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Intertwined magnetic sublattices in the double perovskite compound LaSrNiReO_6

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We report a muon spin rotation (μ^+ SR) study of the magnetic properties of the double perovskite compound LaSrNiReO_6 . Using the unique length and time scales of the μ^+ SR technique, we successfully clarify the magnetic ground state of LaSrNiReO_6 , which was previously deemed as a spin glass state. Instead, our μ^+ SR results point toward a long-range dynamically ordered ground state below $T_C = 23$ K, for which a static limit is foreseen at $T = 0$. Furthermore, between $23 \text{ K} < T \leq 300 \text{ K}$, three different magnetic phases are identified: a dense ($23 \text{ K} < T < 75 \text{ K}$), a dilute ($75 \text{ K} \leq T \leq 250 \text{ K}$), and a paramagnetic ($T > 250 \text{ K}$) state. Our results reveal how two separate yet intertwined magnetic lattices interact within the unique double perovskite structure and the importance of using complementary experimental techniques to obtain a complete understanding of the microscopic magnetic properties of complex materials.

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I. INTRODUCTION

Materials with perovskite crystal structure have for several decades been at the center of attention across a wide scientific scope [1,2]. These compounds exhibit many interesting physical properties, such as various magnetic orders [3] and/or electronic states—metallic [4,5], insulator [6], and superconductivity [7]. Moreover, some perovskites also display multiferroicity [8–11], which is an area that during recent years has received increasing attention due to both fundamental interests as well as applications in sensors, actuators, and memory devices [12].

The smörgåsbord of properties for the perovskites originates from its ABX_3 -type crystal structure, where A and B are cations and X an anion that bonds with B to form BX_6 octahedra. The significance of the perovskite structure is that

the octahedra are flexible and can contract/expand/distort to accommodate almost all elements in the periodic table [13]. A noteworthy and the most common subgroup of perovskites is the oxide perovskite, which is achieved for systems where the X anion is an oxygen ion.

Lately, a new type of perovskite has raised the interest of both experimental and theoretical physicists, the so-called double perovskite [14]. In this case, half of the B cations are substituted with another cation forming an $A_2BB'O_6$ structure. The B cation in these systems may order, where the most common pattern is a rocksalt type (like NaCl, but column or layered also exist), consisting of corner-shared BO_6 and $B'O_6$ octahedra [15,16]. The degrees of freedom for designing perovskite compounds has opened up a wide door from the application point of view. Lately, diverse combinations of compounds [17–19] and physical properties for the double perovskites have been reported [20,21]. In such systems, the magnetic and electronic properties are governed by B and B' superexchange interaction through the O atom. Much like conventional perovskite systems, the double perovskites have been reported to exhibit metallic [22], insulator [23], superconductivity [24], colossal magnetoresistance [14], magnetic order [25], and frustrated magnetism [26], as well as multiferroicity [27].

LaSrNiReO_6 is a double perovskite with two different magnetic ions, Ni (B) and Re (B') [see Fig. 1(a)]. In this

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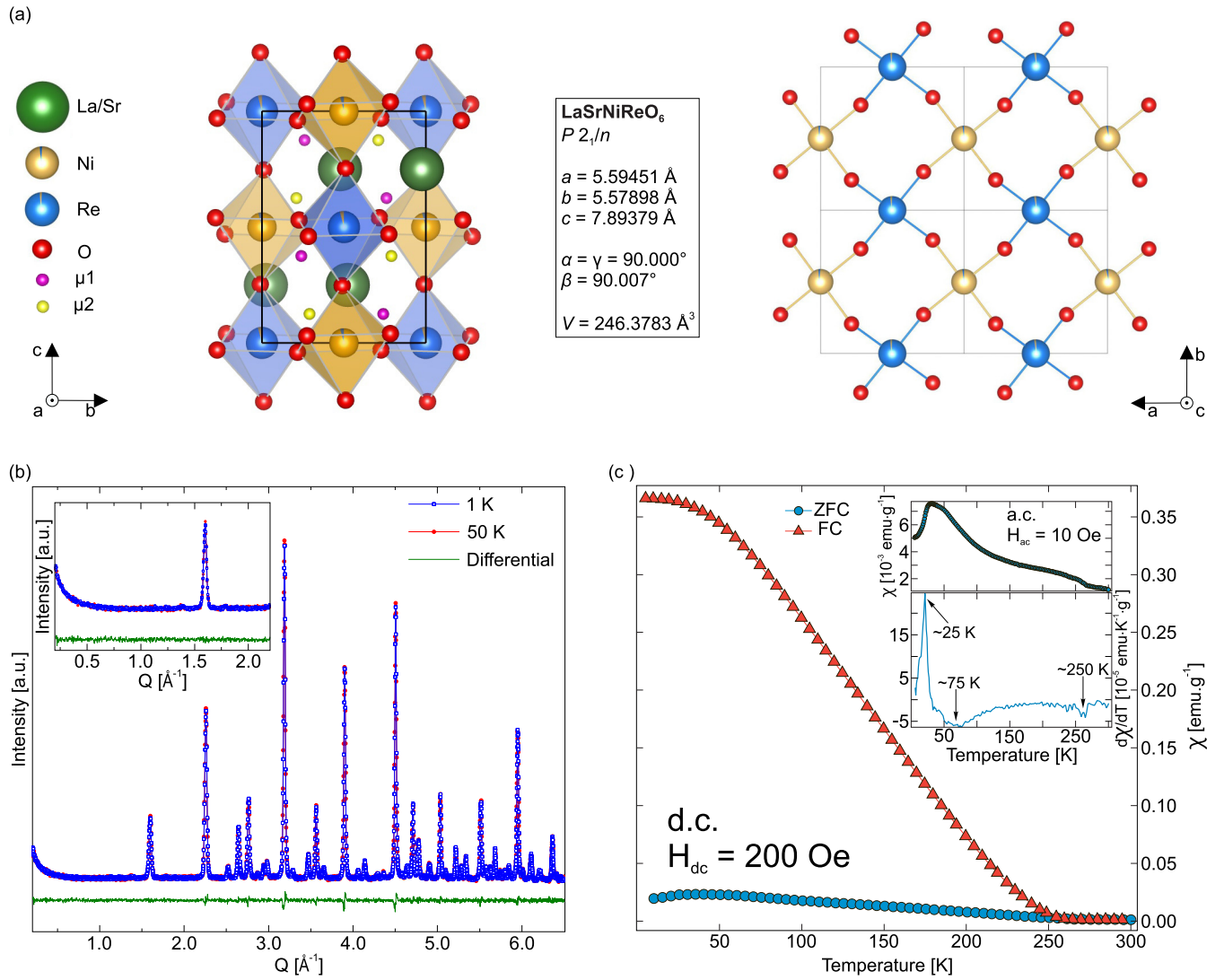


FIG. 1. Crystal structure, neutron powder diffraction pattern, and magnetic susceptibility of LaSrNiReO_6 . (a) On the left is the crystal structure of LaSrNiReO_6 with Ni-O and the Re-O octahedra displayed in orange and blue, respectively. The two predicted muon sites are included as magenta and yellow spheres: site $\mu 1$ at (0.21,0.26,0.875) and site $\mu 2$ at (0.26,0.21,0.625). On the right is a top view of the Re-O and Ni-O lattices. The Sr/La atoms are hidden for clarity. The Ni and Re atoms are displayed in orange and blue, while the Sr/La are in green and the oxygen in red. (b) Neutron powder diffraction data showing the patterns collected above (red filled circles) and below (blue open circles) the transition temperature. The inset is a zoom of the patterns between $Q = 0.2$ and 2.2 \AA^{-1} . The absence of magnetic Bragg peaks is made obvious with the difference plot displayed in green. (c) Zero-field-cooled and field-cooled (ZFC and FC) magnetic susceptibility of LaSrNiReO_6 measured under a field of $H = 200 \text{ Oe}$. Inset shows the temperature dependence of the ZFC magnetic susceptibility in an applied field of 10 Oe , and its temperature derivative highlighting each transition.

particular system, an overlap between orbital symmetry is missing for an effective superexchange interaction. Instead, the ground state is determined by no or weakly interacting magnetic sublattices. A previous study by Ref. [28] observed a frequency-dependent shift in the cusp of ac susceptibility, from where a spin glass ground state was suggested. Moreover, neutron diffraction studies indicated absence of long-range ordering [28,29], in line with a spin glass scenario. For the current sample, the absence of magnetic Bragg peaks in the neutron diffraction pattern are confirmed, as shown in Fig. 1(b). In order to further clarify the ground state, we initiated a muon spin rotation, relaxation, and resonance (μ^+ SR) study. Being a local probe and highly sensitive to magnetism, μ^+ SR is the ideal tool to detect any weak magnetic inter-

actions. Moreover, μ^+ SR allows for measurements in zero field (ZF) and/or weakly applied fields, meaning any influence from the measurements itself can be considered minimal, in comparison to, e.g., magnetic susceptibility measurements. However, local perturbations may be induced, as in Pr-based materials (pyrochlores [30] or PrIn_3 [31]), where the muon causes an anisotropic local modification to the crystal field levels. In this study, a spin precession frequency is observed at the lowest temperature of $T = 2 \text{ K}$, clearly excluding a spin glass scenario. Instead, an incommensurate long-range dynamically ordered ground state below $T_C = 23 \text{ K}$ is proposed. Such state is still in line with previous neutron diffraction [28,29] and χ^{AC} [28] results, as will be shown. Furthermore, between 23 K and 300 K , our μ^+ SR results distinguish three

other magnetic regimes, including dense, dilute, and paramagnetic states. Our findings demonstrate how two separate yet intertwined magnetic lattices interact over a wide temperature range within the unique double perovskite structure. This study also establishes the unique capabilities of the μ^+ SR technique for investigating static and dynamic spins on the microscopic (local) length scale, and underlines the importance of combining complementary techniques to get insights on the true physical properties of complex materials.

II. EXPERIMENTAL METHODS

A polycrystalline sample was prepared using a solid state reaction based on pure La_2O_3 , SrCO_3 , NiO , Re_2O_7 , and Re metal as starting materials. Stoichiometric mixtures of the starting materials reacted in different steps at high temperatures, resulting in a single-phased LaSrNiReO_6 . Details about the synthesis and basic characterization of the sample are found in Ref. [29].

The crystal structure of LaSrNiReO_6 was generated using the Visualization for Electronic and STructural Analysis (VESTA) [32] software. The magnetic susceptibility measurement was performed using both a physical property measurement system (PPMS) and a SQUID magnetometer from Quantum Design. The dc and ac magnetic susceptibilities were recorded as a function of temperature under a magnetic field $H_{\text{dc}} = 200$ Oe and $H_{\text{ac}} = 10$ Oe, respectively, within a temperature range of $T = 5$ –300 K.

The neutron powder diffraction (NPD) experiments were performed at the High-Resolution Powder Diffractometer for Thermal Neutrons (HRPT) [33] instrument at the Swiss Spallation Neutron Source (SINQ), Paul Scherrer Institute (PSI), Switzerland. About 1 g of the sample was filled in a vanadium can and measured with two neutron wavelengths of $\lambda = 1.886$ and 2.95 Å at $T = 1$ and 50 K.

The μ^+ SR experiments were performed at the surface muon beamline M20 and DOLLY instruments at TRIUMF and PSI, respectively. Approximately 1 g of the sample was prepared inside a thin (~ 50 μm) aluminium coated mylar envelope, mounted on a Cu fork sample stick. A standard ^4He flow cryostat was used in order to reach $T_{\text{base}} = 1.8$ K for PSI/DOLLY and $T_{\text{base}} = 2.4$ K for TRIUMF/M20. Finally, the software package musrFIT was used in order to analyze the data [34].

III. RESULTS

A. Neutron powder diffraction and magnetic susceptibility

Magnetization and neutron powder diffraction measurements were performed [Figs. 1(b) and 1(c)] before the μ^+ SR experiments. Starting with the $\chi(T)$, two clear magnetic transitions are observed around $T = 250$ K and $T = 25$ K, which agree with previous reports [28,29]. An additional transition around $T = 75$ K is made clear in the zero-field-cooled (ZFC) configuration and its temperature derivative [inset of Fig. 1(c)].

Figure 1(b) displays the neutron diffraction patterns recorded at temperatures above and below the transition ($T \sim 25$ K) and their difference plot. No magnetic Bragg peaks or reduction of paramagnetic diffuse scattering are

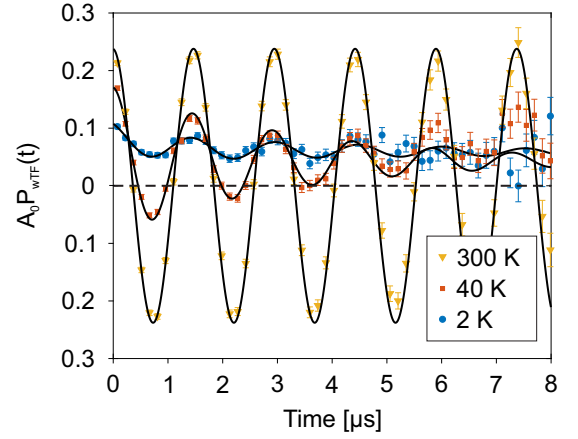


FIG. 2. Weak transverse field (wTF = 50 G) time spectra recorded at $T = 2$ K, 40 K, and 300 K. The solid lines are fits obtained using Eq. (1). A clear oscillatory trend can be seen as a function of temperature and the maximum asymmetry is fully recovered at 300 K.

observed [see inset of Fig. 1(b)] (only slight thermal expansion is seen) within this temperature range. It is worth mentioning that the paramagnetic diffuse scattering may not be observed within the experimental resolution of the present NPD measurement. However, the ordered moments are sufficient to provide magnetic Bragg peaks (see Sec. IV), and their absences exclude a long-range magnetic order, which is in line with previous NPD measurements performed between $T = 2$ and 300 K [28,29]. Detailed NPD and magnetization analysis can be found in Refs. [28,29]. In order to clarify the nature of the ambiguous ground state, μ^+ SR measurements were performed at selected temperatures.

B. Muon spin rotation

μ^+ SR measurements in zero-field (ZF) and weak-transverse-field (wTF) configurations were performed. Here, the field in transverse directions refers to the applied field direction with respect to the initial t_0 muon spin polarization, whereas the term weak signifies that the applied field is significantly weaker than the internal field at low temperatures.

1. Weak transverse field

The obtained time spectra for selected temperatures under wTF = 50 Oe are presented in Fig. 2. Apart from the oscillation resulting from the applied external magnetic field, an offset is observed at lower temperatures. Therefore, the wTF time spectra were fitted using an oscillatory component and two nonoscillatory depolarizing components according to

$$A_0 P_{\text{wTF}}(t) = A_{\text{TF}} \cos(2\pi f_{\text{TF}} t + \phi_{\text{TF}}) e^{-(\lambda_{\text{TF}} t)} + A_{\text{S}} e^{(-\lambda_{\text{S}} t)} + A_{\text{F}} e^{(-\lambda_{\text{F}} t)}, \quad (1)$$

where A_0 is the initial asymmetry and P_{TF} is the muon spin polarization function in a wTF configuration. A_{TF} , f_{TF} , ϕ_{TF} , and λ_{TF} are the asymmetry, frequency, relative phase, and depolarization rate, respectively, originating from the applied wTF. Further, A_{S} , λ_{S} , A_{F} , and λ_{F} are the asymmetry and the respective depolarization rates originating from internal

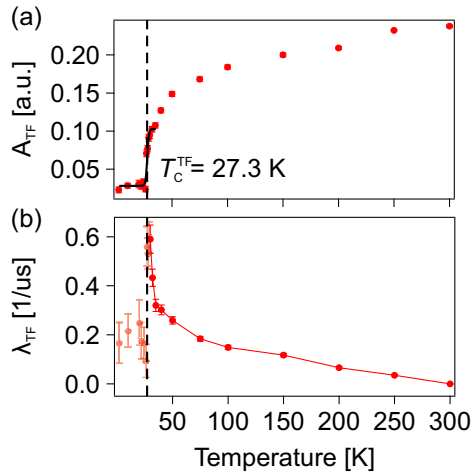


FIG. 3. Summary of the temperature-dependent transverse field fitting parameters. (a) Transverse field asymmetry (A_{TF}) versus temperature. The transition temperature at $T_C^{TF} = 27.3(3)$ K is deduced from a sigmoid fit (black solid line). The maximum asymmetry is only reached above $T = 250$ K. (b) Depolarization rate (λ_{TF}) versus temperature. A clear increase of λ_{TF} is seen at the transition which decreases to near zero at high temperatures. The points below the transition (orange filled circles) are neglected (see text). The solid line is a guide to the eye.

magnetic fields. The indices S and F are conventions used to represent slow and fast components.

The obtained fit parameters for the oscillatory components are summarized in Fig. 3. While the phase and the frequency remain constant through the whole temperature range, the amplitude of the oscillatory component (A_{TF}) changes drastically. A_{TF} corresponds roughly to the paramagnetic fraction of the sample and the abrupt increase from low to high temperature represents a transition from a magnetically ordered to a disordered state. The transition temperature is then defined as the middle point of a sigmoid fit in which $T_C^{TF} = 27.3(3)$ K is obtained. The full asymmetry is only recovered above 250 K, confirming a magnetic contribution to be present up to about 250 K as also suggested from the susceptibility data shown in Fig. 1(c). The nature of this transition will be further discussed in Sec. IV. As expected, the slow component (A_S) is nonzero (not shown) until the full asymmetry of A_{TF} is recovered. Moreover, A_{TF} is low, but nonzero below the transition temperature ($A_{TF} \simeq 0.02$ corresponding to $\sim 9\%$ of the signal), suggesting that part of the muon beam partially hits the sample holder and/or beamline, creating a small background contribution.

The transverse field depolarization rate, λ_{TF} , approaches zero at higher temperatures as expected in the extreme motional narrowing limit of fluctuating magnetic moments. As the temperature is lowered, a critical behavior is displayed close to the transition with a sharp maximum around T_C^{TF} . Such behavior is consistent with critical slowing down of the magnetic moments and broadening of the internal field distribution. Given that the applied field is weak with respect to the internal field, the λ_{TF} values below T_C^{TF} are not considered due to the demagnetization field of the sample ($\lambda_{TF} \simeq 0.2 \mu s^{-1}$ originates from the background signal).

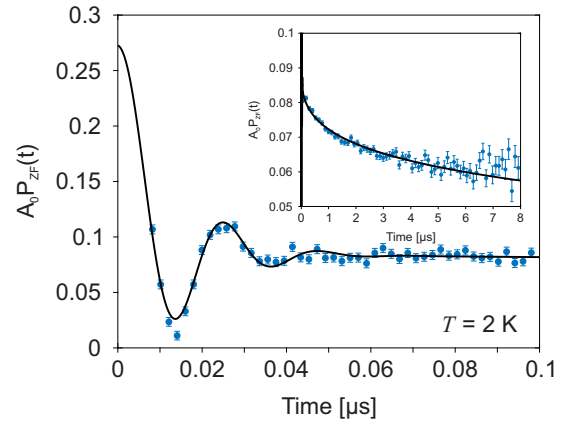


FIG. 4. Short time domain of the zero-field (ZF) time spectrum recorded at $T_{base} \simeq 2$ K, where a damped oscillation is seen. Inset shows the same data in the long time domain. The solid line is a fit of the ZF time spectrum using Eq. (2).

2. Zero field

Figure 4 displays a ZF measurement at $T \simeq 2$ K. The shorter time domain exhibits a highly damped oscillation, which originates from field components perpendicular to the initial muon polarization. The longer time domain (inset Fig. 4) reflects the spin dynamics (the so-called tail component) and was best fitted by a stretched exponential. The time spectrum was then fitted using a combination of a stretched exponential and a Gaussian depolarizing oscillating function

$$A_0 P_{ZF}(t) = A_{IC} J_0(2\pi f_{IC} t) e^{-(\lambda_{IC} t)^{\beta_{IC}}} + A_S e^{-(\lambda_S t)^{\beta_S}}, \quad (2)$$

where A_0 is the initial asymmetry, P_{ZF} is the muon spin polarization function in ZF configuration, and A_{IC} , f_{IC} , β_{IC} , and λ_{IC} are the asymmetry, frequency, stretched exponent, and depolarization rate for the oscillatory component, respectively. J_0 is the zero-order Bessel function of the first kind, while A_S , λ_S , and β_S are the tail components originating from the fact that 1/3 of the field components inside the sample are parallel to the initial muon spin polarization. The tail component exhibits a stretched exponential polarization with a temperature-dependent stretched exponent, β_S . Physical interpretation of the stretched exponent is not trivial, but the function is derived by assuming a distribution of depolarization rates [35,36]. However, a microscopic origin for $\beta = 1, 2, 0.5$ exists: $\beta = 1$ denotes an exponential depolarization channel ('magnetically homogeneous'), while $\beta = 2$ is a Gaussian depolarization channel (quasistatic field distribution) and $\beta = 0.5$ is a so-called root exponential (e.g., a distribution of spin correlation times, also seen above the transition temperature in spin glasses in the motional narrowing limit). A complete interpretation behind Eq. (2) is further discussed in Sec. IV.

a. Below the transition temperature $T = 27$ K. The ZF time spectra from $T \simeq 2$ K up to $T = 27$ K were analyzed using Eq. (2) and the obtained fit parameters are displayed in Fig. 5. At the base temperature, $A_S \simeq A_0/3$ and $A_{IC} \simeq 2A_0/3$, consistent with being the tail and perpendicular components. It should be noted that the $t = 0$ value of the asymmetry obtained is slightly overestimated because of lack of data

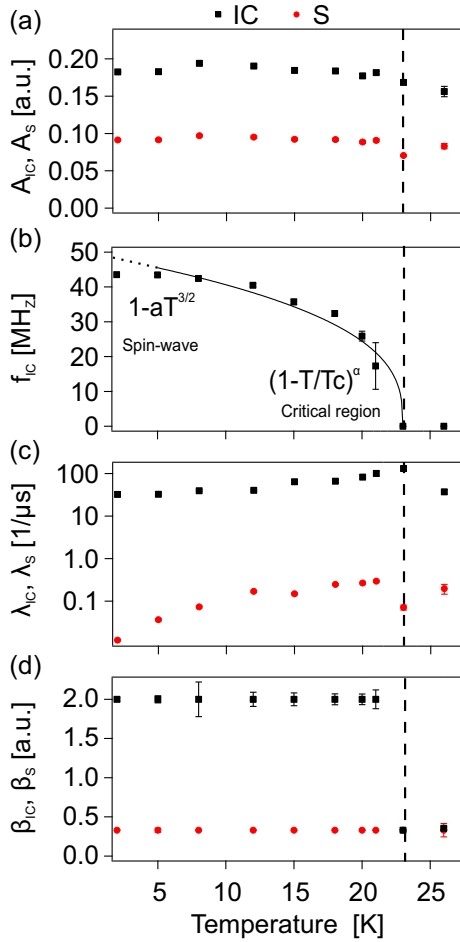


FIG. 5. Temperature dependence of the fit parameters from series of ZF time spectrum from $T = 2$ K to 27 K. (a) Asymmetries, (b) precession frequency, (c) depolarization rates (log scale), and (d) stretched exponents. The solid line in (b) is a fit using $f(T) = f(0)(\frac{T_C - T}{T_C})^\alpha$ down to $T = 5$ K. The low-temperature dotted part is extrapolated.

points at low times. While the asymmetries [Fig. 5(a)] are more or less constant up to the transition, drastic changes can be seen around the transition temperature for the other parameters. The temperature-dependent muon precession frequency confirms an order parameter like dependence and displays a clear transition from an ordered to a disordered state [Fig. 5(b)]. The value of the frequency is directly proportional to the internal field at the muon site. From mean field theory, a fit according to $f(T) = f(0)(\frac{T_C - T}{T_C})^\alpha$ results in $T_C^{ZF} = 23.0(1)$ K, $\alpha = 0.348(47)$, and $f(0) = 49.57(2.49)$. The low-temperature part is not well fitted due to thermal magnon excitation, resulting in a reduction of local spontaneous magnetization given by the Bloch 3/2 law [37]. Note that the slightly higher transition temperature extracted from the wTF measurement ($T_C^{TF} = 27.3$ K) may be due to the applied field and in general, only the ZF data reflect the intrinsic magnetic properties of materials.

Both depolarization rates [Fig. 5(c), plotted for the ordinate axis in log scale] seem to have similar temperature dependence, where the values are increasing as T increases,

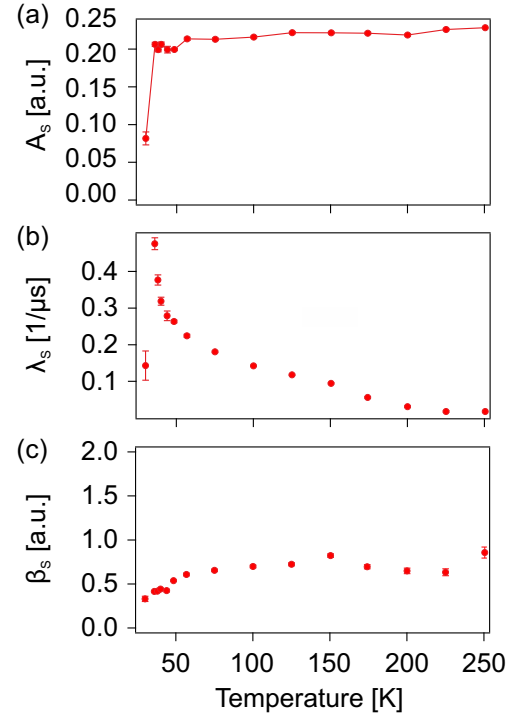


FIG. 6. Temperature dependence of the fit parameters from series of ZF time spectrum from $T = 27$ to 250 K: (a) Asymmetry, (b) depolarization rate, and (c) stretched exponent. The solid line in (a) is a guide to the eye.

consistent with an increase of dynamics close to the phase transition. The parallel component, λ_S , corresponds roughly to the spin-lattice relaxation rate and contains information about the dynamics in the system, while λ_{IC} includes a mixture of both the field distribution and the dynamics. Therefore, the relatively high value of $\lambda_{IC} = 32.4(1.2) \mu s^{-1}$ at T_{base} relates to a high field distribution and dynamics at the muon sites. However, the behavior of $\lambda_S \rightarrow 0$ as $T \rightarrow 0$ is consistent with the sample's magnetism going toward the static limit. Since λ_{IC} seems to level off at lower temperatures, the high value of λ_{IC} originates mostly from a broad field distribution. Based on the temperature dependence of λ_S , a completely static magnetic ground state is expected below $T = 2$ K. Nevertheless, the value $\lambda_S(2 \text{ K}) = 0.012(1) \mu s^{-1}$ is still observed, meaning that the spins are dynamic even at lowest measured temperature. Finally, the stretched exponents are almost constant up to the transition. The stretched exponent of $\beta = 2$ is a Gaussian depolarization channel suggesting that the magnetic phase is quasistatic. $\beta = \frac{1}{3}$ corresponds to the magnetic impurity limit and has already been reported in several spin glass systems [38–40].

b. Above the transition temperature $T = 27$ K. The sample was also studied in ZF configuration for temperatures above T_C^{ZF} up to $T = 250$ K. The data are also well fitted using Eq. (2) in this temperature range (note that $A_{IC} = 0$ above T_C^{TF}). The obtained fit parameters as a function of temperature are shown in Fig. 6. A clear increase in asymmetry is shown with increasing temperature until the maximum asymmetry $A_0 \approx 0.24$ is recovered. The depolarization rate is exhibiting a critical behavior just above T_C^{ZF} . The narrow temperature

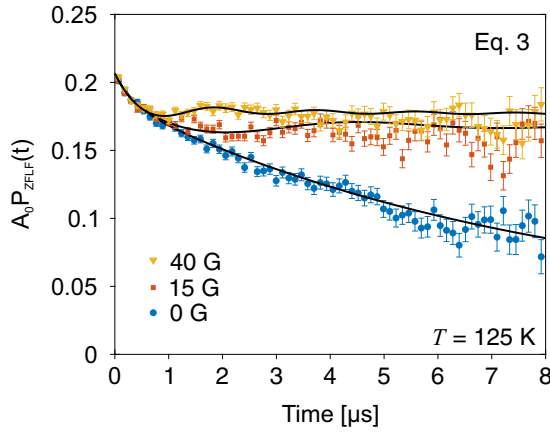


FIG. 7. Zero-field (ZF) and longitudinal field (LF = 15 and 20 G) time spectra with best fits using Eq. (3) are shown as solid black lines.

range of this critical slowdown of electronic moments suggests an exchange coupling $J \sim k_B T_C$. As for the stretched exponent, a recovery of $\beta \rightarrow 1$ is observed at the highest temperature, as expected. Moreover, $\beta \rightarrow \frac{1}{3}$ is seen around the transition, typical for many glassy-like transitions [38–40]. Longitudinal field measurements (LF = 15 and 40 G) show that Eq. (2) may not be suitable in the temperature range of 75–250 K where $\beta \sim 0.7$, because the value of β changes dramatically with the applied field (see the Appendix and Fig. 11). Instead, the ZF+LF time spectra were nicely fitted (Fig. 7) with the following function for this temperature range,

$$A_0 P_{ZF}(t) = A_F e^{-\lambda_F t} + A_{KT} L^{SLKT}(\Delta, t), \quad (3)$$

where A_0 is the initial asymmetry, P_{ZF} is the muon spin polarization function in ZF configuration, and A_F and A_{KT} are the asymmetries for their respective contribution, where L^{SLKT} represents a static Lorentzian Kubo-Toyabe. λ_F is the depolarization rate for an initial fast depolarizing signal, while Δ is related to the internal Lorentzian half-width at half-maximum. The L-KT is the dilute limit of the KT, commonly observed in paramagnets with the presence of dilute magnetic moments [41,42]. A_F is therefore attributed to the fraction of muons sitting close to these dilute magnetic highly fluctuating moments. Indeed, it is only for $T > 250$ K that a Gaussian KT could fit the data, meaning that dilute electronic magnetic moments are present up to this temperature. Furthermore, the data below 75 K could not be fitted to any type of Kubo-Toyabe functions (i.e., dynamic/static Gaussian or Lorentzian distributed KT). This suggests the presence of a distribution of relaxation times for $23 \text{ K} < T < 75 \text{ K}$. Equation (3) is further discussed in Sec. IV.

The obtained fit parameters using Eq. (3) are displayed in Fig. 8. The KT asymmetry slowly recovers the full asymmetry as the temperature increases, while the fast-relaxing component decreases, suggesting that the number of dilute moments is decreasing with temperature. Naturally, this decrease will also show in the temperature dependence of Δ . In principle, Eq. (3) may be replaced by the dynamical L-KT. However, dynamical contributions are usually observed in the tail of the KT, which is not accessible in the present data. Instead, the

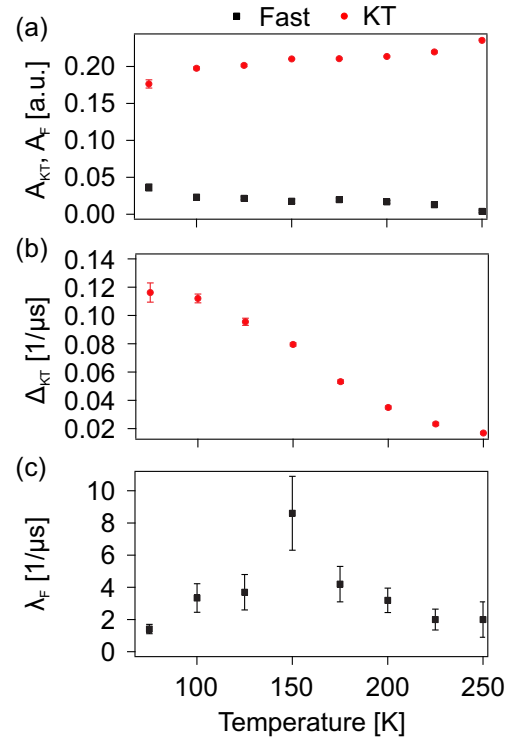


FIG. 8. Temperature dependence of the fast and Kubo-Toyabe (KT) fit parameters from Eq. (3), obtained from series of ZF time spectrum from $T = 70$ K to 250 K: (a) Asymmetry, (b) field distribution width, and (c) depolarization rate.

dynamical contribution is affecting the field distribution width, which is decreasing with increasing temperature. Strangely, the depolarization rate (λ_F) seems to exhibit a maximum around 150 K. Indeed, a small anomaly can also be observed around this temperature in the stretched exponent, shown in Fig. 6(c). The origin of this anomaly is currently unknown and further investigations are required. However, such anomaly does not affect the main results and conclusion drawn in this report.

IV. DISCUSSION

Based on the results presented in Sec. III, the following four magnetic states are identified (Fig. 9): (1) a magnetically ordered state below $T_C^{ZF} = 23$ K, (2) a glassy-like transition to a random dense magnetic state between $23 \text{ K} < T < 75 \text{ K}$, (3) a random dilute magnetic phase between $75 \text{ K} \leq T \leq 250 \text{ K}$, and (4) a paramagnetic state above $T > 250 \text{ K}$. The presence of several magnetic phases is further supported by the magnetic susceptibility measurements shown in Fig. 1(c) and Ref. [29], where both the transition at $T \approx 23$ K and the bifurcation between ZFC and FC curves at $T \approx 250$ K were reported. The latter has also been observed in $\text{Sr}_2\text{CaReO}_6$ [43] and $\text{Sr}_2\text{InReO}_6$ [44] double perovskite compounds and attributed to the nonmagnetic ions located at the B site, causing a geometrical frustration of the Re site on the fcc sublattice. Such situation would lead to a dilute magnetic system and an L-KT-like depolarization would manifest the ZF time spectrum in $\mu^+\text{SR}$, as presented here. Typically, an L-KT

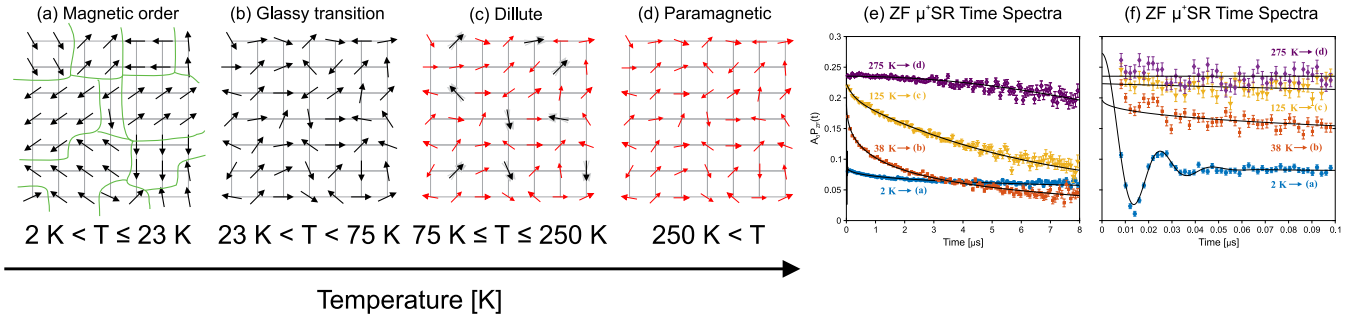


FIG. 9. The different magnetic phases and the corresponding ZF μ^+SR time spectra highlighted in this study with schematic representation of electronic moments (black) and nuclear moments (red). (a) Magnetic order with a distinct correlation length (see text), (b) dense or glassy-like transition, (c) dilute state, (d) paramagnetic phase and ZF time spectra at respective temperatures for each highlighted phase in (a)–(d) in short (e) and long (f) time domains. The solid black lines represent Eq. (2) (2 K and 38 K), Eq. (3) (125 K), and $A_{KT}G^{SGKT}(\Delta, t)$ (275 K), where G^{SGKT} represents a static Gaussian Kubo-Toyabe.

fit is appropriate for dilute electronic moments existing in a nonmagnetic matrix. Moreover, the weak temperature dependence of λ_S from ZF measurement supports such situation in which dilute moments fluctuate [Fig. 6(b)].

In the same temperature region, a stretched exponent of $\beta \sim 0.7$ was obtained. While the stretched exponential is somewhat phenomenological, such value is perhaps indicative of an intermediate case between a dilute and dense motionally narrowed source of magnetic fields. If the magnetic distribution in real space is dense, the field distribution can be approximated by a Gaussian shape for which the muon spin depolarization follows an exponential in the motional narrowing limit. In the dilute limit, the muon spin depolarizes according to a root exponential in the narrowing limit. Therefore, a $\beta \sim 0.7$ for $75 \text{ K} \leq T \leq 250 \text{ K}$ could perhaps be explained as an intermediate case of dense and dilute source of magnetic fields [39,45].

A stretched exponential like depolarization is observed in a wide temperature range ($23 \text{ K} < T < 75 \text{ K}$). Such a situation is usually explained by the presence of a distribution of muon depolarization channels (i.e., spatially disordered systems). The magnetically similar compounds Sr_2NiWO_6 and $\text{Sr}_2\text{NiTeO}_6$ possess nonmagnetic W^{6+} and Te^{6+} ions at the B' site. The Ni $3d$ moments in these compounds order at $T_N = 35 \text{ K}$ and $T_N = 54 \text{ K}$, respectively [46]. Therefore, it seems that some localized moments of Ni^{2+} become prominent at lower temperature for the title compound, effectively destroying the dilute limit and resulting in a distribution of relaxation rates. Therefore, we suggest that an independent Ni sublattice feature is realized below $T_C^{\text{ZF}} = 23 \text{ K}$, resulting in magnetic order. In other words, the Re^{5+} interactions/fluctuations dominate at higher temperature, while the Ni^{2+} interactions become significant at lower temperature. Admittedly, the presented data cannot distinguish the Ni^{2+} moments from Re^{5+} moments, meaning that the opposite case in which the Re^{5+} orders at low T instead of Ni^{2+} is also probable.

Transport measurements [29] suggested that the transition at $T \sim 30 \text{ K}$ is due to a weak ferromagnetic interaction, predicted by Goodenough-Kanamori rules. However, in this study, a Bessel function was used instead of a simple cosine function to fit the time spectrum. This would suggest an incommensurate magnetic ordering at low temperatures. This is justified because using a cosine function results in a

large offset in the initial phase $\phi \approx -50^\circ$ (see the Appendix). For a particular case of an incommensurate single- k collinear magnetic structure the polarization function is given by

$$J_0(\gamma_\mu B_{\text{max}} t) \simeq \sqrt{\frac{2}{\pi \gamma_\mu B_{\text{max}} t}} \cos(\gamma_\mu B_{\text{max}} t - \pi/4). \quad (4)$$

A phase offset may also be realized in magnetic structures, e.g., in cases where the local field fluctuates from parallel to antiparallel direction at a rate $v_c < 2\gamma_\mu B_{\text{fluc}}$ [47]. However, the spin-lattice relaxation rate [λ_S in Fig. 5(c)] indicates a decrease in dynamics with temperature, which in turn would change the phase offset as a function of temperature (not this case). Another case was reported by Ref. [48], where several muon sites were present within a larger magnetic unit cell. While the presence of several muon sites could explain the stretched exponential behavior in this study, only one clear oscillating signal was observed meaning only one (or possibly two magnetically similar) muon site is expected for this compound. Consequently, LaSrNiReO_6 most likely display an incommensurate magnetic spin order below T_C^{ZF} .

It should also be noted that the muon spin precession frequency at the lowest temperature was effectively lowered due to the reduction in spontaneous magnetization [Fig. 5(b)] [37]. However, such situation is only realized for ferro- and ferrimagnets. Indeed, the transition at $T \sim 30 \text{ K}$ was predicted to be due to a weak ferromagnetic interaction [29] according to Goodenough-Kanamori rules. Consequently, given the fact that we observe an incommensurate order, the ground state of LaSrNiReO_6 points toward an incommensurate ferrimagnetic state.

The presence of an oscillatory component in the μ^+SR time spectrum for $T \leq 23 \text{ K}$ (Fig. 4) suggests a magnetically ordered ground state, where χ^{AC} measurements also predicted a magnetic transition occurring around 27 K. However, magnetic Bragg peaks were not observed in the neutron diffraction measurements [28,29] and such discrepancy should be addressed. First off, let us point out that the internal field distribution is wide, as implied by the highly damped oscillation (λ_{IC}). As mentioned, the parallel component of the ZF measurement, λ_S , indicated a dynamic state at the base temperature. While it is possible for spins to be dynamic in only specific directions, it is noted that the measurement was

performed on a powder sample meaning any spatial direction should be averaged out. Furthermore, λ_{IC} seems to level off at lower temperatures while λ_S continues to decrease [Fig. 6(c)]. Therefore, the high damping of the oscillatory component, λ_{IC} , observed in Fig. 5 should mainly be due to a wide field distribution width and supports the fact that the sample is magnetically inhomogeneous. Naturally, magnetically inhomogeneous systems do not yield any clear magnetic Bragg peaks in NPD, which would suggest a short-range magnetic order. However, the observation of an oscillation in the ZF μ^+ SR time spectrum points toward a long-range magnetic order.

The absence of magnetic Bragg peaks in the low-temperature NPD pattern could be connected to a weakly ordered moment. The ordered moment can be estimated from the present μ^+ SR data and by predicting the possible muon site using the density functional theory (DFT) package QUANTUM ESPRESSO [49,50]. For such calculation, (i) the chemical disorder was not considered, (ii) any local perturbations due to the muon were not considered, and (iii) the muon site was assumed to be at the electrostatic potential minimum. Given the above assumption, a self-consistent calculation using the pseudopotentials described by Refs. [51,52] provides two possible muon site candidates $\mu 1$ at (0.21,0.26,0.875) and $\mu 2$ at (0.26,0.21,0.625) (see Fig. 1). Assuming now that the magnetic structure is the same as that of the sister compound LaCaNiReO₆ [29] and that the local field is solely composed of dipolar fields (B_{dip}), the expected internal fields at these sites are calculated to be $f_1 = 45.31$ MHz and $f_2 = 42.49$ MHz ($B_{dip} = f\gamma_\mu$). For these internal fields, the Ni²⁺ and Re⁵⁺ moments were set to $\mu_{Ni} = 2 \mu_B$ and $\mu_{Re} = 1 \mu_B$, respectively. Indeed, the expected internal field for the assumed moment sizes is very close to the experimental one $f(0\text{ K}) = 49.57(2.49)$ MHz (Fig. 5). Therefore, we deduct that the ordered moment is strong enough to be detected by the NPD experiment.

A previous report based on ac susceptibility measurements suggested a spin glass state below $T \sim 25$ K [28]. Indeed, just like in this case, many spin glasses exhibit $\beta \rightarrow \frac{1}{3}$ around the transition temperature. However, the presence of a muon spin precession clearly excludes such scenario. Instead, we suggest that an incommensurate order is stabilized with a distinct magnetic correlation length (ξ) that is long enough for detection for μ^+ SR and χ^{AC} techniques, but not for neutron diffraction (hence magnetically inhomogeneous). On a macroscopic scale, the system may look like a spin glass, where small magnetic domains freeze randomly. However, microscopically, each of these domains is in fact ordered on a shorter length scale [Fig. 9(a)]. Overall, this kind of microscopic picture would yield a frequency-dependent shift in χ^{AC} while also yielding muon spin precession, and the absence of magnetic Bragg peaks in neutron diffraction is explained. From our knowledge, this is a very rare case where such a situation is present and so clearly revealed.

V. CONCLUSIONS

We have utilized muon spin rotation (μ^+ SR) to elucidate the magnetic properties of the double perovskite compound

LaSrNiReO₆. Using the unique length and time scales of the μ^+ SR technique, we have successfully identified four magnetic states: a paramagnetic ($T > 250$ K), a dilute ($75\text{ K} \leq T \leq 250\text{ K}$), a dense ($23\text{ K} < T < 75\text{ K}$), and an incommensurate magnetically ordered state ($2\text{ K} < T \leq 23\text{ K}$). The dilute state is established by weakly interacting and fluctuating Re⁵⁺ ions sitting on the B' site, which develops into an incommensurate order around 23 K, driven by the fcc sublattice of Ni ions on the B sites. This state consist of weakly interacting domains/islands, established by a ferri-magnet interacting with spins, forming an incommensurate spin wave. This study reveals in great detail how two separate yet intertwined magnetic lattices interact over a wide temperature range within the unique double perovskite structure. It also shows the unique capabilities of the μ^+ SR technique for studying static and dynamic spins on the microscopic (local) length scale. We also emphasize the importance of applying a set of complementary experimental techniques in order to obtain a complete and correct understanding of the microscopic magnetic properties in complex materials.

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APPENDIX: ZF FITTING PROCEDURE AT LOW TEMPERATURES

Equation (2) is composed of a zero-order Bessel function of its first kind, instead of a simple cosine function. This was justified because a cosine function yields unreasonably large values of phase. For clarity, a fit using a cosine function is shown in Fig. 10 and a clear phase shift is observed. As a result, a zero-order Bessel function of its first kind was chosen instead of a simple cosine function. Additionally, the asymmetry of the oscillatory component is underestimated with respect to A_0 for the cosine function. However, a small

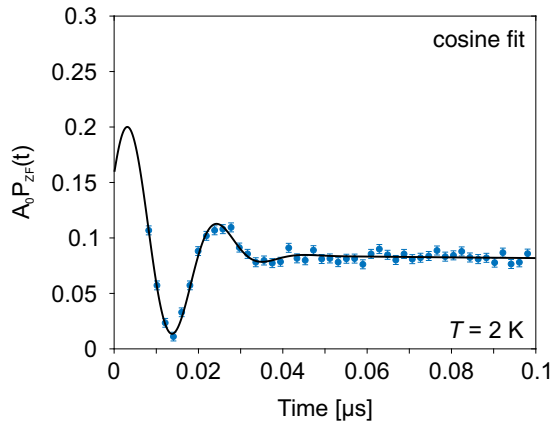


FIG. 10. Short time domain of the zero-field (ZF) time spectrum recorded at $T_{\text{base}} \simeq 2$ K, where a damped oscillation is seen. The solid line is a fit of the ZF time spectrum using $A_0 P_{\text{ZF}}(t) = A_C \cos(2\pi f_C t + \phi) e^{-(\lambda_C t)^2} + A_S e^{-(\lambda_S t)^{\beta_S}}$: $A_C = 0.115(7)$, $\lambda_C = 48(2) \mu\text{s}^{-1}$, $\phi = -54(2)^\circ$, $f_C = 45(1) \text{ MHz}$, $A_S = 0.0912(4)$, $\lambda_S = 0.0121(7) \mu\text{s}^{-1}$, and $\beta_S = 0.330(3)$.

overestimation is observed with fits using Eq. (2). The choice of oscillatory component does not affect the tail component.

Figure 11 shows the ZF+LF time spectrum collected at $T = 125$ K. As described in the main text, a fit using Eq. (2) results in a wide change in the parameter β : 0.66(3) at ZF, 0.143(8) at LF = 15 G, and 0.102(7) at LF = 40 G. The

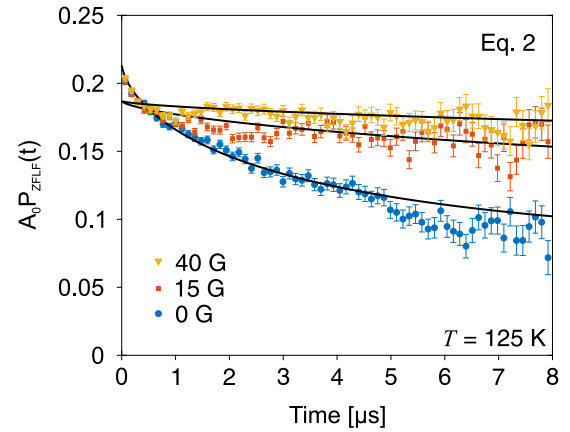


FIG. 11. Zero-field (ZF) and longitudinal-field (LF = 15 and 20 G) time spectra with best fits using Eq. (2) in (a) are shown as solid black lines. A common β was utilized for all field configurations since the spin-spin correlation should be unaffected by such weak LFs.

obtained values under the LF are unreasonably small and more importantly, a large change is seen between ZF and LF suggesting that the spin-spin correlation would change with LF = 15 G. If the parameter is instead shared among the field configurations, a $\beta = 0.65(3)$ is obtained instead. However, the quality of fit is greatly reduced, as seen in Fig. 11. As a result, Eq. (3) was selected for fitting the ZF time spectra in the temperature range $T = 75$ – 250 K.

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