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Letter

# Phonon-Assisted Photoluminescence from Indirect Excitons in Monolayers of Transition-Metal Dichalcogenides

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**KEYWORDS:** dark excitons, photoluminescence, transition-metal dichalcogenides, exciton—phonon interaction, phonon side bands, microscopic model

he cryogenic photoluminescence (PL) spectrum of twodimensional (2D) semiconductors provides a powerful tool to study intriguing quantum phenomena invisible at room temperature or in linear optical experiments. The large variety of low-temperature emission features at energies below the bright exciton resonance indicates the existence of bound exciton configurations, such as trions, biexcitons,<sup>1-6</sup> and trapped excitons,<sup>7,8</sup> but could also result from the indirect recombination of momentum-dark exciton states.<sup>9-16</sup> The radiative decay of a momentum indirect electron-hole pair requires the simultaneous interaction with a phonon to fulfill the momentum conservation and is therefore very inefficient compared to the direct recombination of an exciton with zero center-of-mass momentum. However, in indirect semiconductors, where the momentum indirect exciton is located below the bright state, the low-temperature emission can exhibit strong phonon-assisted signals due to a large population of momentum-dark states, as depicted in Figure 1. Recently, the PL spectrum of hexagonal boron nitride has been shown to be dominated by phonon-assisted processes<sup>17,18</sup> resulting from an indirect band gap. Several theoretical and experimental studies have demonstrated that in tungsten-based monolayer materials, intervalley excitons are located below the optically bright exciton, 15,19-24 and recent experimental PL studies on hBNencapsulated tungsten diselenide have revealed a multitude of

low-temperature emission peaks whose microscopic origin still needs to be clarified.  $^{3-5,9}$ 

While the radiative decay of bright excitons has been extensively studied,<sup>25-30</sup> phonon-assisted exciton recombination has remained widely unexplored in the technologically promising field of TMD monolayers. In particular, a microscopic treatment of the large number of possible decay channels and the complex interplay between phonon-induced dephasing and recombination is challenging. In previous studies, restricted cases, such as optical phonon replicas of bright excitons, have been theoretically investigated within the polaron-frame<sup>31,32</sup> and nonmarkovian treatments of the density matrix.<sup>33,34</sup> However, there is so far no general theoretical framework for the phonon-assisted exciton recombination including optical and acoustic phonons as well as intra- and intervalley recombination channels on a microscopic footing.

Here, we present a fully microscopic model and lowtemperature PL experiments demonstrating the emergence of pronounced phonon-assisted signals from momentum dark

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**Figure 1.** Sketch of direct and indirect decay channels for excitons showing the underlying scattering processes in the excitonic center-of-mass dispersion (right) and the corresponding PL signals (left). Momentum-dark excitons can decay by emitting or absorbing a phonon (blue arrow) and subsequently emitting a photon, which contributes to the indirect PL signal (red arrow).

excitons. Based on the fundamental equations-of-motion of the many-particle density matrix, we find an analytical formula which allows us to calculate temperature-dependent PL spectra. We apply the derived formula to calculate the luminescence spectrum of hBN-encapsulated TMD monolayers. For tungsten diselenide (WSe<sub>2</sub>), our calculations predict clearly visible low-temperature emission features between 50 and 80 meV below the bright exciton, in good agreement with experimental observations. We identify these signals as phonon-assisted recombinations of momentum-dark K-K' excitons. These peaks have been observed in several independent experiments, while their microscopic origin has not been clarified yet.<sup>3,9,35</sup> In contrast, for molybdenum diselenide (MoSe<sub>2</sub>), we find no additional peaks and an opposite asymmetric broadening of the bright exciton resonance compared to WSe2, which can be explained by the absence of lower lying momentum-dark excitons. Overall, our work provides new insights into phonon-assisted exciton luminescence and can be applied to determine emission spectra of arbitrary semiconducting materials, in particular including van der Waals stacked multilayers.

Microscopic Model. The central property determining the PL of a semiconductor is the electronic bandstructure in vicinity of the band gap. Therefore, we focus on the local band extrema, which in TMDs are located at the K, K', and  $\Lambda$  point of the hexagonal Brillouin zone, cf. Figure 2a. Due to the strong Coulomb interaction in 2D materials, electrons and holes are tightly bound into excitons. Thereby, TMDs can host momentum direct intravalley excitons (K-K) as well as intervalley excitons, such as K-K', where electrons and holes are located at the K' and K point, respectively. The latter are optically dark, since the required momentum transfer cannot be provided by a photon. As a result of the peculiar ordering of spin-polarized electronic bands in tungsten-based TMDs,<sup>36</sup> the momentum-dark intervalley K-K' excitons lies below the bright K-K excitons, cf. Figure 2b. When taking into account excitonic effects, the K– $\Lambda$  excitons are also shifted below the bright K-K exciton due to the significantly larger mass of the  $\Lambda$  valley.

To set up a realistic model, we used ab initio input parameters for the electronic bandstructure, phonon dis-



**Figure 2.** Schematic illustration of the (a) electronic and (b) corresponding excitonic dispersion around high-symmetry points in tungsten-based TMDs. While transitions involving electronic bands with the same spin are dipole allowed (red), the spin-dark excitons (pink dashed) require spin-flip processes. The specific spin-orbit coupling in tungsten-based TMDs renders the K–K' as the lowest-lying spin-allowed exciton, in agreement with a recent ab initio calculation.<sup>24</sup>

persion, dielectric constants, and electron-phonon coupling elements.<sup>36–38</sup> The excitonic properties are derived in effective mass approximation by solving the Wannier equation.<sup>39</sup> In the following, we focus on the exemplary monolayers of tungsten diselenide (WSe<sub>2</sub>). Moreover, we only consider spin-like exciton states, since their formation and recombination does not require spin-flip processes. The possible impact of spinunlike K-K excitons is discussed later in the text. In Table 1, we have summarized all relevant exciton energies obtained from our Wannier model for different substrates as well as phonon energies in WSe2 taken from ref 37. The phonon energies are in good agreement with experimental Raman measurements.<sup>40,41</sup> The calculated exciton binding energies and spectral exciton separations agree well with values found in literature using similar Wannier models,<sup>42,43</sup> ab initio studies,<sup>24,44</sup> and experiments.<sup>45</sup> In the following, we focus on hBN encapsulated samples, which have been shown to be less affected by undesirable external disorder effects.<sup>46,47</sup> The exact position of the K– $\Lambda$  state relative to the bright exciton can be externally tuned via substrate-induced screening or strain.<sup>23,24,48</sup> In contrast, the valley-inverted spin-orbit coupling makes sure that the K-K' exciton in tungsten-based TMDs is

Table 1. Relevant Exciton Binding Energy  $E_{\text{bind}}$ , Spectral Exciton Separation  $\Delta_{K-\Lambda}$ ,  $\Delta_{K-K'}$  (with Respect to the Bright K–K State), and Phonon Energies in WSe<sub>2</sub><sup>*a*</sup>

exciton energies WSe <sub>2</sub> (meV)			
	hBN enc. ( $\varepsilon_r = 4.5$ )		vacuum ( $\varepsilon_r = 1$ )
$E_{\text{bind}}(K - K\uparrow\uparrow)$	$168 (172)^{45}$		465 (450, <sup>42</sup> , 480) <sup>44</sup>
$\Delta_{K-\Lambda}$	-34		$-54 (-60)^{24}$
$\Delta_{K-K'}$	-46		$-57 (-60)^{24}$
phonon energies WSe <sub>2</sub> (meV)			
from ref <sup>37</sup>	Г	Λ	К
TA/LA	0	11.6/14.3	15.6/18
TO/LO	30.5/30.8	27.3/32.5	26.7/31.5
A1	30.8	30.4	31

<sup>a</sup>Throughout this work, we consider hBN encapsulated samples. The free-standing results are given for direct comparison with literature values given in brackets. Phonon energies are taken from ref 37.

always below the bright state independently of the used substrate.

After optical excitation and a quick thermalization process, excitons distribute across all valleys to form a Boltzman-like distribution in energy. Therefore, the energetically lowest momentum-dark states have, in particular at low temperatures, a much higher occupation then the bright exciton, so that in principle, PL signatures stemming from the indirect (phononassisted) recombination of dark excitons might become visible. In order to predict intensities and line shapes of the indirect PL signals, a sophisticated model of the mixed exciton-photonphonon interactions is needed. Previous studies on PL phonon-side bands have used perturbative approaches or were restricted to specific phonon modes and intravalley processes. Here, we develop a more universal approach including acoustic and optical modes, intra- and intervalley scattering, all temperature ranges, and a self-consistent description of phonon-induced broadening and recombination.

We derive the PL signal from the many-particle density matrix of an interacting system of electrons, phonons and photons. Throughout this work, we assume an excitation density far away from the exciton-Mott transition and model excitons as a gas of non-interacting bosons. In this regime, the many-particle physics of an undoped monolayer can be described by the excitonic Hamiltonian,<sup>33,49–51</sup> which in the rotating frame<sup>52</sup> reads

$$H = \sum_{\mu \mathbf{Q}_{\parallel}} E_{\mathbf{Q}_{\parallel}}^{\mu} a_{\mu}^{\dagger} a_{\mu} \mathbf{Q}_{\parallel} + \sum_{\alpha \mathbf{q}_{\parallel}} \Omega_{\mathbf{q}_{\parallel}}^{\alpha} b_{\alpha \mathbf{q}_{\parallel}}^{\dagger} b_{\alpha \mathbf{q}_{\parallel}}$$
$$+ \sum_{\sigma \mathbf{k}} \omega_{\mathbf{k}}^{\sigma} c_{\sigma \mathbf{k}}^{\dagger} c_{\sigma \mathbf{k}} + \sum_{\mu \sigma \mathbf{k}} \left( M_{\sigma \mathbf{k}}^{\mu} c_{\sigma \mathbf{k}}^{\dagger} a_{\mu \mathbf{k}_{\parallel}} + M_{\sigma \mathbf{k}}^{\mu *} a_{\mu \mathbf{k}_{\parallel}}^{\dagger} c_{\sigma \mathbf{k}} \right)$$
$$+ \sum_{\nu \mu \mathbf{Q}_{\parallel} \alpha \mathbf{q}_{\parallel}} D_{\alpha \mathbf{q}_{\parallel}}^{\nu \mu} a_{\nu}^{\dagger} a_{\mu} a_{\mu} (b_{\alpha \mathbf{q}_{\parallel}} + b_{\alpha,-\mathbf{q}_{\parallel}}^{\dagger})$$
(1)

where  $\mathbf{k}_{\parallel}$  denotes the component of the momentum  $\mathbf{k}$  parallel to the monolayer plane. We use annihilation (creation) operators  $a_{\mu \mathbf{Q}_{\parallel}}^{(\dagger)}$ ,  $b_{\alpha \mathbf{q}_{\parallel}}^{(\dagger)}$  and  $c_{\sigma \mathbf{k}}^{(\dagger)}$  for excitons in the state  $\mu$ , phonons in the mode  $\alpha$ , and photons with the polarization  $\sigma$ , respectively. Moreover, the corresponding dispersions for the three particle species are given by  $E_{\mathbf{Q}_{\parallel}}^{\mu}, \Omega_{\mathbf{q}_{\parallel}}^{\alpha}$  and  $\omega_{\mathbf{k}}^{\sigma}$ . Here, the excitonic bandstructure  $E^{\,\mu}_{{f Q}_{\parallel}}$  is decomposed into valleys around energetic extrema, cf. Figure 2, where excitons can be described as free particles with effective valley masses. The exciton index  $\mu$  acts as a compound index containing main, angular, spin, and valley quantum numbers. The second line of eq 1 describes the conversion of excitons to photons and vice versa under conservation of the in-plane momentum, whose probability is determined by the exciton-photon matrix element  $M^{\mu}_{\sigma \mathbf{k}}$ . Finally, excitons can scatter from the state ( $\mu$ ,  $\mathbf{Q}_{\parallel}$ ) to  $(\nu, \mathbf{Q}_{\parallel} + \mathbf{q}_{\parallel})$  by emitting or absorbing a phonon, guided by the exciton-phonon matrix element  $D_{\alpha \mathbf{q}_{\parallel}}^{\nu \mu}$ . Details about the calculation of these matrix elements are given in previous works  $^{15,53,54}$  and can also be found in the Supporting Information.

In this framework, the PL can be determined from the temporal change of the photon density  $n_{\mathbf{k}} = \langle c_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} \rangle^{55}$  Applying the Heisenberg equation of motion, we find coupled differential equations for the photon density, the polarization  $S_{\mathbf{k}}^{\mu} = \langle c_{\mathbf{k}}^{\dagger} a_{\mu \mathbf{k}_{\mathbf{k}}} \rangle$ , the phonon-assisted polarization

 $\mathcal{U}_{\mathbf{kq}}^{\boldsymbol{\mu},\pm} = \langle c_{\mathbf{k}}^{\dagger} b_{\mp \mathbf{q}}^{(\dagger)} a_{\boldsymbol{\mu} \mathbf{k}_{\parallel} - \mathbf{q}} \rangle \text{ and further higher-order correlations.}$ We factorize appearing many-particle expectation values according to the cluster expansion scheme.<sup>56</sup> Here, we disregard contributions connected to multiphonon emission/ absorption. However, we include correlations giving rise to the phonon-induced dephasing  $\Gamma_{\mathbf{Q}}^{\mu} = \pi \sum_{\nu \mathbf{q},\pm} |D_{\mathbf{q}}^{\mu\nu}|^2 \eta_{\mathbf{q}}^{\pm} \delta(E_{\mathbf{Q}}^{\mu} \pm \Omega_{\mathbf{q}} - E_{\mathbf{Q}+\mathbf{q}}^{\nu})$  as well as the radiative dephasing for exciton states within the light cone  $\gamma_{\mathbf{k}_{\parallel}}^{\mu} = \pi \sum_{\mathbf{k}'} |M_{\mathbf{k}'}^{\mu}|^2 \delta_{\mathbf{k}_{\parallel}'\mathbf{k}_{\parallel}} \delta(E_{\mathbf{k}_{\parallel}}^{\mu} - \omega_{\mathbf{k}'})$ . A detailed study on these dephasing rates can be found in our previous studies.<sup>15,47</sup> It is of key importance to include these dephasing contributions in the truncation scheme. In particular, we find that phononassisted recombinations via virtual states close to the actual bright state are physically equivalent to a phonon-induced broadening of the bright state. Therefore, a phenomenological inclusion of dephasing rates can give rise to nonphysical negative luminescence signals. A detailed derivation and discussion is provided in the Supporting Information. Finally, we find the following analytic expression for the  $\sigma$ -polarized photon flux emitted in perpendicular direction with respect to the monolayer:

$$I_{\sigma}(E) = \frac{2}{\hbar} \sum_{\mu} \frac{|M_{\sigma}^{\mu}|^{2}}{(E_{0}^{\mu} - E)^{2} + (\gamma_{\sigma 0}^{\mu} + \Gamma_{0}^{\mu})^{2}} \\ \times \left( \gamma_{\sigma 0}^{\mu} N_{0}^{\mu} + \sum_{\nu q, \alpha \pm} |D_{\alpha q}^{\mu\nu}|^{2} N_{q}^{\nu} \eta_{\alpha q}^{\pm} \frac{\Gamma_{q}^{\nu}}{(E_{q}^{\nu} \pm \Omega_{q}^{\alpha} - E)^{2} + (\Gamma_{q}^{\nu})^{2}} \right)$$
(2)

where  $\eta_{\mathbf{q}}^{\pm} = 1/2 \mp 1/2 + \langle b_{\mathbf{q}}^{\dagger} b_{\mathbf{q}} \rangle$  denotes the relevant phonon occupation factor for absorption/emission, and  $N_{\mathbf{Q}}^{\mu} = \langle a_{\mu\mathbf{Q}}^{\dagger} a_{\mu\mathbf{Q}} \rangle$  represents the exciton occupation. The first term reflects the Lorentz-shaped response of the direct recombination of bright excitons, with a small difference that the phonon dephasing only appears in the denominator. However, for energies  $E \approx E_0$ , the second term containing the scattering contributions is proportional to the phonon-assisted in-scattering to the bright state, so that close to thermal equilibrium, the second term in the brackets becomes  $\Gamma_0^{\mu} N_0^{\mu}$ . Therefore, in the resonant case, eq 2 can be well approximated with the exciton Elliot formula:<sup>39</sup>

$$I_{\sigma}(E)_{E\approx E_{0}} = \frac{2}{\hbar} \sum_{\mu} \frac{|M_{\sigma}^{\mu|^{2}}(\gamma_{\sigma0}^{\mu} + \Gamma_{0}^{\mu})}{(E_{0}^{\mu} - E)^{2} + (\gamma_{\sigma0}^{\mu} + \Gamma_{0}^{\mu})^{2}} N_{0}^{\mu}$$
(3)

The second part of eq 2 containing phonon-assisted decay channels agrees with luminescence formulas derived in previous studies<sup>31,32</sup> for optical phonon replicas in the polaron picture. The advantage of our approach is that it consistently includes broadening and additional decay channels allowing to quantitatively compare line shapes and intensities of bright and dark states. The equation can be generally applied to other semiconducting systems as long as the band edge excitations are of excitonic nature. We have used general compound indices for the excitons allowing to include phonon-assisted transitions involving other exciton states as the ones studied in this work, such as phonon-mediated spin-flip transitions and layer-hybridized Moire excitons as well as localized/charge trapped excitons.

Note that the model does not account for exciton-exciton interaction or the presence of residual free charge carriers,

which can enable further bound many-particle states, such as biexcitons or trions. The latter gives rise to well studied low-temperature PL features<sup>1-5,57</sup> below the bright exciton.

**Results.** Now we apply the derived eq 2 together with the calculated exciton energies and wave functions to calculate the PL signal of the multivalley exciton landscape. Figure 3 shows calculated PL spectra for hBN-encapsulated monolayer WSe<sub>2</sub> at four different temperatures. In addition to the full spectra calculated from eq 2 (color shaded), we also present the spectra in the case of  $\Gamma_q^{\nu} \rightarrow 0$  (solid line). This corresponds to  $\delta$  functions in the brackets of eq 2, requiring strict energy conservation for the conversion from an exciton to a phonon and photon. The sharp steps in the solid line conveniently illustrate the multitude of exciton valleys and phonon modes contributing to the overall PL signal. Here, each step in the spectrum corresponds to a transition from the energetic minimum of a certain valley, while absorbing/emitting a phonon.

At 300 and 150 K, the PL spectrum is dominated by the bright exciton resonance, but already here, phonon-assisted indirect recombinations have a significant impact resulting in an asymmetric resonance. At energies larger than  $E_0$ , the signal is mainly shaped by recombinations of small momentum excitons in the K–K valley, which scatter to virtual states in the light cone via low-energy acoustic phonons. For energies smaller than  $E_0$ , a much larger broadening is observed. This can be ascribed to K–K excitons emitting optical phonons and, more importantly, to the indirect decay of momentum-dark



**Figure 3.** PL spectra of hBN-encapsulated WSe<sub>2</sub> monolayers at four different temperatures. Together with the full simulation (colored curves), we also show the solution for zero dark-state dephasing (thin solid lines). At higher temperatures, the lower-lying momentum-dark states K–K' and K– $\Lambda$  give rise to a strong asymmetric broadening of the bright exciton resonance toward lower energies. For low temperatures, the PL signal exhibits indirect peaks stemming from the phonon-assisted recombination of momentum-dark excitons.

intervalley excitons. Our Wannier model predicts that the  $K-\Lambda$  and K-K' excitons are located about 34 and 46 meV below the bright exciton, respectively. These momentum-dark states can perform indirect PL transitions as depicted in Figure 1, preferably to virtual states close to the bright exciton, yielding the asymmetric peak shape at room temperature.

At low temperatures, the optical response shifts toward multiple indirect PL peaks below the bright exciton stemming from the phonon-assisted recombination of the energetically lowest K-K' exciton. The observed temperature dependence is a result of a competition between oscillator strength and occupation probability. The phonon-assisted peaks become only visible at low temperatures because here the exciton distribution becomes very narrow in energy. Therefore, excitons are "forced" to take the unlikely indirect recombination pathway via a virtual state, since it is even more unlikely to occupy the energetically higher bright state. This temperature behavior is analogue to localized excitons, which only become visible for thermal energies smaller than the trapping energy.

The predicted low-temperature PL signals at about -60 meV (K–K', acoustic K phonon-assisted) and -75 meV (K– K', optical K phonon-assisted) correspond well to experimentally observed but so far not fully explained PL peaks in hBN-encapsulated samples tuned to charge neutrality. In agreement with our theory, these peaks are not visible in reflection/absorption spectra.<sup>58</sup> We have also performed calculations for tungsten disulfide (WS<sub>2</sub>) monolayers and find the same qualitative temperature trend. Here, the phononassisted peaks are located at about -70 and -90 meV (cf. Supporting Information), resulting from slightly different exciton and phonon dispersions.

In Figure 4 we directly compare an experimentally measured PL spectrum with our simulation. The blue shaded curve shows the PL measured at T = 15 K for hBN-encapsulated WSe<sub>2</sub> at charge neutrality. Details about the experiment can be found in ref 3. The red line shows the corresponding calculated spectrum. For a better comparison, the calculated spectrum in Figure 4 was convoluted with a 1 meV broad Gaussian to simulate disorder in the experiment, viz. small statistical fluctuations of resonance energies resulting from inhomogeneities throughout the sample. Figure 4 illustrates that the



**Figure 4.** Direct comparison between experiment and theory. The blue shaded curve shows the PL spectrum measured on hBN-encapsulated WSe<sub>2</sub> at charge neutrality at T = 15 K. The red line shows the corresponding simulated spectrum. Peaks P and Q denote the acoustic and optical phonon-assisted recombination of K–K' excitons.

When comparing peak intensities in theory and experiment we find quantitative differences in the height of the bright exciton X<sub>0</sub> and the phonon side peaks P and Q. This deviation could result from numerical inaccuracies in the excitonphonon matrix element, for example, resulting from the applied deformation potential approximation.<sup>37</sup> Moreover, the presence of the neglected defect-bound trions (T) and the spinforbidden exciton (D) could influence the oscillator strength and occupation of the bright state. In general, the complex interplay of optical pumping and phonon-induced relaxations as well as radiative and nonradiative recombination, which at low temperatures take place on comparable time scales, could result in quasi-equilibrium distributions in the experiment that deviate from the assumed Boltzmann distribution. However, we find a good qualitative agreement for the temperature dependence of peak shapes and intensity ratios. In the Supporting Information, we show further spectra measured on the same system at different temperatures. We find that the intensity of P and O relative to X<sub>0</sub> increases, while the slope on the high-energy side of the peak P becomes steeper with decreasing temperature. Both findings are consistent with our model, since both the intensity as well as the peak shape of the phonon-assisted emission are determined by the energetic distribution of excitons  $\propto \exp(-E/k_{\rm B}T)$ .

Moreover, we have summarized several independent PL measurements on hBN-encapsulated WSe2<sup>3-5</sup> in the Supporting Information. All of these studies show the phonon-assisted peaks discussed above. Interestingly, the strongest peak denoted as P in Figure 4 (attributed in our work to the acoustic phonon-assisted decay of K-K' excitons) shows a double peak structure in experiments performed at 4 K. The lower one of the two peaks (P2) splits in magnetic fields into two resonances with the same g-factor as the spin-dark D peak.<sup>60</sup> In contrast, the other peak (P1) shows a different behavior in magnetic fields, cf. Supporting Information. The studies in refs 60 and 61 suggest that P2 is most likely a phonon replica of the spin-dark exciton D, involving chiral E'' phonons for the necessary spin-flip. However, the origin of the second peak P1 has not been explained yet. Polarization resolved measurements show both peaks P1 and P2 in copolarized measurements, while the energetically higher P1 is much weaker in cross-polarized set-ups.<sup>4</sup> Both, the magnetic field dependence from ref 60 as well as the polarization dependent measurements in ref 4 support our assignment of P1 to the phonon-assisted recombination of K-K' spin-like excitons, cf. Supporting Information for further details.

Finally, we compare our results obtained for WSe<sub>2</sub> with molybdenum-based TMDs, cf. Figure 5. Here, we show a continuous temperature study of the PL spectrum for (a) WSe<sub>2</sub> and (b) MoSe<sub>2</sub>. In tungsten-based TMDs, the lower-lying  $K-\Lambda$  and K-K' valley provide a continuous density of (momentum-dark) states below the bright exciton, yielding an asymmetric broadening of the bright exciton peak toward lower energies. In contrast, for MoSe<sub>2</sub>, the bright state constitutes the global minimum of the exciton dispersion



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**Figure 5.** Temperature-dependent PL spectra calculated for (a)  $WSe_2$  and (b)  $MoSe_2$ . For each temperature, the spectra have been normalized to the integrated PL. While  $WSe_2$  shows a clearly asymmetric broadening toward lower energies and distinct indirect peaks at low temperatures,  $MoSe_2$  has no additional indirect peaks and is more strongly broadened toward higher energies.

calculated in our Wannier model. Therefore, there are no phonon-assisted PL peaks below the bright state, and the main peak is asymmetrically broadened toward higher energies, cf. Figure 5b. Here the broadening of the low energy side of the main line is predominantly given by the energy uncertainty of the bright state giving rise to a Lorentzian shape. In contrast, the high-energy side is additionally shaped by the decay of small momentum excitons in the K–K valley assisted by long-range acoustic phonons, which agrees with the findings in ref 34.

In summary, we have presented an analytical expression for the phonon-assisted exciton PL from momentum-dark excitons which allows to model the emission spectrum of an arbitrary semiconducting material. When applying our model to the luminescence of WSe<sub>2</sub>, we find a good agreement with experiment clear PL signals stemming from momentum-dark intervalley excitons, potentially explaining the origin of so far observed but unidentified PL peaks. In contrast, MoSe<sub>2</sub> does not exhibit indirect PL peaks and shows an opposite asymmetric broadening which is consistent with the absence of lower-lying momentum-dark exciton states. Our work will trigger future experimental and theoretical studies on momentum-dark exciton PL and in particular addressing exciton thermalization and diffusion.

#### ASSOCIATED CONTENT

#### **Supporting Information**

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.0c00633.

Derivation of the equations of motion, many-particle dephasing and PL formula; details on the calculation of excitonic energies, wave functions and matrix elements; summary of supporting PL spectra published in other works; time dependent PL of P1 and P2; temperature dependent PL spectra of WSe<sub>2</sub>; calculated energies and PL in WS<sub>2</sub> (PDF)

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#### Notes

The authors declare no competing financial interest.

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