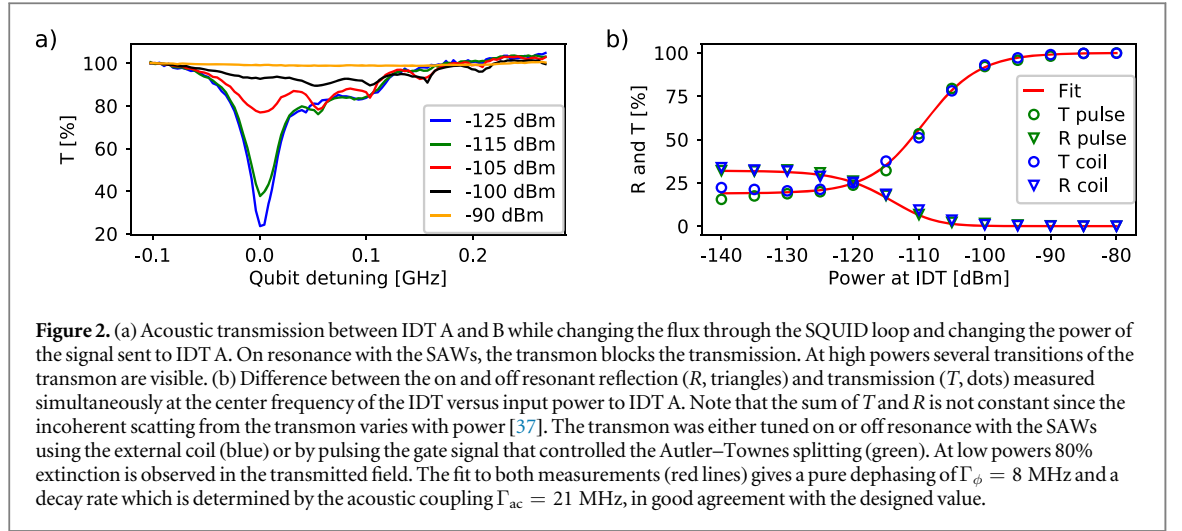
The experiment is operated at a temperature of 12 mK in order to be in the quantum limit, $k_B T \ll \hbar\omega$. In transmission, a continuous signal was sent to IDT A where it was partly electrically reflected due to impedance mismatch and partly transduced into SAWs in both directions and the right propagating waves were measured at IDT B. The measured signal in the frequency domain has been Fourier-transformed into the time domain, where the different parts of the signal could be distinguished due to the slow speed of the SAWs and the sufficient distances between the IDTs and the transmon [35, 36]. For instance in the reflection measurements, the signal reflected from the transmon is separated from the purely electric reflection due to impedance mismatch and from triple transits by about 200 ns (two times the distance between IDT A and the transmon). The reflection data was inversely Fourier-transformed back to the frequency domain, while other parts of the reflection signal were filtered out.

3. Results

We have measured the acoustic scattering of the transmon for different SAW power while tuning the transmon frequency (see figure 2). The transmittance is given by $T = |t|^2$, similarly the reflectance is given by $R = |r|^2$.

3.1. Controlling SAW propagation with magnetic flux

We start by controlling the transmon with an external magnetic flux from a coil (figure 2(a)). SAWs are launched from IDT A and the transmitted SAWs are measured using IDT B. When the transmon is tuned out of resonance with the frequency of the SAWs, f_f , the SAWs are transmitted without interacting with the transmon. On resonance, the SAWs interact with the transmon and are reflected back towards IDT A [18, 25]. This results in a reduction of the transmission and can be seen as a dip in transmission at zero detuning. As the SAW power is increased the qubit is gradually saturated [18] and the transmittance approaches unity. The scattering process is similar to the scattering process of artificial atoms in waveguide QED [2], although here the propagating SAW



field is scattered instead of an electromagnetic field. At small positive detuning and increasing power to IDT A, higher energy transitions corresponding to $f_{02}/2$ and $f_{03}/3$ can be observed. These features are in good agreement with the estimated anharmonicity of $f_{12} - f_{01} = -129$ MHz.

How the transmittance depends on SAW power is shown in figure 2(b), the transmittance (blue dots) and reflectance (blue triangles) at zero detuning were measured simultaneously. We see that the transmittance increases with increasing SAW power whereas the reflectance decreases. The rate at which the transmon reflects the incoming SAW phonons is limited by the coupling strength since the transmon can only scatter one phonon at a time [37]. The decreasing reflectance for increasing power is evidence for the two-level nature of the qubit [18]. For high power the transmon gets fully saturated, consequently the reflectance goes to zero and the transmittance goes to unity.

When the 0–1 transition frequency of the transmon is on resonance with the frequency of the QDT, i.e. at zero detuning, the reflection coefficient is given by [8]

$$r = -\frac{r_0}{1 + \Omega_p^2/\Gamma_{01}\gamma_{01}}. \quad (1)$$

Here $r_0 = 1/(1 + 2\Gamma_\phi/\Gamma_{01})$ is the maximum reflection amplitude, $\Gamma_{01} \approx \Gamma_{ac}$ is the relaxation rate from $|1\rangle$ to $|0\rangle$ of the transmon, $\gamma_{01} = \Gamma_{01}/2 + \Gamma_\phi$ is the 0–1 decoherence rate, Γ_ϕ is the 0–1 pure dephasing rate and Ω_p is the Rabi frequency at which the coherent incoming SAWs drive coherent oscillations of the transmon. The Rabi frequency is proportional to the amplitude of the SAW field, $\Omega_p = k\sqrt{P}$, where P is the incoming SAW power.

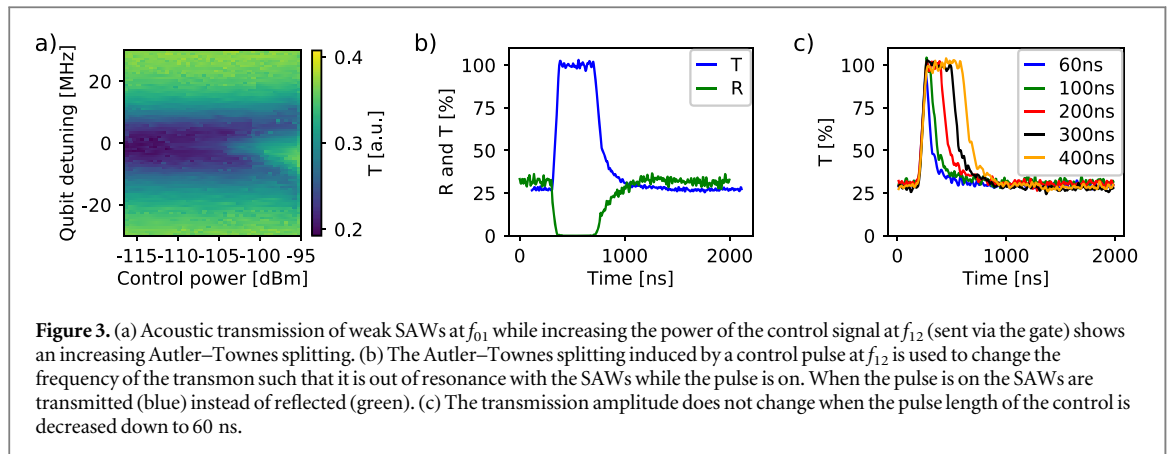
On resonance, the incoming SAWs interfere destructively with the field scattered by the transmon in the forward direction. This should result in perfect reflection and zero transmission on resonance, in the absence of pure dephasing and if the power of the incoming SAWs is low ($\Omega_p \ll \Gamma_{01}, \gamma_{01}$) [38, 39]. From figure 2(b) it is clear that the pure dephasing is not negligible in this device.

In figure 2(b) the measured transmission has been normalized and fitted to the transmittance as a function of P using k and Γ_ϕ as the only fit parameters. This fit is in good agreement with an acoustic coupling of 21 MHz, where $\Gamma_{01} = \Gamma_{ac}$. The transmittance is normalized to the average value when the transmon is detuned and hence not interacting with the propagating SAWs, i.e. 100% transmission when the transmon is detuned. The reflectance is known to be more difficult to normalize. We remove the background by subtracting the average measured reflection when the transmon is detuned. Using k and Γ_ϕ extracted from the fit to the transmittance curve, we then fit the reflectance data using the y -axis scale factor as a free fitting parameter. At low powers the deviation from zero in transmission and from 100% in reflection is due to a pure dephasing $\Gamma_\phi \approx 8$ MHz. The pure dephasing limits the extinction in transmission at low SAW powers to 80%.

The β -factor describes the ratio of the wanted coupling to the total coupling, and in our case the intentional acoustic coupling is quite large, approximately 21 MHz. The non-radiative decay is known to be small, in fact it is too small to be accurately determined. This means that our β -factor is close to 100%.

3.2. Controlling SAW propagation with the Autler–Townes splitting

Hitherto the 0–1 transition frequency of the transmon has been tuned with an external coil, but it can also be changed based on Autler–Townes splitting as shown in figure 1(d) [10, 40]. The levels $|1\rangle$ and $|2\rangle$ are dressed by the control field, causing an Autler–Townes splitting of the 0–1 transition. Using two-tone spectroscopy, we apply a weak continuous SAW signal via IDT A at f_{01} as a probe. At the same time, we apply a control signal via



the capacitively coupled gate (see figure 1) at the 1–2 transition frequency, f_{12} , and measure both reflection (IDT A) and transmission (IDT B) at f_{01} . For no or weak control powers, the SAWs are partly reflected, and we observe 80% extinction as described above and shown in figure 2(b). However, for substantial control powers the energy levels $|1\rangle$ and $|2\rangle$ Autler–Townes split [9]. This results in two transition frequencies different from f_{01} , i.e. the transmon is no longer on resonance with the frequency of the SAWs and the SAWs are transmitted instead of being reflected. The Autler–Townes splitting can be seen in figure 3(a), where the transmission between IDT A and IDT B is plotted versus transmon detuning.

As a control experiment we again probe the reflected and transmitted fields versus power to IDT A, but now use the Autler–Townes splitting to change the transmon in or out of resonance with the SAWs. The measured reflectance (green triangles in figure 2(b)) and transmittance (green dots) was fitted to (1). This gave very similar results as the measurements performed using the external coil. In figure 2(b) the fit shown (red lines) is the combined fit to both measurements.

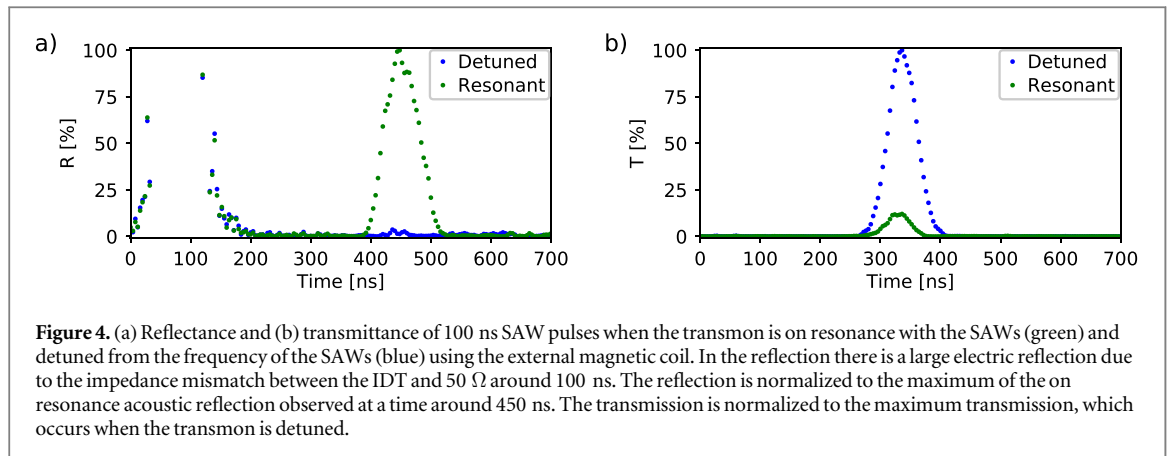
3.3. Fast control of the SAW propagation

The control of SAW propagation can be exploited to create a phonon router in the quantum regime, similar to the photon router that was demonstrated in [10]. In principle either flux control or Autler–Townes control could be used. Here we show a proof of principle of this concept using the Autler–Townes control since it allows fast changes of the transmittance.

Initially the frequency of the transmon, f_{01} , is tuned to be on resonance with the SAWs. A strong control signal is then applied as a pulse to the transmon gate (see figure 1(d)). When the pulse is OFF, the SAWs are partly reflected by the transmon and when it is ON, the SAWs are transmitted. This is shown in figure 3(b) for reflection (green) and transmission (blue) versus time when a 400 ns pulse is applied as the control. The rise time of the router is about 40 ns, limited by the bandwidth of the IDT, while the fall time of the router is 160 ns. The longer fall time is due to multiple transits between the transmon and IDT A in reflection, and between the transmon and IDT B in transmission. These multiple transits occur because the IDTs are not converting all SAW power to electric power, which is measured, but the SAWs are partly reflected back towards the transmon. The transmon reflects the SAWs and each time the SAWs reach the IDTs they are partly converted to electric signal and measured. When the control pulse is turned OFF, these multiple transits appear as the long fall time, since they are delayed by the larger traveling distance. Routing using shorter control pulses is shown in figure 3(c), where the amplitude of the transmitted SAW field is the same down to 60 ns control pulses. Detection of shorter control pulses is limited by the bandwidth of the IDTs.

3.4. Manipulating SAW pulses

For more advanced in-flight manipulation of SAWs, it will be important to not only route continuous SAWs but also route SAW pulses. The possibility to do this with our device is shown in figure 4, where a 100 ns SAW pulse generated at IDT A is routed using the external coil to flux tune the transmon in and out of resonance with the SAWs. When the transmon is out of resonance with the SAWs (blue), the SAW pulse is transmitted without interacting with the transmon. On resonance (green), the SAW pulse is mostly reflected but part of it is also transmitted even at low powers of the SAW pulse. This is due to incoherent scattering, which in turn is due to the pure dephasing as mentioned previously. In this measurement, imperfect reflection is due to pure dephasing, but even without pure dephasing the reflection would be limited by the relaxation rate of the transmon in comparison to the length of the SAW pulse. The pulse length has to be longer than the relaxation time in order to reach full reflection, which will be important to consider for future experiments.



4. Discussion and conclusion

Here we have shown that routing SAWs at the phonon level is feasible. The performance of the phonon router presented here is limited by the pure dephasing which in turn limits the maximum reflection from the transmon. We have also shown that the routing can be done very fast, on the 100 ns timescale. In comparison to the photon router in [10], the phonon router presented here has a four times longer rise time and the pulse length is limited to six times longer due to the narrow bandwidth of the IDTs. This proof of principle demonstration is promising for further in-flight manipulation of propagating single phonons.

An interesting development of the phonon router presented here would be to modify the device to include two transmons between the two IDTs, where the transition frequencies of the two transmons can be tuned individually either with separate capacitively coupled gates or flux lines. If the first transmon is tuned out of resonance and the second transmon on resonance with the frequency of the SAWs, a SAW pulse generated at IDT A can propagate through the first transmon and be reflected at the second transmon. Since it takes a substantial time for the SAWs to propagate, there is ample time to tune the first transmon on resonance with the SAWs and in this way trap the SAW pulse between the two transmons. If the transmons have low pure dephasing, the SAW pulse should be able to travel back and forth without too much dissipation since SAWs propagate the substrate with low propagation losses [31, 36]. The trapped SAW pulse can then be released controllably to the left or to the right by either tuning the first transmon or the second transmon out of resonance with the SAWs.

In principle, a phonon router could also be based on tunable resonators, such resonators should then have low dissipation and dephasing. This could be done for instance by coupling a tunable superconducting resonator to the SAW transmission line. The tunability can be implemented by shorting one end of the resonator to ground via a SQUID [41]. This would increase the dynamic range of the device. We note that in practice it is very hard to implement tunability without also introducing a nonlinearity. The qubit implements both large tunability and large nonlinearity.

Moreover, the integration of qubits into SAW circuits allows a number of other interesting possibilities for future experiments, like emission of single phonons, saturable mirrors etc. Future devices including both qubits and tunable resonator (saturable and normal mirrors) may provide increased functionality in terms of creating and modifying non-classical SAW-phonon states.

In conclusion, we have demonstrated that a superconducting transmon qubit, designed to interact with SAWs, can be used to route propagating phonons. On resonance with the incident SAWs and at low powers, the transmon reflects the SAW field and an extinction of 80% was observed in transmission. Using Autler–Townes splitting of the transmon’s transition frequency the reflection and transmission of the SAW field could also be controlled in time and the propagating phonons could be routed with a rise time of 40 ns. Moreover, we showed that it is possible to route short (100 ns) pulses, which further enables experiments where an acoustic pulse is captured between two transmons and released in a controlled way. In such experiments it is beneficial to use SAW phonons since they have a five orders of magnitude slower speed than photons in vacuum allowing for more time to perform in-flight manipulations of the propagating phonons.

Acknowledgments

We wish to acknowledge financial support from The Knut and Alice Wallenberg Foundation and The Swedish Research Council. The samples were made at the Nanofabrication Laboratory at Chalmers University of

Technology. We thank Marcus Rommel for assistance imaging the sample and we acknowledge fruitful discussions with Sankar Sathyamoorthy, Martin Gustafsson and Anton Frisk-Kockum.

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