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Stepped-Carrier OFDM V2V Resource Allocation for Sensing and Communication Convergence

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Abstract—Stepped-carrier orthogonal frequency division multiplexing (OFDM) radar is a promising low-cost alternative to conventional OFDM radar for automotive applications due to its capability to provide high resolution with low-rate analog-to-digital converters (ADCs). In this paper, we investigate centralized time-frequency resource allocation strategies in vehicular networks for vehicle-to-vehicle (V2V) sidelinks employing stepped-carrier OFDM waveform for joint radar sensing and communications. To quantify radar-communication performance trade-offs, we formulate a nonlinear integer programming problem for weighted optimization of radar accuracy and communication spectral efficiency, and perform Boolean relaxation to obtain an efficiently solvable convex program. Simulation results demonstrate radar-optimal and communication-optimal operation regimes, providing insights into time-frequency weightings along the trade-off curve.

Index Terms—orthogonal frequency division multiplexing, joint radar communications, resource allocation.

I. INTRODUCTION

Co-design of radar and communication systems has recently received a growing interest as mutual interference becomes a compelling issue in view of a large number of spectrally co-existent radars and communication devices [1]. This trend manifests itself especially in the automotive applications, where a rising percentage of vehicles is equipped with sensors and vehicle-to-vehicle (V2V) radio technology for autonomous driving functionalities [2], [3].

To tackle the problem of spectral congestion in vehicular scenarios, a popular co-design approach is to employ orthogonal frequency-division multiplexing (OFDM) as a dual-functional radar-communication (DFRC) waveform as it allows for easy interaction with communication, while still providing satisfactory radar performance [4]–[8]. The study in [4] proposes an algorithm for target range and velocity estimation using the backscattered OFDM signal. In a similar fashion, [5] addresses the design of an OFDM system where pilots are used by radar receiver for target parameter estimation and by communication receiver for channel estimation. Another research strand focuses on OFDM DFRC waveform design via joint optimization of radar and communication performance objectives [6]–[8]. Mutual information (MI) has been used to characterize both radar and communication performance [6], [7], while the Cramér-Rao bound (CRB) is a widely employed metric for radar estimation accuracy [8].

In this paper, we consider a vehicular joint radar-communications network in which a base station (BS) cen-

trally coordinates time-frequency V2V sidelink resource sharing among vehicles through uplink/downlink communications. The available time-frequency window for sidelink consists of individual OFDM blocks, each containing a number of subcarriers and symbols, as shown in Fig. 1. Unlike the OFDM DFRC frequency domain waveform design studies [4]–[8], our problem of interest herein is to assign OFDM resource blocks to vehicles in the time-frequency domain to maximize overall radar communications performance of the network (which leads to *stepped-carrier OFDM* [9] radar due to frequency hopping across blocks). Using Boolean resource selection parameters of vehicles as variables, a nonlinear integer programming problem is formulated to optimize a compound objective function as a weighted combination of radar CRB and communication spectral efficiency (SE). Through a Boolean relaxation, we transform the optimization problem into an efficiently solvable convex semidefinite program (SDP). Simulation results provide valuable insights into delay-Doppler and radar-communication performance trade-offs.

II. SYSTEM MODEL

We consider an OFDM system with a collection of N vehicles and a base station (BS), as shown in Fig. 1. A total bandwidth W is divided into parts: W_{UD} for uplink and downlink data traffic as well as control signaling, and W_{S} for sidelink traffic. The ADC bandwidth at each vehicle is $W_{\text{block}} \ll W_{\text{S}}$. The OFDM system uses a subcarrier spacing $\Delta_f = 1/T$, with the number of subcarriers $K = W_{\text{block}}/\Delta_f$, and has a basic OFDM symbol duration $T_{\text{S}} = T + T_{\text{cp}}$. In a frame-time of T_{frame} , we have a total of $W_{\text{S}}/W_{\text{block}} \times T_{\text{frame}}/T_{\text{block}}$ time-frequency resource blocks, where each block comprises M OFDM symbols and has a total duration $T_{\text{block}} = MT_{\text{S}}$.

Our goal is to assign resources $b_{i_f, i_t}^{(n)} \in \{0, 1\}$ to each vehicle $n \in \mathcal{N}$ to jointly optimize data rate and radar accuracy, where $i_f \in \mathcal{F} \triangleq \{0, 1, \dots, W_{\text{S}}/W_{\text{block}} - 1\}$, $i_t \in \mathcal{T} \triangleq \{0, 1, \dots, T_{\text{frame}}/T_{\text{block}} - 1\}$ and \mathcal{N} is the set of vehicles in the network. To ensure orthogonality among users, we enforce $b_{i_f, i_t}^{(n)} \times b_{i_f, i_t}^{(n')} = 0$ for any two users n and $n' \neq n$. In addition, due to the ADC bandwidth constraint, each vehicle can occupy at most one resource block at a given time, i.e., $b_{i_f, i_t}^{(n)} \times b_{i'_f, i_t}^{(n)} = 0$ for $i_f \neq i'_f$.

III. COMMUNICATION PERFORMANCE METRIC

We consider unicast communication, where for each vehicle $n \in \mathcal{N}$, there is a dedicated receiver $\mathcal{R}(n) \in \mathcal{N}$. We

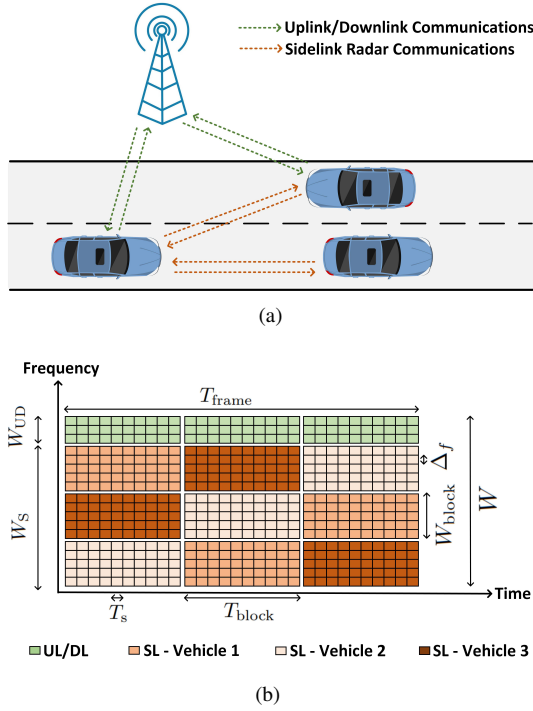


Fig. 1. (a) A vehicular radar communications network whose time-frequency resource allocation over sidelink is coordinated by a base station through uplink/downlink communications. (b) Exemplary time-frequency resource sharing among three vehicles over sidelink, where the aim is to perform joint optimization of overall data rate and radar accuracy.

assume that the receiver knows instantaneous channel state information (CSI) and both the transmitter and the receiver have statistical CSI (which remains constant over a frame duration). The k th OFDM subchannel gain corresponding to the transmit-receive pair $(n, \mathcal{R}(n))$ for the frequency block i_f is assumed to be zero-mean complex Gaussian random variable with variance $(\sigma_{i_f}^{(n, \mathcal{R}(n))}[k])^2$ for $k = 0, \dots, K-1$, known to the BS through uplink. In this scenario, the performance can be measured in terms of sum SE over the blocks, which can be upper-bounded as

$$R^{(n)} \leq \sum_{(i_f, i_t) \in \mathcal{F} \times \mathcal{T}} b_{i_f, i_t}^{(n)} R_{i_f, i_t}^{(n)} \quad (1)$$

where the upper bound for individual blocks is given by [10, Ch. 4.3.3]

$$R_{i_f, i_t}^{(n)} = \sum_{k=0}^{K-1} \log_2 \left(1 + \frac{P_{i_f, i_t}^{(n)}[k] (\sigma_{i_f}^{(n, \mathcal{R}(n))}[k])^2}{N_0 \Delta_f} \right) \quad (2)$$

with $P_{i_f, i_t}^{(n)}[k]$ and N_0 denoting the transmit power on the k th subcarrier and the noise spectral density, respectively.

Let $\mathbf{B}^{(n)} \in \{0, 1\}^{N_f \times N_t}$ denote the Boolean selection matrix that indicates whether vehicle n uses the corresponding time-frequency block $(i_f, i_t) \in \mathcal{F} \times \mathcal{T}$, where $N_f = |\mathcal{F}|$ and $N_t = |\mathcal{T}|$. In the proposed resource allocation framework, the optimization variables are the Boolean selection vectors of all vehicles $\{\mathbf{b}^{(n)}\}_{n \in \mathcal{N}}$, where $\mathbf{b}^{(n)} \triangleq \text{vec}(\mathbf{B}^{(n)}) \in \{0, 1\}^{N_f N_t}$, with $\text{vec}(\cdot)$ representing the matrix vectorization operator

stacking the columns on top of each other. Then, the communication objective on the right-hand side of (1) can be expressed as a function of $\mathbf{b}^{(n)}$ as

$$g^{(n)}(\mathbf{b}^{(n)}) = (\mathbf{r}^{(n)})^T \mathbf{b}^{(n)} \quad (3)$$

where $\mathbf{r}^{(n)} \triangleq \text{vec}(\mathbf{R}^{(n)}) \in \mathbb{R}^{N_f N_t}$, with $\mathbf{R}^{(n)} \in \mathbb{R}^{N_f \times N_t}$ consisting of the elements $R_{i_f, i_t}^{(n)}$ in (2) for $(i_f, i_t) \in \mathcal{F} \times \mathcal{T}$. Equipped with the knowledge of statistical CSIs $\sigma_{i_f}^{(n, \mathcal{R}(n))}[k]$ over all subcarriers and transmitter-receiver pairs, the BS can adjust its resource allocation strategy by employing (3) as the communication performance criterion.

IV. RADAR PERFORMANCE METRIC

A. Radar Signal Model

For radar performance, we consider the accuracy of the estimation of delay τ and Doppler ν , for a typical target (specified by a distance $R = c\tau/2$, velocity $v = c\nu/2$, and complex channel gain α). The OFDM radar observation at a given vehicle (dropping the superscript (n) for simplicity) for the block (i_f, i_t) can be expressed as¹

$$\mathbf{Y}_{i_f, i_t} = b_{i_f, i_t} [\mathbf{P}_{i_f, i_t} \odot \mathbf{X}_{i_f, i_t} \odot \alpha (\Theta_{i_f}(\tau_{i_t})^* \otimes \Phi_{i_t}(\nu))^T + \mathbf{N}_{i_f, i_t}] \quad (4)$$

where

$$\Theta_{i_f}(\tau) \triangleq e^{j2\pi(f_c + i_f W_{\text{block}})\tau} [1, e^{j2\pi\Delta_f\tau}, \dots, e^{j2\pi\Delta_f(K-1)\tau}]^T$$

$$\Phi_{i_t}(\nu) \triangleq e^{j2\pi f_c i_t T_{\text{block}}\nu} [1, e^{j2\pi f_c T_s\nu}, \dots, e^{j2\pi f_c(M-1)T_s\nu}]^T$$

represent delay and Doppler steering vectors, respectively, $\tau_{i_t} \triangleq \tau - \nu i_t T_{\text{block}}$ is the delay for the block (i_f, i_t) , f_c is the carrier frequency, \odot and \otimes denote Hadamard and Kronecker product, respectively, $\mathbf{Y}_{i_f, i_t} \in \mathbb{C}^{K \times M}$ contains the received M OFDM symbols with K subcarriers each, $\mathbf{P}_{i_f, i_t} \in \mathbb{R}^{K \times M}$ is the matrix of transmit powers on subcarriers with the entries $\mathbf{P}_{i_f, i_t}^{(n)}[k, m] = \sqrt{P_{i_f, i_t}^{(n)}[k]}$, $\forall k, m$, $\mathbf{X}_{i_f, i_t} \in \mathbb{C}^{K \times M}$ consists of independent and identically distributed (i.i.d) zero-mean, unit-variance complex Gaussian transmit symbols (i.e., $\text{vec}(\mathbf{X}_{i_f, i_t}) \sim \mathcal{CN}(\mathbf{0}, \mathbf{I})$), and $\mathbf{N}_{i_f, i_t} \in \mathbb{C}^{K \times M}$ contains i.i.d. additive Gaussian noise components with variance σ^2 .

B. Fisher Information Analysis

From the observations $\mathbf{Y} = \{\mathbf{Y}_{i_f, i_t}\}_{(i_f, i_t) \in \mathcal{F} \times \mathcal{T}}$, the modified Fisher information matrix (MFIM) [11] will be used to evaluate the accuracy of estimation of τ and ν since the transmitted symbols \mathbf{X}_{i_f, i_t} are not deterministic. The parameters of interest for the MFIM are given by $\boldsymbol{\eta} = [\tau, \nu, \alpha_R, \alpha_I]^T$, where $\alpha_R \triangleq \Re\{\alpha\}$ and $\alpha_I \triangleq \Im\{\alpha\}$. The (i, j) th element of the 4×4 MFIM can be written as [11]

$$\mathbf{J}_{\boldsymbol{\eta}}[i, j] = \mathbb{E}_{\mathbf{X}} \left\{ \mathbb{E}_{\mathbf{Y} | \mathbf{X}} \left\{ \frac{\partial \log \Lambda(\mathbf{Y} | \mathbf{X}, \boldsymbol{\eta})}{\partial \eta[i]} \frac{\partial \log \Lambda(\mathbf{Y} | \mathbf{X}, \boldsymbol{\eta})}{\partial \eta[j]} \right\} \right\} \quad (5)$$

¹Derivations are omitted due to space limitations.

where $\log \Lambda(\mathbf{Y} | \mathbf{X}, \boldsymbol{\eta})$ is the log-likelihood function of the observations in (4) with $\mathbf{X} = \{\mathbf{X}_{i_f, i_t}\}_{(i_f, i_t) \in \mathcal{F} \times \mathcal{T}}$. After algebraic manipulations on (5), we obtain the MFIM as

$$\mathbf{J}_{\boldsymbol{\eta}} = \begin{bmatrix} (\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{11} & (\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{12} \\ \mathbf{J}_{12}^T (\mathbf{I}_2 \otimes \mathbf{b}) & (\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{22} \end{bmatrix} \in \mathbb{R}^{4 \times 4} \quad (6)$$

where \mathbf{I}_N is the $N \times N$ identity matrix, and the submatrices \mathbf{J}_{11} , \mathbf{J}_{12} and \mathbf{J}_{22} are given in Appendix A. Applying the matrix inversion lemma to (6), we obtain $[\mathbf{J}_{\boldsymbol{\eta}}^{-1}]_{1:2, 1:2} = (\mathbf{G}(\mathbf{b}))^{-1}$, where

$$\mathbf{G}(\mathbf{b}) \triangleq (\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{11} - (\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{12} \left((\mathbf{I}_2 \otimes \mathbf{b})^T \mathbf{J}_{22} \right)^{-1} \mathbf{J}_{12}^T (\mathbf{I}_2 \otimes \mathbf{b}) \quad (7)$$

represents the equivalent MFIM for delay and Doppler parameters. To optimize the delay-Doppler estimation performance of radar, we use the modified Cramér-Rao bound (MCRB) on the covariance matrix of delay and Doppler estimates as our design objective. The MCRB matrix can be obtained as the inverse of the MFIM in (7) [11]. Hence, delay and Doppler estimation variances can be expressed, respectively, as

$$f_{\tau}(\mathbf{b}) = [(\mathbf{G}(\mathbf{b}))^{-1}]_{1,1}, \quad f_{\nu}(\mathbf{b}) = [(\mathbf{G}(\mathbf{b}))^{-1}]_{2,2}. \quad (8)$$

V. JOINT RADAR COMMUNICATIONS BASED RESOURCE ALLOCATION

A. Problem Statement

Our aim is to optimize the joint radar communications performance of the vehicular network by using the sum SE in (3) and the CRBs in (8) as our design objectives. For characterization of performance trade-off between the two functionalities, the problem of resource allocation can be formulated as a weighted optimization of radar delay-Doppler estimation performance and communication SE as follows:

$$\begin{aligned} \text{minimize}_{\{\mathbf{b}^{(n)}\}_{n \in \mathcal{N}}} \quad & w_{\text{rad}} \sum_{n \in \mathcal{N}} [w_{\tau} f_{\tau}^{(n)}(\mathbf{b}^{(n)}) + (1 - w_{\tau}) f_{\nu}^{(n)}(\mathbf{b}^{(n)})] \\ & - (1 - w_{\text{rad}}) \sum_{n \in \mathcal{N}} g^{(n)}(\mathbf{b}^{(n)}) \end{aligned} \quad (9a)$$

$$\text{subject to} \quad \mathbf{b}^{(n)} \in \{0, 1\}^{N_f N_t}, \quad \forall n \in \mathcal{N} \quad (9b)$$

$$\mathbf{e}_{i_t}^T \mathbf{b}^{(n)} \leq 1, \quad \forall n \in \mathcal{N}, \forall i_t \in \mathcal{T} \quad (9c)$$

$$\sum_{n \in \mathcal{N}} \mathbf{b}^{(n)} \preceq \mathbf{1}_{N_f N_t} \quad (9d)$$

$$\mathbf{1}_{N_f N_t}^T \mathbf{b}^{(n)} \leq \kappa_n, \quad \forall n \in \mathcal{N} \quad (9e)$$

where $f_{\tau}^{(n)}(\mathbf{b}^{(n)})$ and $f_{\nu}^{(n)}(\mathbf{b}^{(n)})$ are the vehicle-specific versions of (8), $\mathbf{e}_{i_t} \in \mathbb{R}^{N_f N_t}$ is an all 0's vector except 1's at the indices between $i_t N_f + 1$ and $(i_t + 1) N_f$, $\mathbf{1}_N$ is an all 1's vector of size N , and κ_n is the upper bound on the number of blocks used by vehicle n , which is due to (i) power consumption requirements of vehicles and (ii) efficient usage of spectrum.

In (9), w_{τ} and $1 - w_{\tau}$ denote the preset weightings of delay and Doppler estimation accuracies, while w_{rad} and $1 - w_{\text{rad}}$ are weighting factors for radar and communication

objectives, with $0 \leq w_{\tau}, w_{\text{rad}} \leq 1$. In addition, the constraint (9c) guarantees that each vehicle occupies at most one time-frequency resource block over a block duration (imposed by ADC bandwidth), while the constraint (9d) ensures orthogonality of vehicles in the time-frequency domain. The problem (9) is a nonlinear integer programming problem with high computational complexity. In the following, we propose to relax the Boolean constraint in (9b) to obtain an efficiently solvable convex program.

B. Convexification of (9) via Boolean Relaxation

By introducing the slack variables $\beta_{\tau, n}$, $\beta_{\nu, n}$ and $\mathbf{A}^{(n)} \in \mathbb{S}_+^N$, where \mathbb{S}_+^N is the set of $N \times N$ symmetric positive semidefinite matrices, (9) can be rewritten as follows:

$$\begin{aligned} \text{minimize}_{\{\mathbf{b}^{(n)}, \mathbf{A}^{(n)}, \beta_{\tau, n}, \beta_{\nu, n}\}_{n \in \mathcal{N}}} \quad & w_{\text{rad}} \sum_{n \in \mathcal{N}} [w_{\tau} \beta_{\tau, n} + (1 - w_{\tau}) \beta_{\nu, n}] \\ & - (1 - w_{\text{rad}}) \sum_{n \in \mathcal{N}} (\mathbf{r}^{(n)})^T \mathbf{b}^{(n)} \end{aligned} \quad (10a)$$

$$\text{subject to} \quad \mathbf{G}^{(n)}(\mathbf{b}^{(n)}) \succeq [\mathbf{A}^{(n)}]^{-1}, \quad \forall n \in \mathcal{N} \quad (10b)$$

$$\text{diag}(\mathbf{A}^{(n)}) \preceq [\beta_{\tau, n}, \beta_{\nu, n}], \quad \forall n \in \mathcal{N} \quad (10c)$$

$$(9b) - (9e)$$

where $\mathbf{G}^{(n)}(\mathbf{b}^{(n)})$ is the vehicle-specific version of (7) and $\text{diag}(\cdot)$ represents the diagonal entries of a matrix. Based on the definition of $\mathbf{G}^{(n)}(\mathbf{b}^{(n)})$ in (7) and the Schur complement properties [12, Ch. A.5.5], the constraint (10b) can be equivalently reformulated as

$$\begin{bmatrix} (\mathbf{I}_2 \otimes \mathbf{b}^{(n)})^T \mathbf{J}_{11}^{(n)} - \mathbf{C}^{(n)} & \mathbf{I}_2 \\ \mathbf{I}_2 & \mathbf{A}^{(n)} \end{bmatrix} \succeq 0, \quad \forall n \in \mathcal{N} \quad (11a)$$

$$\begin{bmatrix} \mathbf{C}^{(n)} & (\mathbf{I}_2 \otimes \mathbf{b}^{(n)})^T \mathbf{J}_{12}^{(n)} \\ (\mathbf{J}_{12}^{(n)})^T (\mathbf{I}_2 \otimes \mathbf{b}^{(n)}) & (\mathbf{I}_2 \otimes \mathbf{b}^{(n)})^T \mathbf{J}_{22}^{(n)} \end{bmatrix} \succeq 0, \quad \forall n \in \mathcal{N} \quad (11b)$$

where we introduce the slack variables $\mathbf{C}^{(n)} \in \mathbb{S}_+^2$. We note that the equivalent problem then has a linear objective, Boolean constraints (9b), linear inequality constraints (9c)–(9e) and (10c), and linear matrix inequality (LMI) constraints (11). Via Boolean relaxation of (9b) to its convex hull $[0, 1]^{N_f N_t}$, the problem (10a) can be recast in a relaxed form that turns out to be an SDP and thus can be solved efficiently using off-the-shelf convex optimization tools [13]. With this relaxation, the continuous variables $\mathbf{b}^{(n)}$ can now be interpreted as *time-sharing factors* [14] such that vehicle n uses the block (i_f, i_t) for $M b_{i_f, i_t}^{(n)}$ symbols out of M symbols².

²This physical interpretation holds true under the assumption that the individual summands of MFIM elements in (12) and (13) have negligible variation across time dimension (i.e., symbol dimension m) within a time-frequency block compared to variation between different blocks.

VI. RESULTS

In this part, we evaluate the performance of the proposed joint radar communications resource allocation approach via simulations. We consider a scenario consisting of three vehicles with 2-D positions $\mathbf{x}_1 = [0 \ 0] \text{ m}$, $\mathbf{x}_2 = [10 \ 0] \text{ m}$ and $\mathbf{x}_3 = [25 \ 3] \text{ m}$, sharing a time-frequency resource with $f_c = 60 \text{ GHz}$, $W_S = 500 \text{ MHz}$ and $T_{\text{frame}} = 20 \text{ ms}$. We assume the existence of three communication links with transmit-receive pairs $\{(1, 2), (3, 1), (2, 3)\}$. The OFDM system parameters are set as $W_{\text{block}} = 50 \text{ MHz}$, $T_{\text{block}} = 2 \text{ ms}$, $\Delta_f = 500 \text{ KHz}$, $T = 2 \mu\text{s}$, $T_{\text{cp}} = 0.5 \mu\text{s}$, $K = 100$, $M = 800$, $N_f = N_t = 10$. The transmit powers $P_{i_f, i_t}^{(n)}[k]$ are taken to be uniform across all subcarriers, time-frequency blocks and vehicles, and the total power over a block is set to -20 dBm , while the noise spectral density N_0 is taken as $4.0038 \times 10^{-21} \text{ W/Hz}$. We simulate the radar channel gains according to radar range equation [15, Ch. 2.2] with typical vehicle RCS values (e.g., $[0, 5] \text{ dBsm}$) and 10 dBi antenna gains. The statistical CSIs $\sigma_{i_f}^{(n, \mathcal{R}(n))}[k]$ are assumed to be equal across subcarriers and generated based on the free-space path loss model [10, Ch. 2.3]. For the constraint (9e), we set $\kappa_n = 5$, $\forall n \in \mathcal{N}$.

Fig. 2 illustrates the radar-communication performance trade-off curves corresponding to the solution of the relaxed version of (10). By tuning the trade-off parameter w_{rad} , the vehicular network can transition between radar-optimal ($w_{\text{rad}} = 1$) and communication-optimal ($w_{\text{rad}} = 0$) operation regimes, depending on system requirements. As w_{rad} approaches 0, all trade-off curves asymptotically converge to the maximum SE that can be achieved in radar-free operation. In addition, range accuracy is more sensitive to changes in SE than velocity accuracy since the expression (2) varies only over frequency due to uniform subcarrier powers and time-invariant channel statistics over a frame duration T_{frame} . Moreover, it is observed that better Pareto-optimal solutions can be achieved with higher RCS values, as expected. This suggests, for example, that data rates can be increased in an environment with large RCS objects without changing radar accuracy constraints.

To investigate resource allocation results in the time-frequency domain, Fig. 3 demonstrates the optimal time-sharing factors $\mathbf{b}^{(n)}$ for different weighting factors w_{rad} and w_{τ} , along with the SE $\mathbf{r}^{(n)}$ of the three links over the frequency blocks. First, Fig. 3(b) shows the communication-optimal allocation, which complies with the SE plots in Fig. 3(a) (i.e., each link is assigned the frequency block with the highest data rate). Second, Fig. 3(c), Fig. 3(d) and Fig. 3(e) illustrate radar-optimal time-frequency allocations. It is observed that the delay-optimal solution focuses all the available power on the edges of the frequency spectrum to maximize the root mean square (RMS) bandwidth, while the Doppler-optimal solution utilizes the edges of the time window to maximize the RMS envelope [16]. On the other hand, the delay-Doppler-optimal allocation occupies the corners of the available time-frequency region as a compromise between the

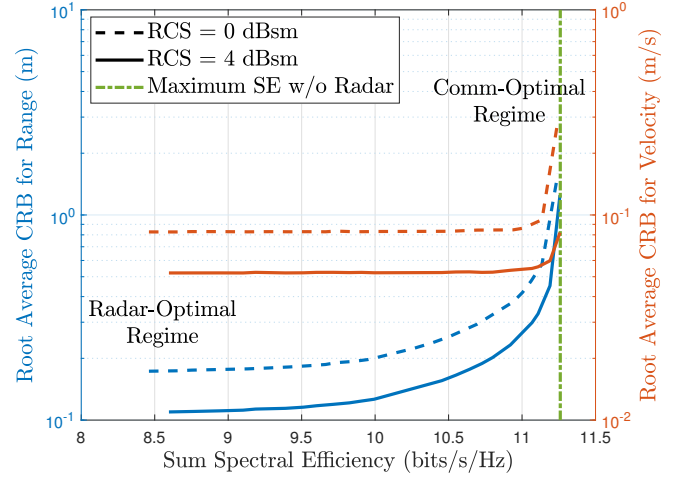


Fig. 2. Radar-communication trade-off curves for multiple target RCS values along with the asymptotic SE line in radar-free operation, where root average CRBs on range and velocity estimation (with $w_{\tau} = 0.5$) are plotted against sum SE as w_{rad} varies over the interval $[0, 1]$ in the relaxed version of (10). Due to time-invariant, frequency-selective channel statistics and uniform subcarrier powers, the trade-off on the radar side is mainly related to the accuracy of range rather than that of velocity.

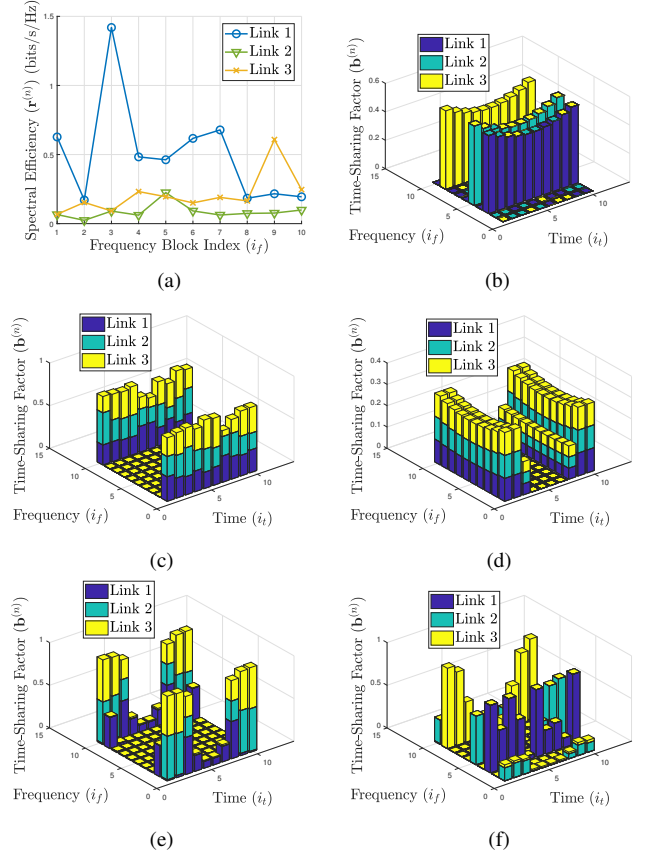


Fig. 3. Optimal time-frequency resource allocation results obtained from the solution of the relaxed version of (10). (a) Time-invariant block SE values $\mathbf{r}^{(n)}$ in (3) over different frequency blocks. (b) Communication-optimal resource allocation with $w_{\text{rad}} = 0$. (c) Radar delay-optimal resource allocation with $w_{\text{rad}} = 1$ and $w_{\tau} = 1$. (d) Radar Doppler-optimal resource allocation with $w_{\text{rad}} = 1$ and $w_{\tau} = 0$. (e) Radar delay-Doppler-optimal resource allocation with $w_{\text{rad}} = 1$ and $w_{\tau} = 0.5$. (f) Weighted radar-communication resource allocation with $w_{\text{rad}} = 0.8$ and $w_{\tau} = 0.5$.

delay- and Doppler-optimal solutions. Finally, Fig. 3(f) shows the weighted radar-communication design, which reflects both delay-Doppler optimality in Fig. 3(e) and link qualities in Fig. 3(a).

VII. CONCLUSIONS

We consider a centralized V2V time-frequency resource allocation scheme for stepped-carrier OFDM based vehicular networks, where each vehicle is assigned a number of OFDM time-frequency resource blocks with the aim of improved overall joint radar communications performance. To investigate performance trade-offs, a nonlinear integer programming problem with Boolean resource selection variables is formulated to optimize weighted average of radar estimation performance and communication spectral efficiency. Simulation results reveal the compromise between the two tasks, indicating Pareto-optimal solutions for different target RCS values. In addition, the interplay between delay-optimal, Doppler-optimal and communication-optimal designs is illustrated in the time-frequency domain. We plan to extend this study by incorporating downlink joint radar communications into the existing resource allocation problem.

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APPENDIX A

ELEMENTS OF THE MODIFIED FISHER INFORMATION MATRIX

We define, for $i_f \in \mathcal{F}$ and $i_t \in \mathcal{T}$,

$$\vartheta[i_f + N_f i_t] \quad (12a)$$

$$= -j2\pi \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] (f_c + i_f W_{\text{block}} + k\Delta_f) \quad (12b)$$

$$\tilde{\vartheta}[i_f + N_f i_t] \quad (12b)$$

$$= 4\pi^2 \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] (f_c + i_f W_{\text{block}} + k\Delta_f)^2$$

$$\varphi[i_f + N_f i_t] \quad (12c)$$

$$= -j2\pi \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] f_c (i_t T_{\text{block}} + (m+1)T_s)$$

$$\tilde{\varphi}[i_f + N_f i_t] \quad (12d)$$

$$= 4\pi^2 \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] f_c^2 (i_t T_{\text{block}} + (m+1)T_s)^2$$

$$\xi[i_f + N_f i_t] \quad (12e)$$

$$= 4\pi^2 \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] f_c (f_c + i_f W_{\text{block}} + k\Delta_f) \\ \times (i_t T_{\text{block}} + (m+1)T_s)$$

and

$$p[i_f + N_f i_t] = \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} P_{i_f, i_t}[k, m] \quad (13)$$

Then, the submatrices constituting the MFIM in (6) are derived as follows:

$$\mathbf{J}_{11} = \frac{2|\alpha|^2}{\sigma^2} \begin{bmatrix} \tilde{\vartheta} & \xi \\ \xi & \tilde{\varphi} \end{bmatrix} \in \mathbb{R}^{2N_f N_t \times 2} \quad (14a)$$

$$\mathbf{J}_{12} = \frac{2}{\sigma^2} \begin{bmatrix} \Re\{\alpha^* \vartheta\} & -\Im\{\alpha^* \vartheta\} \\ \Re\{\alpha^* \varphi\} & -\Im\{\alpha^* \varphi\} \end{bmatrix} \in \mathbb{R}^{2N_f N_t \times 2} \quad (14b)$$

$$\mathbf{J}_{22} = \frac{2}{\sigma^2} \begin{bmatrix} \mathbf{p} & \mathbf{0}_{N_f N_t} \\ \mathbf{0}_{N_f N_t} & \mathbf{p} \end{bmatrix} \in \mathbb{R}^{2N_f N_t \times 2} \quad (14c)$$

where $\mathbf{0}_N$ is an all 0's vector of size N .

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