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Joint 3D User and 6D Hybrid Reconfigurable Intelligent Surface Localization

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Abstract—The latest assessments of the emerging technologies for reconfigurable intelligent surfaces (RISs) have indicated the concept's significant potential for localization and sensing, either as individual or simultaneously realized tasks. However, in the vast majority of those studies, the RIS state (i.e., its position and rotation angles) is required to be known a priori. In this paper, we address the problem of the joint three-dimensional (3D) localization of a hybrid RIS (HRIS) and a user. The most cost- and power-efficient hybrid version of an RIS is equipped with a single reception radio-frequency chain and meta-atoms capable of simultaneous reconfigurable reflection and sensing. This dual functionality is controlled by adjustable power splitters embedded at each hybrid meta-atom. Focusing on a downlink scenario where a multi-antenna base station transmits multicarrier signals to a user via an HRIS, we propose a multistage approach to jointly estimate the metasurface's 3D position and 3D rotation matrix (i.e., 6D parameter estimation) as well as the user's 3D position. Our simulation results verify the validity of the proposed estimator via extensive comparisons of the root-mean-square error of the state estimations with the Cramér-Rao lower bound (CRB), which is analytically derived. Furthermore, it is showcased that there exists an optimal hybrid reconfigurable intelligent surface (HRIS) power splitting ratio for the desired multi-parameter estimation problem. We also study the robustness of the proposed method in the presence of scattering points in the wireless propagation environment.

Index Terms—3D positioning, 3D orientation, parametric channel estimation, hybrid reconfigurable intelligent surface, sensing, synchronization, positioning error bound.

I. INTRODUCTION

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RECONFIGURABLE intelligent surfaces (RISs) are recently being extensively studied as an enabling tech-ECONFIGURABLE intelligent surfaces (RISs) are renology for the upcoming sixth generation (6G) of wireless systems [1], [2]. An RIS is a planar surface made of subwavelength unit cells with controllable electromagnetic (EM) properties [3], [4]. In essence, RISs can modify wave characteristics such as phase, amplitude, frequency, and even polarization, offering radio propagation control [5]–[7]. Smart wireless environments can be achieved via this characteristic of RISs, which provides coverage extension and localization, as well as sensing capabilities [8], [9]. Hence, RISs are expected to be the vital enabler for the 6G of wireless systems [10], [11], where joint communications and localization is expected to aid various use cases [12], such as connected robotics, autonomous systems, and other immersive applications [13]. There have been several studies on RISs' utility in radio localization by developing localization algorithms or deriving Cramér-Rao lower bound (CRB), see, e.g., [14]–[29]. In those works, RISs have been successfully deployed for user equipment (UE) radio localization in two different general scenarios. In the first scenario, except for the base station (BS), the RIS acts as an anchor with a known state, i.e., location and orientation. These kind of systems are known as *RIS-aided* or *RIS-enabled localization* [30], and exploit reflected signals from RISs to improve or assist UE localization. In the second scenario, a UE can use one or more RISs to enable its localization, where the RISs' state is unknown and needs to be estimated. This problem is known as *RIS localization*, which one can see as a *bi-static sensing* or a calibration problem [26].

RIS-aided UE localization has been intensely studied in recent years, ranging from two-dimensional (2D) to 3D scenarios under either far field (FF) or near field (NF) operating conditions, as well as indoor and outdoor scenarios [14]– [25], [31]–[37]. UE localization under the NF condition via analyzing the CRB has been studied in [14] for passive RIS, and for hybrid RIS (HRIS) with line of sight (LOS) blockage in [18]. Moreover, the possibility of UE positioning under non-line-of-sight (NLOS) harsh propagation conditions has been shown [24], [32], in which the RIS is equipped with a large number of reflecting elements. In [20], the authors showed that the Fisher information matrix (FIM) on the UE position estimation, in the case it operates in the NF regime, quadratically increases with the size of the RIS. Furthermore, a UE localization algorithm based on compressed sensing techniques for an uplink NF scenario was presented in [21]. 3D UE localization and synchronization in the FF scenario has been studied in [15], [16], where UE mobility and the spatial-wideband effect were taken into account. In [19], [29], multiple RISs were adopted for UE localization. In [19], the

RISs modulate an impinging unmodulated carrier and timedifference-of-arrival is calculated at the receivers to estimate the UE location. The localization approach in [29] considered narrowband transmission and was based in angle-of-arrival (AOA) estimation. In [25], the potential of using an RIS for UE orientation estimation, besides its location estimation, was studied via a CRB analysis.

The problem of RIS localization, which assumes that the RIS state (i.e., position and/or orientation) is unknown, has been rarely discussed. While the lack of knowledge of the RIS position and orientation generally does not affect RIS-aided communication, it prevents RIS-aided UE localization [38]. RIS position or orientation may be unknown for a number of reasons, including poor calibration, lack of knowledge of the environment map in which the RIS is placed, or due to mobility of the RIS itself [39], [40]. The relevant works are only [26], [28] that focused on a passive RIS. In these works, the locations of the transmitters and receivers are assumed to be known, which requires some overhead for infrastructure calibration. The estimation of AOA and angle-of-departure (AOD) separately at the RIS offers a promising way for RIS localization jointly with the localization of the transmitter or the receiver [27], reducing the aforementioned calibration overhead. However, one cannot separately estimate the AOA and AOD at a passive RIS. Adding sensing capability to an RIS can be a promising solution to overcome this challenge [27], which was first proposed in [41] for individual channel estimation. This version of an RIS was then extended in [42]– [44] to a HRIS that is capable of simultaneous reflection and sensing. According to this RIS hardware architecture, waveguides feed the incident signals at each hybrid metaatom to reception (RX) radio frequency (RF) chains, which are connected to a baseband unit. This reception mechanism effectively acts as an analog combiner whose phase shifts can be dynamically optimized [42]. A HRIS-assisted orthogonal time-frequency-space system has been proposed, leveraging the HRIS capability to fully absorb the pilot signal for UE-HRIS channel estimation through a proposed transmission scheme $[45]$ ¹. Very recently, $[18]$ studied UE localization in an NF scenario, considering multiple RX RF chains at the HRIS and that its state is precisely known. HRIS-assisted MIMO radar-communication systems have been investigated, where the HRIS simultaneously reflected communications signals and received radar echos [46]. However, HRISs with a single RX RF chain in localization problems, where their states are unknown, have not yet been investigated.

In this paper, we extend our recent work in [27], which addressed joint 2D UE and HRIS localization, to joint 3D UEs and HRIS localization under FF conditions, including the 3D rotation matrix estimation for the HRIS. The main contributions of this paper are summarized as follows.

• We devise a multi-stage algorithm for joint multipleinput-single-output (MISO) 3D localization and synchronization of a UE and an HRIS under FF scenarios. In the first step, we estimate the geometric parameters of

TABLE I: Notations.

Parameter	Symbol*/dimension	
Combining vector at the HRIS	$\mathbf{c}_t \in \overline{\mathbb{C}^{M_R}}$	
Reflection phase shift vector at the HRIS	$\pmb{\gamma}_t \in \mathbb{C}^{\mathrm{M_R}}$	
Beamforming vector at the BS	$\mathbf{f}_t\,\in \mathbb{C}^{\mathrm{M}_{\mathrm{B}}}$	
Received signals at the HRIS	$\mathbf{y}_{\text{R}\,,t}\in\mathbb{C}^K$	
Received signals at the UE	$\mathbf{y}_{\mathrm{U},t} \in \mathbb{C}^K$	
Received signals at the UE from the BS via LOS path	$\mathbf{y}_{\text{BU},t} \in \mathbb{C}^K$	
Received signals at the UE from the BS via the HRIS	$\mathbf{y}_{{\rm BRU},t} \in \mathbb{C}^{K}$	
Interference signals at the UE in BS-UE path	$\mathbf{y}_{{\rm BU},t}^{s} \in \mathbb{C}^{K}$	
Interference signals at the UE in BS-HRIS-UE path	$\mathbf{y}_{{\scriptscriptstyle\mathrm{BRU}},t}^{s} \in \mathbb{C}^{K}$	
AOD from the BS to the UE	$\pmb{\theta}_\mathrm{BU} \in \mathbb{R}^2$	
AOD from the BS to the HRIS	$\pmb{\theta}_\text{\tiny BR} \in \mathbb{R}^2$	
AOD from the HRIS to the UE	$\pmb{\theta}_\mathrm{RU} \in \mathbb{R}^2$	
AOA to the HRIS from the BS	$\boldsymbol{\phi}_{\textsc{rb}} \in \mathbb{R}^2$	
AOD from the HRIS to the j th SP	$\boldsymbol{\theta}_{\text{RS},j} \in \mathbb{R}^2$	
AOD from the BS towards the <i>i</i> th SP	$\pmb{\theta}_{\mathtt{BS},i} \in \mathbb{R}^2$	
The steering vector at the BS	$\mathbf{a}_{\textsc{b}}(\cdot) \in \mathbb{C}^{M_{\textsc{b}}}$	
The steering vector at the HRIS	$\mathbf{a}_\mathrm{R}(\cdot) \in \mathbb{C}^{M_\mathrm{R}}$	
Delay steering vector	$\mathbf{d}(\cdot) \in \mathbb{C}^K$	
Channel parameters vector	$\pmb{\zeta} \in \mathbb{R}^{\bar{1}7}$	
State parameters vector	$\pmb{\zeta}_s \in \mathbb{R}^{17}$	
Observation matrix at the HRIS	$\mathbf{Y}_\text{R} \in \mathbb{C}^{K \times T}$	
Observation matrix at the UE	$\mathbf{Y}_{\text{U}} \in \mathbb{C}^{K \times T}$	

 $*$ The index t associated with certain vectors indicates the specific time instant. **Simulation parameters are provided in Table II.

- the associated channels, i.e., delay, gain, AOA/AOD at HRIS, and AOD at the BS. The AOA/AOD estimation at the HRIS is enabled by its single RX RF chain. Using these estimations at a further stage, we calculate the 3D position and clock bias of the UE and the HRIS. At the final step of the proposed approach, we make use of the positions' estimates, the AOA at the HRIS from the BS and the AOD from the HRIS to the UE to estimate the 3D rotation matrix of the HRIS.
- We investigate the role of several system parameters (the transmit power at the BS, the power splitting ratio at the HRIS, and the presence of scatterers) on the error of the proposed estimation approach via extensive simulations, and through comparisons with the estimator's CRB, which is derived for this purpose. In this investigation, we consider HRIS phase profiles from the discrete-Fouriertransform (DFT). Our simulation results showcase the efficiency of the proposed estimation algorithm, which attains the corresponding CRB at high transmit power levels. The critical role of the HRIS power splitting ratio on the localization performance is also unveiled. We finally show that the proposed approach is robust to the presence of the scattering points (SPs).

The rest of this paper is organized as follows. In Section II, the system and signal models are described, while the Fisher information of the estimations is detailed in Section III. The proposed estimation algorithm is presented in Section IV. In Section V, we numerically evaluate the root-mean-squareerror (RMSE) of the parameters' estimation and compare it with the respective CRBs. Section VI concludes the paper.

Notation: Vectors and matrices are indicated by lowercase and uppercase bold letters, respectively. Unless otherwise stated, all vectors are columns. The element in the i -th row and j-th column of matrix **A** is denoted by $[\mathbf{A}]_{i,j}$ and $\det(\mathbf{A})$ returns A's determinant. The sub-index $i : j$ determines

¹In contrast to the study proposed in [45], our system allows the HRIS to both absorb and reflect signals simultaneously from either the UE or the BS.

Fig. 1: The considered wireless system comprising a multi-antenna BS, a single-antenna UE, and a single-RX-RF HRIS. The 3D location of the UE and the 6D state of the HRIS are unknown.

all the elements between i and j . The complex conjugate, Hermitian, transpose, and Moore–Penrose inverse operators are represented by $(.)^*, (.)^{\mathsf{H}}, (.)^{\mathsf{T}},$ and $(.)^{\dagger}$, respectively. $\|\cdot\|$ calculates the norm of vectors or Frobenius norm of matrices. ⊙ and ⊗ indicate the element-wise and Kronecker products, respectively. $\mathbb R$ and $\mathbb C$ are the real and complex number sets, $\Re\{\cdot\}$ and $\Im\{\cdot\}$ give the real and imaginary parts of a complex number, and $j = \sqrt{-1}$. $\mathbf{1}_K$ and $\mathbf{0}_K$ are column vectors with length K comprising all ones and zeros, respectively. The functions atan2 (y, x) and acos(x) are the four-quadrant inverse tangent and inverse cosine functions, respectively. Before describing the system and signal model, we present the important notations used in this document in Table I.

II. SYSTEM AND SIGNAL MODELS

In this section, we introduce the considered HRISempowered system model as well as the models for the received signals and the wireless channel that will be deployed for the proposed localization approach.

A. System Setup

Consider the wireless system scenario in Fig. 1 consisting of one $M_{\rm B}$ -antenna BS with a known location ${\bf p}_{\rm B} \in \mathbb{R}^3$, one single-antenna UE with an unknown location $\mathbf{p}_U \in \mathbb{R}^3$, and an HRIS with unknown location $\mathbf{p}_R \in \mathbb{R}^3$ and unknown orientation.² We consider the downlink scenario where the BS sends T orthogonal frequency division multiplexing (OFDM) symbols over time via K subcarriers. We assume that all the associated channels remain constant during each transmission time slot. To model the HRIS orientation, we use a 3×3 rotation matrix R that determines local coordinate frames, which belongs in the special orthogonal group SO(3), i.e., orthogonal matrices with unit-valued determinant. In particular, we define a reference orientation where the axes are in the same direction as those of the global coordinate frame, as shown in Fig. 1. We assume that the global coordinate system is aligned with the BS local coordinate system. Accordingly, we can express the HRIS rotation matrix as follows:

$$
\mathbf{R} = \mathbf{R}_z(\alpha) \mathbf{R}_y(\beta) \mathbf{R}_x(\gamma), \tag{1}
$$

where $\mathbf{R}_z(\alpha)$, $\mathbf{R}_y(\beta)$, and $\mathbf{R}_x(\gamma)$ represent the rotation matrices w.r.t. z -axis, y -axis, and x -axis, respectively, and are expressed as follows:

$$
\mathbf{R}_z(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix},
$$
 (2a)

$$
\mathbf{R}_{y}(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix},
$$
 (2b)

$$
\mathbf{R}_x(\gamma) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \gamma & -\sin \gamma \\ 0 & \sin \gamma & \cos \gamma \end{bmatrix} . \tag{2c}
$$

The direction vectors from the HRIS to the BS and the UE in the local coordinate system can be respectively obtained as:

$$
\mathbf{q}_{RB} = \mathbf{R}^\top (\mathbf{p}_B - \mathbf{p}_R) / ||\mathbf{p}_B - \mathbf{p}_R||, \tag{3a}
$$

$$
\mathbf{q}_{\text{RU}} = \mathbf{R}^\top (\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}})/\|\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}}\|.\tag{3b}
$$

Similarly, we respectively write the direction vectors from the BS to the HRIS and the UE in the BS coordinate system as:

$$
\mathbf{q}_{\text{BR}} = (\mathbf{p}_{\text{R}} - \mathbf{p}_{\text{B}})/\|\mathbf{p}_{\text{R}} - \mathbf{p}_{\text{B}}\|, \tag{4a}
$$

$$
\mathbf{q}_{BU} = (\mathbf{p}_U - \mathbf{p}_B) / ||\mathbf{p}_U - \mathbf{p}_B||. \tag{4b}
$$

Moreover, the HRIS and UE are assumed unsynchronized with the BS, leading to the unknown clock biases b_R and b_U at the HRIS and UE, respectively, with respect to the BS. Therefore, in addition to the HRIS location and UE position, the latter clock bias components need to be estimated.

The BS is assumed equipped with a uniform planar array (UPA) with $M_{\rm B} = M_{\rm B}^r \times M_{\rm B}^c$ elements.³ The element in each rth row $(r \in \{0, ..., M_{\rm B}^r - 1\})$ and sth column $(s \in \{0, ..., M_{\rm B}^c - 1\})$ has the position $\mathbf{q}_{r,s} = [d(2r - M_{\rm B}^r +$ $(1)/2$, $(0, d(2s - M_{\rm B}^{\rm c} + 1)/2)]^{\rm T}$ in the local coordinate system of the BS, with d being the spacing between the elements. Similarly, the HRIS is a UPA with $M_{\rm R} = M_{\rm R}^r \times M_{\rm R}^c$ unit elements, all attached via a dedicated waveguide to a single RX RF chain [42], enabling simultaneous tunable reflection

³Using a single-antenna BS or a BS with a uniform linear array will make the targeted estimation problem infeasible, due to the fact that there will not be enough measurements for this task. However, when deploying a UPA at the BS, four additional measurements are feasible: a 2D AOD measurement at the BS from the UE and the HRIS. For instance, using a single-antenna BS, we will have seven measurements, i.e., 2D AOA and 2D AOD at the RIS from/to the BS/UE and three TOAs from the BS-UE, BS-HRIS-UE, and BS-HRIS links, and eleven unknown states estimate: the 3D UE position, the 3D HRIS position, and the 3D HRIS orientation, leading to an unsolvable estimation problem. To treat this infeasibility situation, more anchor nodes need to added [28]. For example, at least two single-antenna BSs will make the scenario feasible, which results in a different setup.

²One can extend the scenario to the multi-user case, which would improve the localization performance. As the positioning method is working in the DL, one can locate other user, and this would actually improve the overall performance because the measurement from all users would contribute to the determination of the HRIS state.

and sensing of impinging signals. Accordingly, each (n, m) th element $(n \in \{0, ..., M_{R}^{r} - 1\})$ and $m \in \{0, ..., M_{R}^{c} - 1\})$ of the HRIS has the position $\mathbf{q}_{n,m} = [d(2n - M_{\rm R}^r +$ $(1)/2$, $0, d(2m - M_{\rm R}^c + 1)/2$][⊤] in the local coordinate system of the HRIS. We assume for both the BS and HRIS that $d \leq \lambda/2$ with λ being the carrier frequency wavelength. We also assume that the HRIS is larger than the BS, following the literature in RIS-aided communications [47], [48]. This is because manufacturing the RIS is more cost-effective and demands less analog or digital hardware per antenna element in contrast to a BS [49]. We further assume that the UE operates in the far-field range of the BS and the $HRIS⁴$. Our final assumption is that the HRIS and the UE share their observations with a fusion center (FC) via a reliable link [51]. The FC is responsible for carrying out the joint location estimation of the UE and HRIS, which we will be presented in the sequel.

B. Signal and Channel Models

The HRIS is capable of simultaneously sensing and reflecting its impinging signals. To this end, it possesses $M_{\rm R}$ identical power splitters within its structure to divide the received signal power at each meta-atom into two parts [42]–[44]: one for reflection and the other for sensing/reception. For the latter operation, the HRIS adopts a phase shifting network to feed a portion of the impinging signals on its elements to the single RX RF chain. Mathematically, this phase shifting network applies a combining vector modeled by $c_t \in \mathbb{C}^{M_R}$ with $|[\mathbf{c}_t]_i| = 1 \ \forall \ i = 1, \dots, M_{R}$ during each time interval t. Each i-th HRIS unit element also reflects the remaining portion of its impinging signal at each time t , which is modeled by the phase shift $[\gamma_t]_i$ with $\gamma_t \in \mathbb{C}^{M_{\rm R}}$ and $|[\gamma_t]_i| = 1$. We make the assumption that the FC has complete knowledge about the HRIS combining vector and phase profile. We further assume that the multi-antenna BS applies the DFT codebook for its beamforming vector $f{f} \in \mathbb{C}^{M_B}$ at each time instant t, and transmits unit-power symbols.

Under the above assumptions, after cyclic prefix removal and fast Fourier transform (FFT) application, the received signals at the HRIS and the UE at each time instant t , which are respectively denoted by the vectors $y_{R,t} \in \mathbb{C}^K$ and $y_{U,t} \in \mathbb{C}^K$, can be expressed as follows:⁵

$$
\mathbf{y}_{\text{R},t} = g_{\text{BR}} \sqrt{\rho P_{\text{B}}} \mathbf{d}(\tau_{\text{BR}}) \mathbf{c}_{t}^{\top} \mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_{t} + \mathbf{n}_{\text{R},t}, \quad (5a)
$$

$$
\mathbf{y}_{U,t} = \mathbf{y}_{BU,t} + \mathbf{y}_{BRU,t} + \mathbf{y}_{BU,t}^s + \mathbf{y}_{BRU,t}^s + \mathbf{n}_{U,t},
$$
 (5b)

where g_{BR} denotes the unknown complex gain of the BS-HRIS link, P_B is the BS transmit power, ρ represents the common power splitting ratio at each hybrid meta-atom used for the sensing operation, and $n_{R,t} \in \mathbb{C}^K$ and $n_{U,t} \in \mathbb{C}^K$ indicate the effect of additive thermal noise at the HRIS

and the UE, respectively, each modeled as a vector with zero-mean circularly-symmetric independent and identically distributed Gaussian elements with variance σ^2 . The model can be generalized to accommodate unequal power splitting [44], but such a generalization is not considered in the current work. In (5b), $\mathbf{y}_{\text{BU},t} \in \mathbb{C}^K$ and $\mathbf{y}_{\text{BRU},t} \in \mathbb{C}^K$ represent the received signals at time t at the UE from the BS through their direct LOS path and through the HRIS, respectively, while $\mathbf{y}_{\text{\tiny{BU}},t}^s \in \mathbb{C}^K$ and $\mathbf{y}_{\text{\tiny{BRU}},t}^s \in \mathbb{C}^K$ denote the received interference signals⁶ at time t at the UE in the BS-UE and BS-HRIS-UE paths, respectively. The latter four contributions at the UE received signal in (5b) are given by:

$$
\mathbf{y}_{\text{BU},t} = g_{\text{BU}} \sqrt{P_{\text{B}}} \mathbf{d}(\tau_{\text{BU}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BU}}) \mathbf{f}_{t},
$$
\n
$$
\mathbf{y}_{\text{new}} = g_{\text{new}} \sqrt{(1-\rho) P_{\text{B}}} \mathbf{d}(\tau_{\text{new}}) \mathbf{a}^{\top}(\boldsymbol{\theta}_{\text{new}}) \text{diag}(\boldsymbol{\gamma})
$$
\n(6a)

$$
\mathbf{y}_{\text{BRU},t} = g_{\text{BRU}} \sqrt{(1 - \rho) P_{\text{B}}} \mathbf{d}(\tau_{\text{BRU}}) \mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RU}}) \operatorname{diag}(\boldsymbol{\gamma}_{t})
$$

$$
\mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_{t}, \qquad (6b)
$$

 \overline{N}

$$
\mathbf{y}_{\text{BU},t}^s = \sum_{i=0}^{N_{\text{BU}}} g_{\text{BSU},i} \sqrt{P_{\text{B}}} \mathbf{d}(\tau_{\text{BSU},i}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BS},i}) \mathbf{f}_t, \tag{6c}
$$

$$
\mathbf{y}_{\text{BRU},t}^{s} = \sum_{j=0}^{N_{s_1}} g_{\text{BRSU},j} \sqrt{(1-\rho)P_{\text{B}}}\mathbf{d}(\tau_{\text{BRSU},j}) \mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RS},j}) \text{diag}(\boldsymbol{\gamma}_{t})
$$

$$
\mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_{t}, \qquad (6d)
$$

where N_{s_0} and N_{s_1} indicate the number of SPs in the BS-UE and HRIS-UE links, respectively. In addition, g_{BH} and g_{BRU} denote the unknown complex gains of the BS-UE and BS-HRIS-UE links, respectively, while $g_{\text{bsU},i}$ and $g_{\text{bsU},j}$ are respectively the unknown complex gains of the $BS-SP_i-UE$ and BS-HRIS-SP_j-UE links. As previously mentioned, the effect of the reflection of the BS-SP_j-HRIS link via the HRIS on the received signal strength at the UE is neglected in (6d). Finally, $d(\cdot)$ appearing in (5a) and (6a)– (6d) represents the delay steering vector, which is defined as:

$$
\mathbf{d}(\tau) \triangleq \left[1, e^{-j2\pi\Delta_f \tau}, \dots, e^{-j2\pi(K-1)\Delta_f \tau}\right]^\top \in \mathbb{C}^K, \quad (7)
$$

where Δ_f denotes the sub-carrier spacing. Under our lackof-synchronization assumption between the BS and the other network nodes, the propagation delay for all associated links is given by:

$$
\tau_{\text{BR}} = \frac{d_{\text{BR}}}{c} + b_{\text{R}}, \tau_{\text{BRU}} = \frac{d_{\text{BR}} + d_{\text{RU}}}{c} + b_{\text{U}}, \tag{8a}
$$

$$
\tau_{\text{BSU},i} = \frac{d_{\text{BS},i} + d_{\text{US},i}}{c} + b_{\text{U}}, \tau_{\text{BU}} = \frac{d_{\text{BU}}}{c} + b_{\text{U}},\qquad(8b)
$$

$$
\tau_{\text{BRSU},j} = \frac{d_{\text{BR}} + d_{\text{RS},j} + d_{\text{US},j}}{c} + b_{\text{U}},\tag{8c}
$$

where $d_{\text{BR}} \triangleq \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{R}}\|$, $d_{\text{BU}} \triangleq \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{U}}\|$, $d_{\text{RU}} \triangleq \|\mathbf{p}_{\text{R}} - \mathbf{p}_{\text{U}}\|$, $d_{{\rm BS},i}\triangleq \|\mathbf{p_B}-\mathbf{p}_{i,s}\|, d_{{\rm RS},j}\triangleq \|\mathbf{p_R}-\mathbf{p}_{j,s}\|, d_{{\rm US},j}\triangleq \|\mathbf{p_U}-\mathbf{p}_{j,s}\|,$ and $d_{\text{us},i} \triangleq ||\mathbf{p}_{\text{U}} - \mathbf{p}_{i,s}||$ with c being the speed of light. $\mathbf{p}_{i,s}$ and $\mathbf{p}_{i,s}$ denote the position of the *i*th and *j*th SP positions in the BS-UE and HRIS-UE links, respectively.

In (5) and (6), θ_{BR} and θ_{BU} respectively represent the AODs from the BS towards the HRIS and the UE, based on the BS

⁶To reduce the complexity in the derivation of the targeted location estimator and its CRB, we ignore the effects of SPs in the environment on the received signals at the HRIS and UE.

⁴The far-field region, which is usually defined as the range greater than the Fraunhofer distance $2D^2/\lambda$ [50]. Here, D is the greatest dimension of the HRIS or the BS.

⁵We assume that there are no scatterers in the BS-HRIS link. This holds from the common placement assumption of (H)RISs in strong LOS conditions from the BS, and mainly close to it [2], [3], [30], [52]. We can also envisage scenarios where the BS and the HRIS are elevated while the UE is located close to the ground.

local coordinate system. These vectors are respectively along the directions of \mathbf{q}_{BR} and \mathbf{q}_{BU} in (4), and can be expressed as:

$$
\begin{aligned} \boldsymbol{\theta}_{\scriptscriptstyle\mathrm{BR}} &= [\theta_{\scriptscriptstyle\mathrm{BR}}^{(az)}, \theta_{\scriptscriptstyle\mathrm{BR}}^{(el)}]^\top = [\text{atan2}([\mathbf{q}_{\scriptscriptstyle\mathrm{BR}}]_2, [\mathbf{q}_{\scriptscriptstyle\mathrm{BR}}]_1), \text{acos}([\mathbf{q}_{\scriptscriptstyle\mathrm{BR}}]_3)]^\top, \\ \boldsymbol{\theta}_{\scriptscriptstyle\mathrm{BU}} &= [\theta_{\scriptscriptstyle\mathrm{BU}}^{(az)}, \theta_{\scriptscriptstyle\mathrm{BU}}^{(el)}]^\top = [\text{atan2}([\mathbf{q}_{\scriptscriptstyle\mathrm{BU}}]_2, [\mathbf{q}_{\scriptscriptstyle\mathrm{BU}}]_1), \text{acos}([\mathbf{q}_{\scriptscriptstyle\mathrm{BU}}]_3)]^\top. \end{aligned} \tag{9b}
$$

Similarly, $\theta_{\text{\tiny{RU}}}$ and $\phi_{\text{\tiny{RB}}}$ represent respectively the AOD from the HRIS to the UE and the AOA to the HRIS from the BS, both expressed with respect to the HRIS local coordinate system. In fact, $\theta_{\text{\tiny RU}}$ and $\phi_{\text{\tiny RB}}$ are in the directions of $\mathbf{q}_{\text{\tiny RU}}$ and q_{RB} in (3), respectively, and are given as follows:

$$
\boldsymbol{\phi}_{_{RB}} = [\phi_{_{RB}}^{(az)}, \phi_{_{RB}}^{(el)}]^\top = [\text{atan2}([\mathbf{q}_{_{RB}}]_2, [\mathbf{q}_{_{RB}}]_1), \text{acos}([\mathbf{q}_{_{RB}}]_3)]^\top, \n\boldsymbol{\theta}_{_{RU}} = [\theta_{_{RU}}^{(az)}, \theta_{_{RU}}^{(el)}]^\top = [\text{atan2}([\mathbf{q}_{_{RU}}]_2, [\mathbf{q}_{_{RU}}]_1), \text{acos}([\mathbf{q}_{_{RU}}]_3)]^\top. \n\tag{10b}
$$

In the same way, $\theta_{\text{RS},j}$ represents the AOD from the HRIS to the jth SP, based on the HRIS local coordinate system, while $\theta_{BS,i}$ denotes the AOD from the BS towards the *i*th SP with respect to the BS local coordinate system.

Finally, in (5) and (6), $\mathbf{a}_{\scriptscriptstyle{B}}(\cdot) \in \mathbb{C}^{\dot{M}_{\scriptscriptstyle{B}}}$ and $\mathbf{a}_{\scriptscriptstyle{R}}(\cdot) \in \mathbb{C}^{M_{\scriptscriptstyle{R}}}$ represent the steering vectors at the BS and the HRIS, respectively, and both can be expressed in the form $\mathbf{a}(\psi) \triangleq \mathbf{a}_r(\psi) \otimes \mathbf{a}_c(\psi)$, where each *n*-th element of $\mathbf{a}_r(\cdot)$ and $\mathbf{a}_c(\cdot)$ is defined as:

$$
[\mathbf{a}_r(\boldsymbol{\psi})]_n = e^{-\jmath \frac{2\pi n d}{\lambda} \sin[\boldsymbol{\psi}]_{\text{el}} \cos[\boldsymbol{\psi}]_{\text{az}}},\tag{11a}
$$

$$
[\mathbf{a}_c(\boldsymbol{\psi})]_n = e^{-\jmath \frac{2\pi n d}{\lambda} \cos[\boldsymbol{\psi}]_{\text{el}}},\tag{11b}
$$

where ψ denotes the AOA/AOD at the HRIS or AOD at the BS. It implies that one can compute the steering vector at the BS or the HRIS by substituting ψ with either θ_{BR} , θ_{BU} , θ_{RU} , or ϕ_{RB} , taking into account the number of antenna elements at each. In addition, $[\psi]_{az}$ and $[\psi]_{el}$ are the azimuth and elevation components of ψ , respectively.

III. FISHER INFORMATION ANALYSIS

In this section, we present the Fisher information matrix (FIM) of the associated channels' parameters, the HRIS and UE positions, the HRIS rotation matrix, as well as the HRIS and UE synchronization.

A. FIM of Channel Parameters

We first concatenate the t -th noise-free observation over the k-th sub-carrier at the HRIS, $[\mu_{R,t}]_k \in \mathbb{C}$, and at the UE, $[\boldsymbol{\mu}_{U,t}]_k \in \mathbb{C}$, in the vector $\boldsymbol{\mu}_{t,k} \triangleq [[\boldsymbol{\mu}_{E,t}^{\text{max}}]_k, [\boldsymbol{\mu}_{U,t}]_k]^{\top} \in \mathbb{C}^2$. Let us define the aggregated vectors $\tau \triangleq [\tau_{\text{BR}}, \tau_{\text{BU}}, \tau_{\text{BR}}]^{\top} \in \mathbb{R}^3$, $\boldsymbol{\theta} \triangleq [\boldsymbol{\theta}_{\scriptscriptstyle{\text{BR}}}, \boldsymbol{\theta}_{\scriptscriptstyle{\text{RU}}}, \boldsymbol{\phi}_{\scriptscriptstyle{\text{RB}}}^\top]^\top \in \mathbb{R}^8, \text{ and } \mathbf{g} \triangleq [\mathbf{g}_{\scriptscriptstyle{\text{BR}}}^\top, \mathbf{g}_{\scriptscriptstyle{\text{RU}}}^\top, \mathbf{g}_{\scriptscriptstyle{\text{BRU}}}^\top]^\top \in \mathbb{R}^6,$ where $\mathbf{g}_{BR} \triangleq [\Re(g_{BR}), \Im(g_{BR})]^\top \in \mathbb{R}^2$, $\mathbf{g}_{BL} \triangleq$ $[\Re(g_{_{\text{BU}}}), \Im(g_{_{\text{BU}}})]^\top \in \mathbb{R}^2$, and $\mathbf{g}_{_{\text{BRU}}} \triangleq [\Re(g_{_{\text{BRU}}}), \Im(g_{_{\text{BRU}}})]^\top \in \mathbb{R}^2$. Using the latter notations, we introduce the vector with the associated unknown channels parameters:

$$
\boldsymbol{\zeta} = [\boldsymbol{\tau}^\top, \boldsymbol{\theta}^\top, \mathbf{g}^\top]^\top \in \mathbb{R}^{17}.
$$
 (12)

Considering the availability of the stacked observation vector $\mu_{t,k}$ at the fusion center, and given (5a)–(6b) and the Slepian-Bangs formula [53, Sec. 3.9], we can write the FIM of ζ , $\mathbf{J}_{\zeta} \in \mathbb{R}^{17 \times 17}$, as follows:

$$
\mathbf{J}_{\zeta} \triangleq \frac{2}{\sigma^2} \sum_{t=1}^{T} \sum_{k=1}^{K} \Re \left\{ \frac{\partial \boldsymbol{\mu}_{t,k}}{\partial \boldsymbol{\zeta}} \left(\frac{\partial \boldsymbol{\mu}_{t,k}}{\partial \boldsymbol{\zeta}} \right)^{\mathsf{H}} \right\}.
$$
 (13)

The latter expression can be used to obtain the equivalent FIM (EFIM) of the AOAs, AODs, and TOAs via the formula:

$$
\mathbf{J}_{\eta} \triangleq [[\mathbf{J}_{\zeta}^{-1}]_{1:11,1:11}]^{-1} \quad . \tag{14}
$$

The CRBs corresponding to AOAs, AODs, and TOAs, namely, the angle of arrival error bound (AAEB), angle of departure error bound (ADEB), and time of arrival error bound (TEB) can be respectively obtained using (14) as follows:

$$
\sigma_{\tau_i} = \sqrt{\mathbb{E}[(\tau_i - \hat{\tau}_i)^2]} \geq \text{TEB}_i \triangleq \sqrt{[\mathbf{J}_{\boldsymbol{\eta}}^{-1}]_{j,j}} ,
$$

\n
$$
\forall (i, j) \in \{(\text{BR}, 1), (\text{BU}, 2)(\text{BRU}, 3)\},
$$

\n
$$
\sigma_{\theta_i} = \sqrt{\mathbb{E}[\|\theta_i - \hat{\theta}_i\|^2]} \geq \text{ADEB}_i \triangleq \sqrt{[\mathbf{J}_{\boldsymbol{\eta}}^{-1}]_{j,j}} ,
$$

\n
$$
\forall (i, j) \in \{(\text{BR}, 4:5), (\text{BU}, 6:7), (\text{RU}, 8:9)\},
$$

\n
$$
\sigma_{\phi_{RB}} = \sqrt{\mathbb{E}[\|\phi_{RB} - \hat{\phi}_{RB}\|^2]} \geq \text{AAEB}_{RB} \triangleq \sqrt{[\mathbf{J}_{\boldsymbol{\eta}}^{-1}]_{10:11,10:11}},
$$

\n(15c)

where $\hat{\tau}_{i}$, $\hat{\theta}_{i}$, and $\hat{\phi}_{RB}$ are the estimation of the true parameters τ_i , θ_i , and ϕ_{RB} , respectively.

B. FIM of State Parameters

We commence by expressing the rotation matrix in (1) with respect to its columns, i.e., as $\mathbf{R} = [\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3]$ with \mathbf{r}_1 , \mathbf{r}_2 , and r_3 being three-dimensional column vectors. Then, we introduce the following state parameters vector:

$$
\boldsymbol{\zeta}_s \triangleq [\mathbf{p}_\mathrm{R}^\top, \mathbf{p}_\mathrm{U}^\top, b_\mathrm{R}, b_\mathrm{U}, \mathbf{r}^\top] \in \mathbb{R}^{17},\tag{16}
$$

where $\mathbf{r} \triangleq [\mathbf{r}_1^\top, \mathbf{r}_2^\top, \mathbf{r}_3^\top]^\top \in \mathbb{R}^9$. Given the relationship between the channel and the state parameters, we can derive the FIM of the latter parameters using the transformation matrix $T \in$ $\mathbb{R}^{11\times17}$, where the element at the ℓ -th row and m-th column of **T** is obtained as $[\mathbf{T}]_{\ell,m} = \partial[\eta]_{\ell}/\partial[\zeta_{s}]_{m}$ [53, Eq.(3.30)]. The elements of $J_{\mathcal{L}}$ and T are provided in the Appendices A and B, respectively. Then, using these matrices and (14), we can compute the FIM of the state parameters as follows:

$$
\mathbf{J}_{\zeta_{\rm s}} = \mathbf{T}^\top \mathbf{J}_{\eta} \mathbf{T}.\tag{17}
$$

To derive the error bounds for estimating the state parameters, it is necessary to consider the constraint on R. Therefore, we derive the constrained Cramér-Rao bound (CCRB) [54], which gives the lower bound on the covariance error of the estimate for each unbiased estimator, taking into account the required constraint on R. The orthogonality of this matrix, i.e., $\mathbf{R}^\top \mathbf{R} = \mathbf{I}_3$, imposes the following constraint:

$$
\boldsymbol{h}(\mathbf{r}) \triangleq \left[\|\mathbf{r}_1\|^2 - 1, \mathbf{r}_2^\top \mathbf{r}_1, \mathbf{r}_3^\top \mathbf{r}_1, \|\mathbf{r}_2\|^2 - 1, \mathbf{r}_2^\top \mathbf{r}_3, \|\mathbf{r}_3\|^2 - 1 \right]^\top = \mathbf{0}_6. \qquad (18)
$$

We next define the matrix $\Phi \triangleq \text{blkdiag}(\mathbf{I}_8, \frac{1}{\sqrt{2}})$ $(\frac{1}{2}\mathbf{\Phi}_0) \in \mathbb{R}^{17 \times 17}$ including the matrix notation:

$$
\Phi_0 \triangleq \begin{bmatrix} -\mathbf{r}_3 & \mathbf{0}_3 & \mathbf{r}_2 \\ \mathbf{0}_3 & -\mathbf{r}_3 & -\mathbf{r}_1 \\ \mathbf{r}_1 & \mathbf{r}_2 & \mathbf{0}_3 \end{bmatrix}, \tag{19}
$$

which satisfies $\mathbf{G}(\zeta)\mathbf{\Phi} = 0$ where $[\mathbf{G}]_{i,j} = \partial [\bm{h}(\zeta_{s})]_{i}/\partial [\zeta_{s}]_{j}$ $\forall i = 1, \ldots, 17$ and $\forall j = 1, \ldots, 17$ [54]. Then, the CCRB of the state parameters (i.e., $\mathbf{C}_{\zeta_s} \in \mathbb{R}^{17 \times 17}$) can be written as:

$$
\mathbf{C}_{\zeta_{\mathrm{s}}} = \mathbf{\Phi}(\mathbf{\Phi}^{\top} \mathbf{J}_{\zeta_{\mathrm{s}}} \mathbf{\Phi})^{-1} \mathbf{\Phi}^{\top}.
$$
 (20)

Using the latter expression, one can write the position error bound (PEB) of the HRIS and UE, the clock bias error bound (CEB) of the HRIS and UE, and the HRIS orientation error bound (OEB) as follows:

$$
\sigma_{\mathbf{p}_{i}} = \sqrt{\mathbb{E}\left[\|\mathbf{p}_{i} - \hat{\mathbf{p}}_{i}\|^{2}\right]} \geq \text{PEB}_{i} \triangleq \sqrt{[\mathbf{C}_{\zeta_{s}}]_{j:j+2,j:j+2}},
$$

$$
\forall (i, j) \in \{(\mathbf{R}, 1), (\mathbf{U}, 4)\},
$$
 (21a)

$$
\sigma_{\mathbf{r}} = \sqrt{\mathbb{E} \left\| (\mathbf{r} - \hat{\mathbf{r}} \|^2 \right\|} \ge \text{OEB} \triangleq \sqrt{[\mathbf{C}_{\zeta_s}]_{9:17,9:17}} \quad , \quad (21b)
$$

$$
\sigma_{b_i} = \sqrt{\mathbb{E}\left(b_i - \hat{b}_i\right)^2} \ge \text{CEB}_i \triangleq \sqrt{[\mathbf{C}_{\zeta_s}]_{j,j}},
$$

$$
\forall (i, j) \in \{(\mathbf{R}, 7), (\mathbf{U}, 8)\},
$$
 (21c)

where $\hat{\mathbf{p}}_i$, $\hat{\mathbf{r}}$, and \hat{b}_i are the estimates of the true parameters \mathbf{p}_i , \mathbf{r} , and b_i , respectively.

IV. PROPOSED PARAMETERS ESTIMATOR

In this section, we develop a multi-stage estimator that exploits the relationships between the states and channel parameters presented in Section II-B. To this aim, we sequentially estimate the associated channels. The underlying approach in the derivation of the estimator is the maximum likelihood principle, where the refined parameter search is initialized by a coarse search. In this process, the order of the operations is crucial, leading to different procedures for different links.

A. BS-HRIS Channel Parameter Estimation

Stacking all observation vectors, at the HRIS over T time instants into a matrix $\mathbf{Y}_{R} \in \mathbb{C}^{K \times T}$ yields:

$$
\mathbf{Y}_{\scriptscriptstyle\rm R} = g_{\scriptscriptstyle\rm BR} \sqrt{\rho P_{\scriptscriptstyle\rm B}} \mathbf{d}(\tau_{\scriptscriptstyle\rm BR}) \mathbf{a}_{\scriptscriptstyle\rm B}^\top (\boldsymbol{\theta}_{\scriptscriptstyle\rm BR}, \boldsymbol{\phi}_{\scriptscriptstyle\rm RB}) \,\boldsymbol{\Omega} + \mathbf{N}_{\scriptscriptstyle\rm R},\qquad (22)
$$

where we used the notations:

$$
\boldsymbol{a}_{\scriptscriptstyle{\mathrm{B}}}(\boldsymbol{\theta}_{\scriptscriptstyle{\mathrm{BR}}},\boldsymbol{\phi}_{\scriptscriptstyle{\mathrm{RB}}})\triangleq\text{vec}(\,\mathbf{a}_{\scriptscriptstyle{\mathrm{R}}}(\boldsymbol{\phi}_{\scriptscriptstyle{\mathrm{RB}}})\mathbf{a}_{\scriptscriptstyle{\mathrm{B}}}^{\top}(\boldsymbol{\theta}_{\scriptscriptstyle{\mathrm{BR}}}))\,\in\mathbb{C}^{M_{\scriptscriptstyle{\mathrm{B}}}M_{\scriptscriptstyle{\mathrm{R}}}},\quad(23a)
$$

$$
\mathbf{\Omega} \triangleq [\mathbf{f}_1 \otimes \mathbf{c}_1 \ldots, \mathbf{f}_T \otimes \mathbf{c}_T] \in \mathbb{C}^{M_{\mathrm{B}} M_{\mathrm{R}} \times T}, \quad (23b)
$$

and $N_{R} \in \mathbb{C}^{K \times T}$ is the noise matrix at the HRIS's single RX RF chain over all sub-carriers and time slots; this matrix contains zero-mean circularly-symmetric independent and identically distributed Gaussian elements with variance σ^2 . We then estimate the delay τ_{BR} between BS and HRIS using the approach prresented in [15, Secs. IV-A and IV-B]. The delay of this path can be obtained via solving the following optimization problem:

$$
\hat{\tau}_{_{BR}} = \arg \max_{\tau_{_{BR}}} ||\mathbf{d}^H(\tau_{_{BR}}) \mathbf{Y}_{_{R}}||. \tag{24}
$$

We can solve the problem (24) through 1D line search or gradient-based iterative search with an initial point, which can be provided by an FFT-based method [26].

We next remove the effect of τ_{BR} from \mathbf{Y}_{R} by calculating $\mathbf{Y}_{\text{\tiny R}} \odot (\mathbf{d}(-\hat{\tau}_{\text{\tiny BR}})\mathbf{1}_{T}^{\top})$. Taking the sum over the subcarriers, and after some algebraic manipulations, the following expression is deduced:

$$
\mathbf{z}_{_{\rm R}} = K g_{_{\rm BR}} \sqrt{\rho P_{\rm B}} \mathbf{\Omega}^{\top} \mathbf{a}_{_{\rm B}} (\boldsymbol{\theta}_{_{\rm BR}}, \boldsymbol{\phi}_{_{\rm RB}}) + \mathbf{n}_{_{\rm R}}',\tag{25}
$$

where $\mathbf{z}_{R} \in \mathbb{C}^{T}$ and $\mathbf{n}'_{R} \triangleq (\mathbf{N}_{R}^{\top} \odot (\mathbf{1}_{T} \mathbf{d}(-\hat{\tau}_{BR})^{\top})) \mathbf{1}_{K} \in \mathbb{C}^{T}$. We next use the matrix $\Psi \triangleq \Omega^{\top} A \in \mathbb{C}^{T \times J}$ with $J \gg T$, where $\boldsymbol{A}\triangleq[\boldsymbol{a}_{_{\mathbb{B}R_{1}}}, \overline{\boldsymbol{\phi}}_{_{\mathbb{R}\mathrm{B}_{1}}}), \ldots, \boldsymbol{a}_{_{\mathbb{B}}}(\overline{\boldsymbol{\theta}}_{_{\mathbb{B}\mathrm{R}_{J}}}, \overline{\boldsymbol{\phi}}_{_{\mathbb{R}\mathrm{B}_{J}}})]\in\mathbb{C}^{{M_{_{\mathbb{B}}}}{M_{_{\mathbb{R}}}}\times J}$ is a dictionary matrix containing combined array response vectors, given by (23a), with the AOD from the BS to the HRIS and the AOA at the HRIS from the BS pairs $(\theta_{_{\text{BR}_j}}, \phi_{_{\text{RB}_j}})$ $\forall j = 1, 2, ..., J$. Using this matrix definition, we can approximate z_R as follows:

$$
\mathbf{z}_{R} \approx \mathbf{\Psi} \mathbf{x} + \mathbf{n}_{R}^{\prime},\tag{26}
$$

where $\mathbf{x} \in \mathbb{C}^J$ is a sparse vector including a single non-zero element that is approximately equal to $K g_{BR} \sqrt{\rho P_B}$. The latter expression enables us to use compressed sensing (CS) methods to estimate x, the AOA at the HRIS, and the AOD from the BS to the HRIS. To this end, we deploy a simple grid search in the dictionary,⁷ which selects the column of Ψ that has the maximum scalar product with z_R . Finally, we refine the angle estimation. Thus, one can apply these estimated angles as an initial guess for the Newton's method to solve the negative maximum likelihood optimization problem,⁸ which can be expressed, using (25), as follows:

$$
\left[\hat{\boldsymbol{\theta}}_{\text{BR}}, \hat{\boldsymbol{\phi}}_{\text{RB}}\right] = \arg \min_{\boldsymbol{\theta}_{\text{BR}}, \boldsymbol{\phi}_{\text{RB}}} \|\mathbf{z}_{\text{R}} - K \sqrt{\rho P_{\text{B}}} \hat{g}_{\text{BR}}(\boldsymbol{\theta}_{\text{BR}}, \boldsymbol{\phi}_{\text{RB}})
$$

$$
\boldsymbol{\Omega}^{\top} \boldsymbol{a}_{\text{B}}(\boldsymbol{\theta}_{\text{BR}}, \boldsymbol{\phi}_{\text{RB}})\|^{2}, \qquad (27)
$$

where $\hat{g}_{_{\text{BR}}}(\theta_{_{\text{BR}}}, \phi_{_{\text{RB}}}) \triangleq (\mathbf{\Omega}^{\top} \boldsymbol{a}_{_{\text{B}}}(\theta_{_{\text{BR}}}, \phi_{_{\text{RB}}})^{\dagger} \mathbf{z}/(K\sqrt{\rho P_{\text{B}}}).$

B. BS-UE and BS-HRIS-UE Channel Parameter Estimation

We first stack all observation vectors at the UE over T time instants in a matrix $\mathbf{Y}_{\text{U}} \in \mathbb{C}^{K \times T}$, yielding:

$$
\mathbf{Y}_{\mathrm{U}} = \mathbf{Y}_{\mathrm{BU}} + \mathbf{Y}_{\mathrm{BRU}} + \mathbf{N}_{\mathrm{U}},\tag{28}
$$

and $N_{\text{U}} \in \mathbb{C}^{K \times T}$ represents the noise matrix received at the UE's receiver across all sub-carriers and time slots. This matrix consists of circularly-symmetric, independent, and identically distributed Gaussian elements with zero mean and a variance of σ^2 . The BS-UE and BS-HRIS-UE signal components can

 7 The resolution of the grid searches is fine enough to initialize the Newton method searches, and thus off-grid effects do not limit the achievable accuracy. To avoid the increased complexity of very fine grid searches, a hierarchical approach is followed, where a finer search is done around the optimum obtained with a coarse search.

⁸This estimation approach has a weak similarity with the Newtonized orthogonal matching pursuit proposed in [55]. However, in that paper, the proposed algorithm was used to jointly estimate TOA, AOA, and the channel gains [56], [57], which constitutes a different goal compared to our paper. Our proposed algorithm applies a multi-stage estimator where TOA and AOA/AOD are sequentially estimated, followed by refinement using the Newton's method. TOA's estimation is particularly performed using the FFT, followed by fractional refinement.

be separated using an appropriate design of the HRIS phase profile and BS beamformer [16], as explained below. The FC can combine the signals in such a way that the interference between both components is eliminated in a static scenario, thus facilitating the derivation of an estimator.

To design the HRIS phase profile and the precoder at the BS, we set T to be an even number and define $\gamma_{2t} = -\gamma_{2t+1}$ and $\mathbf{f}_{2t} = \mathbf{f}_{2t+1}$ for $t = 0, 1, \dots, T/2$. Given this HRIS phase profile, and considering (6a) and (6b), we can write:

$$
[\mathbf{Y}_{\text{BU}}]_{:,2t} = [\mathbf{Y}_{\text{BU}}]_{:,2t+1},\tag{29}
$$

$$
[\mathbf{Y}_{\text{BRU}}]_{:,2t} = -[\mathbf{Y}_{\text{BRU}}]_{:,2t+1}.
$$
 (30)

Using the latter expressions, the FC performs post-processing to calculate the matrices $\mathbf{Z}_{\text{\tiny BU}} \in \mathbb{C}^{K \times T/2}$ and $\mathbf{Z}_{\text{\tiny BRU}} \in \mathbb{C}^{K \times T/2}$ as follows:

$$
[\mathbf{Z}_{\text{BU}}]_{:,2t} = [\mathbf{Y}_{\text{U}}]_{:,2t} + [\mathbf{Y}_{\text{U}}]_{:,2t+1} = 2g_{\text{BU}}\sqrt{P_{\text{B}}}d(\tau_{\text{BU}}) \mathbf{a}_{\text{B}}^\top(\boldsymbol{\theta}_{\text{BU}})
$$

$$
\mathbf{f}_{\text{z}_t} + [\mathbf{N}_{\text{U}}]_{:,2t} + [\mathbf{N}_{\text{U}}]_{:,2t+1},
$$
(31a)

$$
[\mathbf{Z}_{\text{BRU}}]_{:,2t} = [\mathbf{Y}_{\text{U}}]_{:,2t} - [\mathbf{Y}_{\text{U}}]_{:,2t+1} = 2g_{\text{BRU}}\sqrt{(1-\rho)P_{\text{B}}} \mathbf{d}(\tau_{\text{BRU}})
$$

$$
\mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RU}}) \operatorname{diag}(\boldsymbol{\gamma}_{\text{A}}) \mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_{\text{A}} + [\mathbf{N}_{\text{U}}]_{:,2t} - [\mathbf{N}_{\text{U}}]_{:,2t+1},
$$
(31b)

where N'_{i} $U_{\text{U}} \in \mathbb{C}^{K \times T/2}$ is the noise matrix at the UE after post-processing, over all sub-carriers and time slots, containing zero-mean circularly-symmetric independent and identically distributed Gaussian elements with variance $2\sigma^2$. As can be observed form (31a) and (31b), the matrices $\mathbf{Z}_{\text{\tiny{BU}}}$ and $\mathbf{Z}_{\text{\tiny{BHI}}}$ depend only the parameters of the direct and the reflected channels, respectively. Thus, these channels become separated. It is emphasized here that the proposed HRIS reflection phase profiles do not lead to a waste of resources due to repeating the beams. This holds because, after the post-processing given by (31a) and (31b), the signals Z_{BU} and Z_{BRU} have high signalto-noise ratio (SNR) compared to the signals Y_{BU} and Y_{BRU} , respectively.

1) BS-UE channel estimation: We commence with BS-UE channel estimation using (31a). To this end, we rewrite this expression as follows:

$$
\mathbf{Z}_{\text{\tiny BU}} = 2g_{\text{\tiny BU}}\sqrt{P_{\text{B}}}\mathbf{d}(\tau_{\text{\tiny BU}})\,\mathbf{a}_{\text{\tiny B}}^{\top}(\boldsymbol{\theta}_{\text{\tiny BU}})\mathbf{F} + \mathbf{N}_{\text{\tiny U}}^{'},\tag{32}
$$

where $\mathbf{F} \triangleq [\mathbf{f}_0, \dots, \mathbf{f}_{T/2}] \in \mathbb{C}^{M_B \times T/2}$. We next follow a similar approach to that in Sec. IV-A to estimate τ_{BU} (see expression (24)). After removing the effect of this TOA and integrating the signals over the K subcarrier frequencies, the following expression is deduced:

$$
\mathbf{z}_{\text{BU}} = 2K g_{\text{BU}} \sqrt{P_{\text{B}}} \mathbf{F}^{\top} \mathbf{a}_{\text{B}} (\boldsymbol{\theta}_{\text{BU}}) + \mathbf{n}_{\text{U}}^{'}, \tag{33}
$$

where $\mathbf{z}_{\text{BU}} \in \mathbb{C}^{T/2}$ and $\mathbf{n}'_v \triangleq (\mathbf{N}'_v)$ U ⊤ ⊙ $(\mathbf{1}_{T/2}\mathbf{d}(-\hat{\tau}_{BU})^{\top})\mathbf{1}_{K} \in \mathbb{C}^{T/2}$. Using (33), we can write the negative maximum likelihood optimization problem as:

$$
\hat{\boldsymbol{\theta}}_{\text{BU}} = \arg\min_{\boldsymbol{\theta}_{\text{BU}}} \|\mathbf{z}_{\text{BU}} - 2K\sqrt{P_{\text{B}}}\hat{g}_{\text{BU}}(\boldsymbol{\theta}_{\text{BU}})\mathbf{F}^{\top}\mathbf{a}_{\text{B}}(\boldsymbol{\theta}_{\text{BU}})\|^{2}, \quad (34)
$$

where $\hat{g}_{\text{BU}}(\theta_{\text{BU}}) = (\mathbf{F}^{\top} \mathbf{a}_{\text{B}}(\theta_{\text{BU}}))^{\dagger} \mathbf{z}_{\text{BU}}/(2K\sqrt{P_{\text{B}}})$. To solve this problem, we first apply a coarse 2D search over $[\theta_{\text{\tiny BU}}]_{el}$ - $[\theta_{\text{BU}}]_{\text{az}}$ search space to jointly estimate the elevation and azimuth angles. Then, we refine the coarse estimation by applying its estimated angles as an initial guess for Newton's method.

2) BS-HRIS-UE channel estimation: The remaining parameters that need to be estimated for the BS-HRIS-UE channel are τ_{BRI} and θ_{RI} . Based on (27), we can rewrite (31b) as:

$$
[\mathbf{Z}_{\text{BRU}}]_{:,2t} = 2g_{\text{BRU}}\sqrt{(1-\rho)P_{\text{B}}} \mathbf{d}(\tau_{\text{BRU}})\mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RU}})\mathbf{b}_{\text{2t}} + [\mathbf{N}_{\text{U}}^{'}]_{:,2t},
$$
\n(35)

where $\mathbf{b}_{2t} \triangleq \text{diag}(\gamma_{2t}) \mathbf{a}_{R}(\hat{\boldsymbol{\phi}}_{RB}) \mathbf{a}_{B}^{\top}(\hat{\boldsymbol{\theta}}_{BR}) \mathbf{f}_{2t} \in \mathbb{C}^{M_{R} \times 1}$. Using (35), we then stack all observation vectors related to the BS-HRIS-UE link to express $\mathbf{Z}_{\text{\tiny{RRU}}}$ as follows:

$$
\mathbf{Z}_{\text{BRU}} = 2g_{\text{BRU}}\sqrt{(1-\rho)P_{\text{B}}}\mathbf{d}(\tau_{\text{BRU}})\mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RU}})\mathbf{B} + \mathbf{N}_{\text{U}}^{'},\qquad(36)
$$

where $\mathbf{B} \triangleq [\mathbf{b}_0, \mathbf{b}_2, \dots, \mathbf{b}_{T_Z}] \in \mathbb{C}^{M_R \times T/2}$. As before, τ_{BRU} can be estimated using (24), and then, it can be removed. By integrating the processed signals over the K subcarrier frequencies, one can obtain the vector $\mathbf{z}_{\text{\tiny{BRU}}} \in \mathbb{C}^{T/2}$ as:

$$
\mathbf{z}_{\text{BRU}} = g_{\text{BRU}} \mathbf{B}_0^\top \mathbf{a}_{\text{R}} (\boldsymbol{\theta}_{\text{RU}}) + \mathbf{n}_{\text{U}}^{\prime\prime}, \tag{37}
$$

where $\mathbf{B}_0 \triangleq 2K\sqrt{(1-\rho)P_B}\mathbf{B}^\top \in \mathbb{C}^{T/2\times M_R}$ and $\mathbf{n}_{\mathrm{U}}'' \triangleq$ $(N^{'}_{\scriptscriptstyle{I}}$ $U_{\rm U}^{(-)} \odot (\mathbf{1}_{T/2} \mathbf{d}(-\hat{\tau}_{\text{BRU}})^{\top})) \mathbf{1}_{K} \in \mathbb{C}^{T/2}$. To estimate $\theta_{\rm RU}$, we formulate the negative maximum likelihood problem as follows:

$$
\hat{\boldsymbol{\theta}}_{\text{\tiny RU}} = \arg\min_{\boldsymbol{\theta}_{\text{\tiny RU}}} \|\mathbf{z}_{\text{\tiny BRU}} - \hat{g}_{\text{\tiny BRU}} \mathbf{B}_0^\top \mathbf{a}_{\text{\tiny R}}(\boldsymbol{\theta}_{\text{\tiny RU}})\|^2, \qquad (38)
$$

where $\hat{g}_{BRU} = (\mathbf{B}_0^{\top} \mathbf{a}_{R}(\theta_{RU}))^{\dagger} \mathbf{z}_{BRU}$. Similar to Sec. IV-B1, we first find a coarse estimate of θ_{RU} through a 2D search. Then, we refine the estimation by applying the coarse estimation of θ_{RU} as an initial point in Newton's method.

C. Estimation of HRIS and UE Position and Clock Bias

Exploiting the one-to-one mapping presented in Section II-B between the channel and state parameters, and specifically expressions (8a) and (8b), we define the following parameter:

$$
\hat{d} \triangleq d_{\text{BR}} + d_{\text{RU}} - d_{\text{BU}} = c(\hat{\tau}_{\text{BRU}} - \hat{\tau}_{\text{BU}}). \tag{39}
$$

and the following direction vector:

$$
\boldsymbol{\kappa}(\boldsymbol{\psi}) \triangleq \begin{bmatrix} \cos[\boldsymbol{\psi}]_{\mathrm{az}} \sin[\boldsymbol{\psi}]_{\mathrm{el}} \\ \sin[\boldsymbol{\psi}]_{\mathrm{az}} \sin[\boldsymbol{\psi}]_{\mathrm{el}} \\ \cos[\boldsymbol{\psi}]_{\mathrm{el}} \end{bmatrix} . \tag{40}
$$

Using the latter definition and the estimated AOA/AODs at the BS and HRIS, the angles of the BS-HRIS-UE triangle (see Fig. 1) can be obtained as:

$$
\beta_0 = \text{acos}\left(\boldsymbol{\kappa}^\top (\hat{\boldsymbol{\theta}}_{\text{\tiny RU}}) \boldsymbol{\kappa} (\hat{\boldsymbol{\phi}}_{\text{\tiny RB}})\right),\tag{41a}
$$

$$
\beta_1 = \text{acos}\left(\boldsymbol{\kappa}^\top (\hat{\boldsymbol{\theta}}_{_{\text{BU}}}) \boldsymbol{\kappa} (\hat{\boldsymbol{\theta}}_{_{\text{BR}}})\right),\tag{41b}
$$

$$
\beta_2 = \pi - \beta_0 - \beta_1,\tag{41c}
$$

Capitalizing on (39) and (41), and applying the law of sines in the triangle with edges the BS, HRIS, and UE in Fig. 1, the distances from the BS to the other two network nodes are computed as follows:

$$
\hat{d}_{\text{BU}} = \frac{\hat{d}\sin\beta_0}{\sin\beta_2 + \sin\beta_1 - \sin\beta_0},\tag{42}
$$

$$
\hat{d}_{\text{BR}} = \frac{\hat{d}\sin\beta_2}{\sin\beta_2 + \sin\beta_1 - \sin\beta_0}.
$$
 (43)

Using (40), (42), (43), and the AODs from the BS to the other nodes, one can estimate the positions of the HRIS and UE as:

$$
\hat{\mathbf{p}}_{\scriptscriptstyle{\text{R}}} = \mathbf{p}_{\scriptscriptstyle{\text{B}}} + \hat{d}_{\scriptscriptstyle{\text{BR}}} \kappa(\hat{\theta}_{\scriptscriptstyle{\text{BR}}}), \text{ and } \hat{\mathbf{p}}_{\scriptscriptstyle{\text{U}}} = \mathbf{p}_{\scriptscriptstyle{\text{B}}} + \hat{d}_{\scriptscriptstyle{\text{BU}}} \kappa(\hat{\theta}_{\scriptscriptstyle{\text{BU}}}). \tag{44}
$$

Finally, using the estimated TOAs and node positions, we respectively estimate the clock bias at the HRIS and UE as:

$$
\hat{b}_{\text{R}} = \hat{\tau}_{\text{BR}} - \frac{\hat{d}_{\text{BR}}}{c}, \text{ and } \hat{b}_{\text{U}} = \hat{\tau}_{\text{BU}} - \frac{\hat{d}_{\text{BU}}}{c}.
$$
 (45)

D. HRIS Rotation Matrix Estimation

We rewrite (3) as follows:

$$
\boldsymbol{\kappa}(\boldsymbol{\phi}_{_{RB}}) = \mathbf{R}^{\top}(\mathbf{p}_{B} - \mathbf{p}_{R}) / ||\mathbf{p}_{B} - \mathbf{p}_{R}|| \in \mathbb{R}^{3}, \tag{46a}
$$

$$
\kappa(\boldsymbol{\theta}_{\text{\tiny RU}}) = \mathbf{R}^{\top} (\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}}) / \|\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}}\| \in \mathbb{R}^{3}.
$$
 (46b)

If we replace the values of ϕ_{RB} , θ_{RU} , p_R , and p_U with their estimates (i.e., (27), (38), (44), and (44), respectively), then the least-squares estimate of the HRIS rotation matrix **can** obtained by solving the following optimization problem:

$$
\hat{\mathbf{R}} = \arg\min_{\mathbf{R}} \|\mathbf{Q} - \mathbf{R}\Theta\|,\tag{47a}
$$

subject to $\mathbf{R}^\top \mathbf{R} = \mathbf{I}_3$, and $\det(\mathbf{R}) = 1$, (47b)

where we have used the definitions:

$$
\boldsymbol{\Theta} \triangleq \begin{bmatrix} \kappa(\hat{\boldsymbol{\phi}}_{_{\mathsf{RB}}}) & \kappa(\hat{\boldsymbol{\theta}}_{_{\mathsf{RU}}}) \end{bmatrix} \in \mathbb{R}^{3 \times 2}, \tag{48a}
$$

$$
\mathbf{Q} \triangleq \begin{bmatrix} \frac{\mathbf{p}_B - \hat{\mathbf{p}}_R}{\|\mathbf{p}_B - \hat{\mathbf{p}}_R\|} & \frac{\hat{\mathbf{p}}_U - \hat{\mathbf{p}}_R}{\|\hat{\mathbf{p}}_U - \hat{\mathbf{p}}_R\|} \end{bmatrix} \in \mathbb{R}^{3 \times 2}.
$$
 (48b)

Note that the first constraint in (47b) does not automatically ensure the second constraint. The first constraint specifies that the matrix **R** is orthogonal, meaning $\mathbf{R}^\top \mathbf{R} = \mathbf{I}_3$, which implies $\mathbf{R}^{\top} = \mathbf{R}^{-1}$. The determinant of an orthogonal matrix **R** can be det(**R**) = ± 1 . Since **R** represents a rotation, its determinant should be 1.

The optimization problem (47) is known as the *orthogonal Procrustes problem* [58]) and its solutions is given by [59], [60, eq. (8)] as follows:

$$
\hat{\mathbf{R}} = \mathbf{U}_0 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & \det(\mathbf{U}_0 \mathbf{U}_1^\top) \end{bmatrix} \mathbf{U}_1^\top, \tag{49}
$$

where $\mathbf{U}_0 \in \mathbb{R}^{3 \times 3}$ and $\mathbf{U}_1 \in \mathbb{R}^{3 \times 3}$ are the left and right singular vectors of matrix⁹ $Q\Theta$ [†].

It is worthwhile mentioning that due to the HRIS's sensing capability, the estimation of HRIS and UE positions can be achieved independently of the rotation matrix R. The TOA and AOA sensing capabilities of the RIS are necessary because

Algorithm 1: Proposed UE/HRIS 3D State Estimation

Require: Y_{R} , Y_{U} , **A**, \mathbf{c}_{t} , γ_{t} , and \mathbf{f}_{t} , $t = 0, \ldots, T$ Channel Estimation of BS-HRIS link

- 1: Estimate $\hat{\tau}_{\text{\tiny BP}}$ using (24) and remove its effect from the channel.
- 2: Coarse estimates $\hat{\theta}_{_{\text{BR}}}$ and $\hat{\phi}_{_{\text{RB}}}$ via grid search using dictionary A.

3: Obtain the refined $\hat{\theta}_{BR}$ and $\hat{\phi}_{RB}$ by solving (27) initialized with $\hat{\theta}_{_{\text{BR}}}$ and $\hat{\phi}_{_{\text{RB}}}$.

Post processing of the UE received signals

4: Resolve BS-UE path $(\mathbb{Z}_{\text{\tiny{BU}}})$ from BS-HRIS-UE path $(\mathbf{Z}_{\text{\tiny{BRU}}}).$

Channel Estimation of BS-UE link

- 5: Estimate $\hat{\tau}_{\text{BH}}$ and remove its effect from the channel.
- 6: Coarse estimate $\hat{\theta}_{\text{BU}}$ by solving (34) via 1D grid search.
- 7: Obtain the refined $\hat{\theta}_{\text{BU}}$ by solving (34) initialized with $\hat{\boldsymbol{\theta}}_{_{\rm BU}}$.

Channel Estimation of BS-HRIS-UE link

8: Estimate $\hat{\tau}_{\text{BRI}}$ and remove its effect from the channel. 9: Coarse estimate $\hat{\theta}_{\text{\tiny{RU}}}$ by solving (38) via 1D grid search. 10: Obtain the refined $\hat{\theta}_{\text{\tiny{RU}}}$ by solving (38) initialized with

$\hat{\boldsymbol{\theta}}_{_{\rm RU}}$. State estimate of the UE and the HRIS

- 11: Estimates d_{BU} and d_{BR} using (42)–(43).
- 12: Estimates $\hat{\mathbf{p}}_{\text{U}}$ and $\hat{\mathbf{p}}_{\text{R}}$ using (44).
- 13: Estimates \hat{b}_R and \hat{b}_U using (45).
- 14: Estimates \bf{R} using (49).

Return:
$$
\hat{\mathbf{p}}_{\nu}
$$
, $\hat{\mathbf{p}}_{\kappa}$, \hat{b}_{κ} , \hat{b}_{ν} , and $\hat{\mathbf{R}}$.

the position of the HRIS is unknown. As a by-product, we also obtain the HRIS orientation. Once the HRIS orientation is known, we are then in conditions assumed in many other papers, such as [16], where the HRIS rotation matrix can be utilized. Despite this, incorporating the HRIS rotation matrix in localization systems aids in efficiently estimating the position of a new UE, simplifying the process and benefiting methods involving sensing or directional beamforming with the HRIS. Overall, the proposed method for joint localization of 3D user and 6D HRIS can be summarized as described in Algorithm 1.

E. Estimation Complexity Analysis

In this subsection, we analyze the computational complexity of the proposed estimator, which is dominated by the computation of the channel parameters and rotation matrix. In channel parameters' estimation, we need to compute a 2D N_F -point FFT for the delay estimation, whose computational cost is given by $\mathcal{O}(N_F \log(N_F))$. The joint estimation of θ_{BR} and ϕ_{RB} needs to build the dictionary, which is requires $\mathcal{O}(TM_{\rm B}M_{\rm B}J)$ operations. In addition, $\mathcal{O}(TJ)$ operations are needed for searching over the dictionary. Note that the coarse and fine search for the joint estimation of $\theta_{\text{\tiny BR}}$ and $\phi_{\text{\tiny BR}}$ have the same computational complexity order. The computational cost of the final refinement of θ_{BR} and ϕ_{RB} , based on (27), is given by $\mathcal{O}(TM_{\rm B}M_{\rm R}I_1)$, where I_1 indicates the number of iterations. For the BS-UE channel estimation (i.e., $\hat{\theta}_{BU}$), we resort to Jacobi-Anger expansion to simplify the 2D search into 1D

⁹The singular value decomposition (SVD) of $\mathbf{Q}\mathbf{\Theta}^{\top}$ is $\mathbf{Q}\mathbf{\Theta}^{\top} = \mathbf{U}_0 \mathbf{\Sigma} \mathbf{U}_1^{\top}$, where Σ is a diagonal matrix containing the singular values of $\mathbf{Q}\Theta$ [⊤].

Fig. 2: The Newton method's convergence in solving the optimization prob-Fig. 2: The Newton method's convergence in solving the optimization problems outlined in equations (27), (34), and (38), initialized by coarse estimation lems outlined in equations (27), (34), and (38), initialized by coarse estimation solutions, is analyzed. The analysis assumes a transmit power of 20dBm. solutions, is analyzed. The analysis assumes a transmit power of 20dBm.

search [61], resulting in complexity $\mathcal{O}(TM_{\text{B}}(2N+1)r)$ [62, Appendix C], where $2N + 1$ and r respectively indicate the number of terms in the Jacobi-Anger approximation and the number of terms in the Jacobi-Anger approximation and the searching dimension in the azimuth or elevation angles. It searching dimension in the azimuth or elevation angles. It is worthwhile mentioning that, if we applied a simple 2D is worthwhile mentioning that, if we applied a simple 2D search, the computational complexity would be $\mathcal{O}(TM_{\rm B}r^2)$; this requires much more computational complexity than the this requires much more computational complexity than the Jacobi-Anger approach since $r \gg (2N+1)$. For the refinement of $\hat{\theta}_{BU}$ according to (34), the computational complexity is $\mathcal{O}(TM_{\rm B}(2N+1)I_2)$ with I_2 denoting the number of iterations. Similarly, the coarse and fine estimations of $\theta_{\text{\tiny{RU}}}$ are given by $\mathcal{O}(TM_{\rm R}(2N+1)r)$ and $\mathcal{O}(TM_{\rm R}(2N+1)I_3)$, respectively, with I_3 being the number of iterations. Therefore, the computational complexity of the rotation matrix estimation is bounded to complexity of the rotation matrix estimation is bounded to $O(27)$ operations. Putting all above together, the complexity order of the proposed estimator is:

$$
C_{\text{prop}} \approx \mathcal{O}(N_F \log(N_F)) + \mathcal{O}(T M_{\text{B}} M_{\text{R}} (J + I_1))
$$

+ $\mathcal{O}(T M_{\text{B}} N I_2) + \mathcal{O}(T M_{\text{R}} N (r + I_3)).$ (50)

The term $\mathcal{O}(TM_{\rm B}M_{\rm R}(J + I_{1}))$ is in most cases dominant. To enhance clarity and provide a comprehensive analysis of To enhance clarity and provide a comprehensive analysis of computational complexity, we illustrate the convergence of computational complexity, we illustrate the convergence of refined parameter estimation using the cost functions outlined refined parameter estimation using the cost functions outlined in optimization problems (27) , (34) , and (38) in Fig. 2. As depicted in Fig. 2, the Newton method achieves convergence depicted in Fig. 2, the Newton method achieves convergence after 24 iterations $(I_1 = 24)$ for solving (27), represented by the blue curve. Similarly, it achieves convergence after 6 by the blue curve. Similarly, it achieves convergence after 6 iterations $(I_2 = 6)$ for (34) (shown in red) and 5 iterations $(I_3 = 5)$ for (38) (shown in purple).

V. NUMERICAL RESULTS AND DISCUSSION V. NUMERICAL RESULTS AND DISCUSSION

In this section, we evaluate the performance of the proposed estimation algorithm. In particular, we compare the RMSE of the estimated parameters with their corresponding CRBs, of the estimated parmameters with their corresponding CRBs, as derived in Sec. III. For the RMSE calculations, we have averaged the results over 500 independent noise realizations. averaged the results over 500 independent noise realizations. All the reflection phase shifts of the HRIS hybrid meta-All the reflection phase shifts of the HRIS hybrid metaatoms have been drawn from the uniform distribution, i.e., atoms have been drawn from the uniform distribution, i.e., $\angle[\gamma_t]_k \sim \mathcal{U}[0, 2\pi)$ $\forall t$ and $\forall k = 1, ..., M_{\rm R}$. For the HRIS sensing combiner c_t and the BS precoder $f_t \forall t$, we have used
DET codebooks. Each channel gain has been modeled as: DFT codebooks. Each channel gain has been modeled as: DFT codebooks. Each channel gain has been modeled as:

$$
g_i \triangleq |g_i|e^{-j\phi_i} \quad i \in \{\text{BR}, \text{BU}, \text{BRU}\},\tag{51}
$$

TABLE II: The considered simulation parameters. TABLE II: The considered simulation parameters.

Parameter	Symbol	Value
Wavelength	λ	1 cm
HRIS/BS element distance	d.	0.25 cm
Light speed	ϵ	3×10^8 m/sec
Number of subcarriers	K	128
Number of transmissions	T	100
Sub-carrier spacing	Δf	120 kHz
Noise PSD	N_0	-174 dBm/Hz
RX's noise figure	n_f	5 dB
IFFT Size	N_F	4096
UE position	\mathbf{p}_{U}	$[5 \text{ m}, 2 \text{ m}, 1 \text{ m}]$
BS position	\mathbf{p}_B	$[0 \; \text{m}, 0 \; \text{m}, 0 \; \text{m}]^{\top}$
HRIS position	P_{R}	$[2 \; \text{m}, 12 \; \text{m}, 3 \; \text{m}]$
RIS orientation angles	$[\alpha, \gamma, \beta]$	$[20^{\circ}, 10^{\circ}, 15^{\circ}]^{\top}$
Number of BS antennas	$M_{\tt w}$	4×4
Number of HRIS elements	$M_{\tt R}$	16×16

where $\phi_i \sim U[0, 2\pi)$ and $|g_i|$ follows the model described in [63, eq. (21)–(23)]. In addition, $g_{\text{BSU},i}$ and $g_{\text{BRSU},i}$ follow the radar equation [64]. The rest of the simulation parameters are summarized in Table II. summarized in Table II.

A. Channel Parameter Estimation A. Channel Parameter Estimation

We first show the performance of the channel parameter We first show the performance of the channel parameter estimation routine from Secs. IV-A and IV-B as a function estimation routine from Secs. IV-A and IV-B as a function of the transmit power P_B . To this end, we have selected the P_B range such that the BRU link is not very weak, to avoid failure of the AOD estimation from the HRIS to the UE, which can be a bottleneck for joint HRIS and UE localization. The can be a bottleneck for joint HRIS and UE localization. The results are shown in Fig. 3 considering an HRIS, common results are shown in Fig. 3 considering an HRIS, common for all its hybrid meta-atoms, power splitting factor of $\rho =$ 0.5 . In terms of TOA estimation, we observe in Fig. ?? that for the considered range of transmit powers, the TEB bounds coincide with the corresponding RMSE values (denoted by σ_i with $i \in \{T_{BR}, T_{BU}, T_{BRU}\}\)$. Due to the path loss differences,
the TOA estimation of the BBU path is the worst, while the the TOA estimation of the BRU path is the worst, while the the TOA estimation of the BRU path is the worst, while the TOA estimation of the BR path is the best. This indicates that TOA estimation of the BR path is the best. This indicates that the BRU path is the bottleneck in TOA estimation, and thus, the BRU path is the bottleneck in TOA estimation, and thus, in positioning. For the estimation of the AOA and AOD shown in Fig. ??, the AOA at the HRIS performance is the best. We note that the RMSE of θ_{BR} is smaller than the RMSE of the θ_{BU} because the BS-HRIS link has a higher SNR thanks to the beamforming gain at the HRIS in spite of the larger BS-the beamforming gain at the HRIS in spite of the larger BS-HRIS distance compared to the BS-UE distance. As can be HRIS distance compared to the BS-UE distance. As can be also seen, the worst estimation performance is achieved for also seen, the worst estimation performance is achieved for the AOD from HRIS to the UE. the AOD from HRIS to the UE. with $i \in \{\tau_{BR}, \tau_{BU}, \tau_{BRU}\}\)$. Due to the path loss differences,

B. UE and HRIS Position Estimation B. UE and HRIS Position Estimation

In Fig. 4, we present numerical results for the UE and HRIS positioning performance, as well as the HRIS orientation HRIS positioning performance, as well as the HRIS orientation estimation performance. As depicted in Fig. $?$?, the UE can be localized somewhat better than the HRIS. However, the positioning performance difference is small, since the two positioning performance difference is small, since the two spatial states are coupled. In terms of the HRIS orientation spatial states are coupled. In terms of the HRIS orientation estimation, as illustrated in Fig. ??, the proposed estimator achieves the bound for most considered transmit power tor achieves the bound for most considered transmit power levels. Nevertheless, the estimations for the HRIS and the levels. Nevertheless, the estimations for the HRIS and the UE positions and that for the HRIS orientation affect each UE positions and that for the HRIS orientation affect each

Fig. 3: The evaluation of the proposed channel parameter estimator. The power splitting factor is set to $\rho = 0.5$. (a) The RMSE of the TOAs; (b) The RMSE of the AOA/AODs. of the AOA/AODs. of the AOA/AODs.

TABLE III: The considered scenarios for studying the effect of the HRIS state on the UE state estimation, and vice versa.

Scenarios	\mathbf{p}_R	$p_{\rm U}$	R.
C ₁	unknown	unknown	unknown
C2	unknown	known	known
CЗ	unknown	unknown	known
C ₄	unknown	known	unknown
\overline{C} 5	known	unknown	known
	known	unknown	unknown

10¹

10⁰

scenarios described in Table III. Based on these scenarios, we school and the scenarios described in Table III. Based on these scenarios, we calculate the CRBs on the HRIS and UE position estimations, $\frac{1}{2}$ information about the UE position causes the improvement that the PEB of the UE and the HRIS are the same regardless 24 , will
mpact (c
stimation
25 and C
with the 1 in the HRIS positioning error (compare C1 with C2 and of whether the state of the matrix R is known or not. This C4), while the HRIS orientation does not have a considerable impact (compare C1 with C3). Similarly, the UE position UE and HRIS positions (see Sec. IV-C). All parameters except $\frac{1}{1}$ and $\frac{1}{1}$ and RIS state estimator. The power earenate the exists of the FIRES and OE position estimations,
which are shown in Fig. 5. As it can be observed, having k
مو 10² with the unknown HRIS position case, i.e., compare C1 with happen because matrix \bf{R} is not used in the estimation of the happen because matrix \bf{R} is not used in the estimation of the other's accuracy.¹⁰ To investigate this fact, we consider the estimation comes with smaller error, i.e., compare C1 with C5 and C6, when the HRIS position is known, as compared C3. One can also see from comparing C1 and C3 in Fig. 5

splitting factor is set to \mathcal{L} and \mathcal{L} and position estimation estimation estimation estimation estimations;

Fig. 4: The evaluation of the proposed UE and RIS state estimator. The power splitting factor is set to $\rho = 0.5$. (a) The RMSE of the position estimations;
(b) The PMSE of the HDIS's rotation matrix estimation (b) The KNISE of the TIKES S foldfort matrix estimation, (b) The RMSE of the HRIS's rotation matrix estimation. (b) The RMSE of the HRIS's rotation matrix estimation. (b) The RMSE of the HRIS's rotation matrix estimation.

Fig. 5: The role HRIS position estimation on the UE positioning accuracy, and vice versa. The HRIS common power splitting factor and the BS transmit power were set to $\rho = 0.5$ and $P_{\rm B} = 15$ dBm, respectively.

the HRIS rotation matrix are estimated based on solving the triangle formed by the BS, HRIS, and UE, and the relative angle between the BS-HRIS AOA and the HRIS-UE AOD is independent of having prior knowledge of the HRIS rotation. the UE and HRIS estimated positions (see Sec. IV-D). On the contrary, the estimation of the HRIS orientation uses

C. The Role of the HRIS Power Splitting Ratio ρ

We investigate the effect of ρ on the estimation accuracy in Figs. ?? and ??. As previously demonstrated, the sensing/reception power at the HRIS improves with increasing μ . Therefore, as it can be observed, when the value of increases, the corresponding CRBs of the BS-HRIS channel $\overline{\text{h}}$ corometers' estimation (i.e., $\overline{\text{ANER}}$ and $\overline{\text{TRR}}$ parameters' estimation (i.e., ADEB_{BR}, AAEB_{RB}, and TEB_{BR}) $ρ$. Therefore, as it can be observed, when the value of $ρ$ decline. Furthermore, we can see that the CRB of the HRIS-UE channel parameters exhibits a high error variance as ρ

 10 The role of passive RISs in localizing UEs has been studied in the literature, e.g., [15], [29]. In this paper, we focus on the joint estimation of the HRIS state and UE position, and leave the investigation on the UE localization accuracy improvement with an HRIS, as compared to a solely reflective RIS [51], for a future work.

Fig. 6: The effect of the HRIS common power splitting ratio ρ on the Fig. 6: The effect of the HRIS common power splitting ratio p on the estimation performance when the BS transmit power is set to $P_B = 25$ dBm. estimation performance when the BS transmit power is set to $P_B = 25$ dBm.
(a) The effect on the position TOA and rotation matrix estimations: (b) The (a) The effect on the position, TOA, and rotation matrix estimations; (b) The effect on the angles estimations effect on the angles estimations. effect on the angles estimations. effect on the angles estimations.

increases. We also observe that, as ρ tends to zero, the signal processed at the FIKES becomes very weak, and the error in the estimation of the BS-HRIS delay, AOD, and AOA increases. Δ a sum attach the DFD and OFD of the HRIS-decreases. μ s capecica, inc TED and OED of the OE degrade as went. $\frac{1}{2}$ conversely, when ρ tends to one, the signal received by the OE was the BB TIRB be this becomes very weak, and the error In the corresponding delay and $10D$, increases, again arrecting $\frac{A}{B}$ and OEB of the OE, Therefore, there is a value of p
that minimizes the DEB and the OEB which is not necessarily Converse to the signal the SED, which is not hecessarily $\alpha = 0.5$ looks to a reasonable performance trade officiently possible corrected to contain the correct matter of the correction behavior has been observed for full channel state information t_{eff} and t_{eff} and t_{eff} and t_{eff} and t_{eff} and t_{eff} are intermediated. $\sum_{i=1}^{\infty}$ processed at the HRIS becomes very weak, and the error in the As expected, the PEB and OEB of the UE degrade as well. Conversely, when ρ tends to one, the signal received by the UE via the BS-HRIS-UE link becomes very weak, and the error in the corresponding delay and AOD increases, again affecting the PEB and OEB of the UE. Therefore, there is a value of ρ that minimizes the PEB and the OEB, which is not necessarily the same for both metrics. Roughly speaking a value around $\rho = 0.5$ leads to a reasonable performance trade-off; similar behavior has been observed for full channel state information $testimation$ [42].

D. The Impact of SPs on the Estimation Performance

We finally investigate the robustness of the proposed estimation approach in the presence of additional SPs in the wireless of the state parameters for 20 realizations of the SP positions. tation $N_e \triangleq N_e + N_e$. The SPs in the BS-UE link are randomly distributed in the channel environment with coordirandomly distributed in the enamer environment with coordi-
nates [x_0, y_0, z_0], where $x_0 \sim \mathcal{U}(-8m, 8m)$, $y_0 \sim \mathcal{U}(0m, 3m)$, and $z_0 \sim U(-5m, 1m)$. Similarly, the SPs in the HRIS-UE and $z_0 \sim U(-5m, 1m)$. link are placed randomly in the environment with coordinates nink are placed randomly in the environment with coordinates $[x_1, y_1, z_1]$, where $x_1 \sim U(2.5m, 4.5m)$, $y_1 \sim U(4m, 11m)$, and $z_1 \sim U(-5m, 1m)$. We model the channel gain for the SPs and z_1 and z_1 and z_2 is the radar equation [64], considering that the radar according to the radar equation [64], considering that the radar α uncertaing to the Hadar equation [σ , σ], commensing that the Hadar cross-section is 1m^2 . As can be seen from both figures, the link are placed randomly in the environment with coordinates, the interference from the SPs deteriorates the estimation accuracy. Without loss of generality, we set $N_{s_0} = N_{s_1}$, and we use the notation $N_s \triangleq N_{s_0} + N_{s_1}$. The SPs in the BS-UE link are interference from the SPs deteriorates the estimation accuracy. environment. Figures 7a and 7b illustrate the estimation error

Fig. 7: The evaluation of the proposed estimator for the case where SPs exist in the BS-UE and HRIS-UE links, which are randomly distributed in $[x_0, y_0, z_0]$ and $[x_1, y_1, z_1]$, with $x_0 \sim \mathcal{U}(-8m, 8m)$, $y_0 \sim \mathcal{U}(0m, 3m)$, and [x₀, y₀, z₀] and [x₁, y₁, z₁], with x₀ ∼ *U*(−8m, 8m), y₀ ∼ *U*(0m, 3m), and z_0 ∼ *U*(4m, 11m), as well as x_1 ∼ *U*(2.5m, 4.5m) and y_1 ∼ *U*(4m, 11m), $z_0 \sim U(-5m, 1m)$, as well as $x_1 \sim U(2.5m, 4.5m)$ and $y_1 \sim U(4m, 11m)$,
 $z_1 \sim U(-5m, 1m)$. Their radar cross section is $1m^2$ and the HRIS common
nower splitting factor is set to $\rho = 0.5$ (a). The effect on the estimati $\alpha_1 \sim v_1$ om, 1m). Their radar cross section is 1m² and the HRIS common power splitting factor is set to $ρ = 0.5$. (a) The effect on the estimation of the UE and HRIS positions; and (b) The effect on the estimation of **.** \mathbf{I} and \mathbf{I} becomes positions; and \mathbf{I}

 \overline{SPs} increases. Interestingly, it is depicted that the proposed estimation performs satisfactorily even in the presence of a sumation performs satisfactority even in the presence of a ing commerce of severe is determined by a similar matter of Framing angle cannot come that the control of the proposed loss of the received signals via SPs in the HRIS-SP-UE and $SSSP-HE$ links being significantly weaker compared to the $RIS-IF$ and $RS-IF$ links respectively when considering ealistic and even large SPS with RCS of $1m^2$ relatively large outliers. This turns out to be due to the path It is shown that this accuracy degrades as the number N_s of SPs increases. Interestingly, it is depicted that the proposed large number of SPs, but is affected by a small number of relatively large outliers. This turns out to be due to the path BS-SP-UE links being significantly weaker compared to the presence of a presence o HRIS-UE and BS-UE links, respectively, when considering realistic and even large SPS with RCS of $1m^2$.

VI CONCLUSIONS \mathbf{v} of the received signals via SPs in the HRIS-SPS in t VI. CONCLUSIONS

BS-SP-UE links being significantly weaker compared to the In this paper, we presented a multi-stage estimator for the $\frac{1}{2}$ unknown 3D rotation matrix and 3D position of a single- $\sum_{n=1}^{\infty}$ The proposed estimation approach exploits the geometrical In the proposed estimation approach exproses the geometrical channel features to effectively estimate the unknown state parameters. Our simulation results confirmed the validity of parameters: our simulation results committed the varially of the presented approach and showcased that the RMSE of the are presented approach and showcased and the ranks of the estimations attains the corresponding CRBs within a certain The proposed estimation and the proposition geometrical contains the contains the corresponding of the geometrical contains the containing of the geometrical contains the containing α antenna UE in a multi-carrier system with a multi-antenna BS. transmit power range. Moreover, it was demonstrated that the RX-RF HRIS and the unknown 3D position of a singleHRIS power splitting ratio between the reflecting and sensing operations of the hybrid meta-atoms plays a critical role on the overall estimation accuracy. It was finally demonstrated that the proposed joint 3D user and 6D HRIS localization method is robust enough when additional scatter points (SPs) are present in the wireless propagation environment under investigation.

APPENDIX A DERIVATION OF J_c

To calculate J_{ζ} in (13), we need to compute $\partial \mu_{t,k}/\partial \zeta =$ $\left[\partial[\mu_{R,t}]_k/\partial\zeta,\partial[\mu_{U,t}]_k/\partial\zeta\right]^{\top} \in \mathbb{C}^{17}$. By considering the noise-free parts of the observations at the HRIS and the UE, as given by (5) and (6), we can derive the following expressions:

$$
\frac{\partial [\boldsymbol{\mu}_{R,t}]_k}{\partial \tau_{BR}} = g_{BR} \sqrt{\rho P_B} [\dot{\mathbf{d}}(\tau_{BR})]_k \mathbf{c}_t^\top \mathbf{a}_R(\boldsymbol{\phi}_{RR}) \mathbf{a}_B^\top(\boldsymbol{\theta}_{BR}) \mathbf{f}_t,
$$
\n(52a)

$$
\frac{\partial [\boldsymbol{\mu}_{\text{u},t}]_k}{\partial \tau_{\text{BR}}} = 0, \quad \frac{\partial [\boldsymbol{\mu}_{\text{R},t}]_k}{\partial \tau_{\text{BU}}} = 0, \quad \frac{\partial [\boldsymbol{\mu}_{\text{R},t}]_k}{\partial \tau_{\text{BRU}}} = 0, \quad (52b)
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\mathsf{U},t}]_k}{\partial \tau_{\mathsf{BU}}} = g_{\mathsf{BU}} \sqrt{P_{\mathsf{B}}} [\dot{\mathbf{d}}(\tau_{\mathsf{BU}})]_k \mathbf{a}_{\mathsf{B}}^\top (\boldsymbol{\theta}_{\mathsf{BU}}) \mathbf{f}_t, \qquad (52c)
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\mathbf{U},t}]_k}{\partial \tau_{\text{BRU}}} = g_{\text{BRU}} \sqrt{(1-\rho) P_{\text{B}}} [\dot{\mathbf{d}}(\tau_{\text{BRU}})]_k \mathbf{a}_k^\top (\boldsymbol{\theta}_{\text{RU}})
$$

diag $(\gamma_t) \mathbf{a}_k (\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_k^\top (\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_t,$ (52d)

$$
\frac{\partial [\boldsymbol{\mu}_{R,t}]_k}{\partial [\boldsymbol{\theta}_{BR}]_i} = g_{BR} \sqrt{\rho P_B} [\mathbf{d}(\tau_{BR})]_k \mathbf{c}_t^\top \mathbf{a}_R (\boldsymbol{\phi}_{RB}) \frac{\partial \mathbf{a}_B^\top (\boldsymbol{\theta}_{BR})}{\partial [\boldsymbol{\theta}_{BR}]_i} \mathbf{f}_t
$$

$$
\forall i \in \{\text{el}, \text{az}\}, \tag{52e}
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\text{\tiny U},t}]_k}{\partial [\boldsymbol{\theta}_{\text{\tiny BR}}]_i} = g_{_{\text{\tiny BRU}}}\sqrt{(1-\rho)\,P_{\text{B}}}[\mathbf{d}(\,\tau_{_{\text{\tiny BRU}}})\,]_k \mathbf{a}_{_{\text{\tiny R}}}^\top(\,\boldsymbol{\theta}_{_{\text{\tiny RD}}})\,\text{diag}(\,\boldsymbol{\gamma}_{_t})
$$

$$
\mathbf{a}_{\scriptscriptstyle{\mathrm{R}}}(\boldsymbol{\phi}_{\scriptscriptstyle{\mathrm{RB}}})\,\frac{\partial \mathbf{a}_{\scriptscriptstyle{\mathrm{B}}}^{\top}(\boldsymbol{\theta}_{\scriptscriptstyle{\mathrm{BR}}})}{\partial [\boldsymbol{\theta}_{\scriptscriptstyle{\mathrm{BR}}}]_i}\mathbf{f}_{\scriptscriptstyle{t}} \quad \forall i \in \{\mathrm{el}, \mathrm{az}\},\tag{52f}
$$

$$
\frac{\partial [\boldsymbol{\mu}_{R,t}]_k}{\partial \boldsymbol{\theta}_{BU}} = \mathbf{0}_2^{\top}, \text{ and } \frac{\partial [\boldsymbol{\mu}_{R,t}]_k}{\partial \boldsymbol{\theta}_{RU}} = \mathbf{0}_2^{\top},
$$
(52g)

$$
\frac{\partial [\boldsymbol{\mu}_{\mathbf{U},t}]_k}{\partial [\boldsymbol{\theta}_{\mathbf{B}\mathbf{U}}]_i} = g_{\mathbf{B}\mathbf{U}} \sqrt{P_{\mathbf{B}}} [\mathbf{d}(\tau_{\mathbf{B}\mathbf{U}})]_k \frac{\partial \mathbf{a}_{\mathbf{B}}^{\perp} (\boldsymbol{\theta}_{\mathbf{B}\mathbf{U}})}{\partial [\boldsymbol{\theta}_{\mathbf{B}\mathbf{U}}]_i} \mathbf{f}_t \quad \forall i \in \{\text{el}, \text{az}\},\tag{52h}
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\text{U},t}]_k}{\partial [\boldsymbol{\theta}_{\text{RU}}]_i} = g_{\text{BRU}} \sqrt{(1-\rho) P_{\text{B}}} [\mathbf{d}(\tau_{\text{BRU}})]_k \frac{\partial \mathbf{a}_{\text{R}}^{\top}(\boldsymbol{\theta}_{\text{RU}})}{\partial [\boldsymbol{\theta}_{\text{RU}}]_i} \operatorname{diag}(\boldsymbol{\gamma}_t)
$$

$$
\mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^{\top}(\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_t \quad \forall i \in \{\text{el}, \text{az}\},\tag{52i}
$$

$$
\frac{\partial [\mu_{R,t}]_k}{\partial [\phi_{RB}]_i} = g_{BR} \sqrt{\rho P_B} [\mathbf{d}(\tau_{BR})]_k \mathbf{c}_t^{\top} \frac{\partial \mathbf{a}_R (\phi_{RB})}{\partial [\phi_{RB}]_i} \mathbf{a}_B^{\top} (\theta_{BR}) \mathbf{f}_t
$$

\forall i \in \{\text{el}, \text{az}\}, (52j)

$$
\frac{\partial [\boldsymbol{\mu}_{\mathbf{U},t}]_k}{\partial [\boldsymbol{\phi}_{\mathbf{RB}}]_i} = g_{\text{BRU}} \sqrt{(1-\rho) P_{\text{B}}} [\mathbf{d}(\tau_{\text{BRU}})]_k \mathbf{a}_{\mathbf{R}}^\top (\boldsymbol{\theta}_{\mathbf{RU}}) \text{ diag}(\boldsymbol{\gamma}_t)
$$

$$
\frac{\partial \mathbf{a}_{\mathbf{R}}(\boldsymbol{\phi}_{\mathbf{RB}})}{\partial [\boldsymbol{\phi}_{\mathbf{RB}}]_i} \mathbf{a}_{\mathbf{B}}^\top (\boldsymbol{\theta}_{\mathbf{BR}}) \mathbf{f}_t \quad \forall i \in \{\text{el}, \text{az}\}, \tag{52k}
$$

$$
\frac{\partial [\boldsymbol{\mu}_{R,t}]_k}{\partial \mathbf{g}_{\scriptscriptstyle{BR}}} = \mathbf{e}^\top \otimes \sqrt{\rho P_{\scriptscriptstyle{B}}} [\mathbf{d}(\tau_{\scriptscriptstyle{BR}})]_k \mathbf{c}_t^\top \mathbf{a}_{\scriptscriptstyle{R}}(\boldsymbol{\phi}_{\scriptscriptstyle{RB}}) \mathbf{a}_{\scriptscriptstyle{B}}^\top (\boldsymbol{\theta}_{\scriptscriptstyle{BR}}) \mathbf{f}_t,
$$
\n(52l)

$$
\frac{\partial [\boldsymbol{\mu}_{\mathbf{U},t}]_k}{\partial \mathbf{g}_{\mathbf{B}\mathbf{R}}} = \mathbf{0}_2^\top, \frac{\partial [\boldsymbol{\mu}_{\mathbf{R},t}]_k}{\partial \mathbf{g}_{\mathbf{B}\mathbf{U}}} = \mathbf{0}_2^\top, \frac{\partial [\boldsymbol{\mu}_{\mathbf{R},t}]_k}{\partial \mathbf{g}_{\mathbf{B}\mathbf{U}}} = \mathbf{0}_2^\top, \qquad (52m)
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\mathsf{U},t}]_k}{\partial \mathbf{g}_{\mathsf{BU}}} = \mathbf{e}^\top \otimes \sqrt{\rho P_{\mathsf{B}}} [\mathbf{d}(\tau_{\mathsf{BU}})]_k \mathbf{a}_{\mathsf{B}}^\top (\boldsymbol{\theta}_{\mathsf{BU}}) \mathbf{f}_t, \tag{52n}
$$

$$
\frac{\partial [\boldsymbol{\mu}_{\mathbf{u},t}]_k}{\partial \mathbf{g}_{\text{BRU}}} = \mathbf{e}^\top \otimes \sqrt{(1-\rho) P_{\text{B}}} [\mathbf{d}(\tau_{\text{BRU}})]_k \mathbf{a}_k^\top (\boldsymbol{\theta}_{\text{RU}}) \operatorname{diag}(\boldsymbol{\gamma}_t)
$$

$$
\mathbf{a}_{\text{R}}(\boldsymbol{\phi}_{\text{RB}}) \mathbf{a}_{\text{B}}^\top (\boldsymbol{\theta}_{\text{BR}}) \mathbf{f}_t, \qquad (520)
$$

where $\dot{\mathbf{d}}(\tau) \triangleq -\jmath 2\pi \Delta_f [0, \ldots, k-1]^\top \odot \mathbf{d}(\tau)$, $\mathbf{e} \triangleq [1, \jmath]^\top$, and $\forall i \in \{el, az\}$:

$$
\frac{\partial \mathbf{a}(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_i} = \frac{\partial \mathbf{a}_r(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_i} \otimes \mathbf{a}_c(\boldsymbol{\psi}) + \mathbf{a}_r(\boldsymbol{\psi}) \otimes \frac{\partial \mathbf{a}_c(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_i}.
$$
 (53)

By using (11a) and (11b), and the notation m \triangleq [−(M − $1)/2, ..., (M-1)/2$ ^{\perp} with $M \in \{M_{\rm B}, M_{\rm R}\}\,$, we can write:

$$
\frac{\partial \mathbf{a}_r(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_{el}} = -j \frac{2\pi d}{\lambda} \cos [\boldsymbol{\psi}]_{el} \cos [\boldsymbol{\psi}]_{ax} \mathbf{m} \odot \mathbf{a}_r(\boldsymbol{\psi}), \quad (54a)
$$

$$
\frac{\partial \mathbf{a}_r(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_{\scriptscriptstyle \rm ax}} = \jmath \frac{2\pi d}{\lambda} \sin [\boldsymbol{\psi}]_{\scriptscriptstyle \rm el} \sin [\boldsymbol{\psi}]_{\scriptscriptstyle \rm ax} \mathbf{m} \odot \mathbf{a}_r(\boldsymbol{\psi}), \tag{54b}
$$

$$
\frac{\partial \mathbf{a}_c(\boldsymbol{\psi})}{\partial [\boldsymbol{\psi}]_{\mathrm{el}}} = \jmath \frac{2\pi d}{\lambda} \sin [\boldsymbol{\psi}]_{\mathrm{el}} \mathbf{m} \odot \mathbf{a}_c(\boldsymbol{\psi}),\tag{54c}
$$

$$
\frac{\partial \mathbf{a}_c(\psi)}{\partial [\psi]_{\scriptscriptstyle{\text{ax}}}} = \mathbf{0}_{\scriptscriptstyle{M}}.
$$
\n(54d)

APPENDIX B DERIVATION OF T

Using (8a) and (8b), the elements of T are computed as:

$$
\mathbf{T}(1,1:3) = \frac{\partial \tau_{\text{BR}}}{\partial \mathbf{p}_{\text{R}}} = \frac{\mathbf{p}_{\text{R}} - \mathbf{p}_{\text{B}}}{c \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{R}}\|},
$$
(55a)

$$
\mathbf{T}(1,7) = \frac{\partial \tau_{_{\text{BR}}}}{\partial b_{\text{R}}} = 1, \quad \text{and} \quad \mathbf{T}(2,8) = \frac{\partial \tau_{_{\text{BU}}}}{\partial b_{\text{U}}} = 1, \tag{55b}
$$

$$
\mathbf{T}(2,4:6) = \frac{\partial \tau_{\text{BU}}}{\partial \mathbf{p}_{\text{U}}} = \frac{\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{B}}}{c \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{U}}\|},\tag{55c}
$$

$$
\mathbf{T}(3,1:3) = \frac{\partial \tau_{\text{BRU}}}{\partial \mathbf{p}_{\mathbf{R}}} = \frac{\mathbf{p}_{\mathbf{R}} - \mathbf{p}_{\mathbf{B}}}{c \|\mathbf{p}_{\mathbf{B}} - \mathbf{p}_{\mathbf{R}}\|},\tag{55d}
$$

$$
\mathbf{T}(3,4:6) = \frac{\partial \tau_{\text{BRU}}}{\partial \mathbf{p}_{\text{U}}} = \frac{\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{B}}}{c \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{U}}\|},\tag{55e}
$$

$$
\mathbf{T}(3,7:8) = \left[\frac{\partial \tau_{_{BRU}}}{\partial b_{\rm R}}, \frac{\partial \tau_{_{BRU}}}{\partial b_{\rm U}}\right] = [1,1].
$$
 (55f)

To derive the derivatives of the AOAs and AODs w.r.t. state parameters, we first introduce the following auxiliary variables:

$$
\mathbf{u}_{\scriptscriptstyle\mathrm{DR}} \triangleq \frac{\mathbf{p}_{\scriptscriptstyle\mathrm{R}}-\mathbf{p}_{\scriptscriptstyle\mathrm{B}}}{\|\mathbf{p}_{\scriptscriptstyle\mathrm{R}}-\mathbf{p}_{\scriptscriptstyle\mathrm{B}}\|} \quad \text{and} \quad \mathbf{u}_{\scriptscriptstyle\mathrm{DU}} \triangleq \frac{\mathbf{p}_{\scriptscriptstyle\mathrm{U}}-\mathbf{p}_{\scriptscriptstyle\mathrm{B}}}{\|\mathbf{p}_{\scriptscriptstyle\mathrm{U}}-\mathbf{p}_{\scriptscriptstyle\mathrm{B}}\|}, \qquad (56a)
$$

$$
\mathbf{v}_{AB} \triangleq \frac{\mathbf{p}_B - \mathbf{p}_R}{\|\mathbf{p}_B - \mathbf{p}_R\|} \quad \text{and} \quad \mathbf{v}_{DU} \triangleq \frac{\mathbf{p}_U - \mathbf{p}_R}{\|\mathbf{p}_U - \mathbf{p}_R\|}, \qquad (56b)
$$

as well as $\mathbf{u}_1 \triangleq [1, 0, 0]^\top$, $\mathbf{u}_2 \triangleq [0, 1, 0]^\top$, and $\mathbf{u}_3 \triangleq [0, 0, 1]^\top$. Then, we may rewrite the AOAs and AODs as follows [65, Appendix A]:

$$
\begin{aligned} \boldsymbol{\theta}_{\scriptscriptstyle\mathrm{BR}} &= [\theta_{\scriptscriptstyle\mathrm{BR}}^{(az)}, \theta_{\scriptscriptstyle\mathrm{BR}}^{(el)}]^\top = [\text{atan2}(\mathbf{u}_2^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DR}}, \mathbf{u}_1^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DR}}), \text{acos}(\mathbf{u}_3^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DR}})]^\top, \\ \boldsymbol{\theta}_{\scriptscriptstyle\mathrm{BU}} &= [\theta_{\scriptscriptstyle\mathrm{BU}}^{(az)}, \theta_{\scriptscriptstyle\mathrm{BU}}^{(el)}]^\top = [\text{atan2}(\mathbf{u}_2^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DU}}, \mathbf{u}_1^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DU}}), \text{acos}(\mathbf{u}_3^\top\mathbf{u}_{\scriptscriptstyle\mathrm{DU}})]^\top, \\ \boldsymbol{\phi}_{\scriptscriptstyle\mathrm{RB}} &= [\phi_{\scriptscriptstyle\mathrm{RB}}^{(az)}, \phi_{\scriptscriptstyle\mathrm{RB}}^{(el)}]^\top = [\text{atan2}(\mathbf{r}_2^\top\mathbf{v}_{\scriptscriptstyle\mathrm{AB}}), \mathbf{r}_1^\top\mathbf{v}_{\scriptscriptstyle\mathrm{AB}})), \text{acos}(\mathbf{r}_2^\top\mathbf{v}_{\scriptscriptstyle\mathrm{AB}})]^\top, \\ (57b) \\ \text{(57c)} \end{aligned}
$$

$$
\boldsymbol{\theta}_{\text{\tiny RU}} = [\theta_{\text{\tiny RU}}^{(az)}, \theta_{\text{\tiny RU}}^{(el)}]^\top = [\text{atan2}(\mathbf{r}_2^\top \mathbf{v}_{\text{\tiny DU}}, \mathbf{r}_1^\top \mathbf{v}_{\text{\tiny DU}}), \text{acos}(\mathbf{r}_3^\top \mathbf{v}_{\text{\tiny DU}})]^\top, \tag{57d}
$$

yielding the following derivatives:

$$
\frac{\partial \mathbf{u}_{\text{DR}}}{\partial \mathbf{p}_{\text{R}}} = (\mathbf{I}_3 - \mathbf{u}_{\text{DR}} \mathbf{u}_{\text{DR}}^{\top}) / \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{R}}\| \quad , \tag{58a}
$$

$$
\frac{\partial \mathbf{u}_{\text{DU}}}{\partial \mathbf{p}_{\text{U}}} = (\mathbf{I}_3 - \mathbf{u}_{\text{DU}} \mathbf{u}_{\text{DU}}^\top) / \|\mathbf{p}_{\text{B}} - \mathbf{p}_{\text{U}}\| \quad , \tag{58b}
$$

$$
\frac{\partial \mathbf{V}_{AB}}{\partial \mathbf{p}_{R}} = (\mathbf{v}_{AB} \mathbf{v}_{AB}^{\top} - \mathbf{I}_{3}) / \|\mathbf{p}_{B} - \mathbf{p}_{R}\| \quad , \tag{58c}
$$

$$
\frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{R}}} = (\mathbf{v}_{\text{DU}} \mathbf{v}_{\text{DU}}^{\top} - \mathbf{I}_{3}) / \|\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}}\|,
$$
 (58d)

$$
\frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{U}}} = (\mathbf{I}_3 - \mathbf{v}_{\text{DU}} \mathbf{v}_{\text{DU}}^\top) / \|\mathbf{p}_{\text{U}} - \mathbf{p}_{\text{R}}\| \quad , \tag{58e}
$$

$$
\frac{\partial \theta_{\text{BR}}^{(\text{az})}}{\partial \mathbf{u}_{\text{DR}}} = \frac{(\mathbf{u}_1^{\top} \mathbf{u}_{\text{DR}}) \mathbf{u}_2 - (\mathbf{u}_2^{\top} \mathbf{u}_{\text{DR}}) \mathbf{u}_1}{(\mathbf{u}_1^{\top} \mathbf{u}_{\text{DR}})^2 + (\mathbf{u}_2^{\top} \mathbf{u}_{\text{DR}})^2}, \qquad (58f)
$$

$$
\frac{\partial \theta_{\text{BR}}^{(\text{el})}}{\partial \mathbf{u}_{\text{DR}}} = -\frac{\mathbf{u}_3}{\sqrt{1 - (\mathbf{u}_3^{\top} \mathbf{u}_{\text{DR}})^2}} , \qquad (58g)
$$

$$
\frac{\partial \theta_{\text{BU}}^{(\text{az})}}{\partial \mathbf{u}_{\text{DR}}} = \frac{(\mathbf{u}_1^\top \mathbf{u}_{\text{DR}}) \mathbf{u}_2 - (\mathbf{u}_2^\top \mathbf{u}_{\text{DR}}) \mathbf{u}_1}{(\mathbf{u}_1^\top \mathbf{u}_{\text{DR}})^2 + (\mathbf{u}_2^\top \mathbf{u}_{\text{DR}})^2},
$$
(58h)

$$
\frac{\partial \theta_{BU}^{(el)}}{\partial \mathbf{u}_{DR}} = -\frac{\mathbf{u}_3}{\sqrt{1 - (\mathbf{u}_3^\top \mathbf{u}_{DR})^2}} , \qquad (58i)
$$

$$
\frac{\partial \mathbf{u}_{\text{DR}}}{\partial \theta_{\text{RU}}^{(\text{az})}} = \frac{\sqrt{1 - (\mathbf{u}_3^{\top} \mathbf{u}_{\text{DR}})^2}}{(\mathbf{r}_1^{\top} \mathbf{v}_{\text{DU}}) \mathbf{r}_2 - (\mathbf{r}_2^{\top} \mathbf{v}_{\text{DU}}) \mathbf{r}_1}
$$
\n
$$
(59)
$$

$$
\frac{\partial \theta_{\text{RU}}^{(\text{az})}}{\partial \mathbf{v}_{\text{DU}}} = \frac{(\mathbf{r}_1^{\top} \mathbf{v}_{\text{DU}}) \mathbf{r}_2 - (\mathbf{r}_2^{\top} \mathbf{v}_{\text{DU}}) \mathbf{r}_1}{(\mathbf{r}_1^{\top} \mathbf{v}_{\text{DU}})^2 + (\mathbf{r}_2^{\top} \mathbf{v}_{\text{DU}})^2} \quad , \tag{58j}
$$

$$
\frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{v}_{\text{DU}}} = -\frac{\mathbf{r}_3}{\sqrt{1 - (\mathbf{r}_3^T \mathbf{v}_{\text{DU}})^2}} \quad , \tag{58k}
$$

$$
\frac{\partial \phi_{\text{RB}}^{(\text{az})}}{\partial \mathbf{v}_{\text{AB}}} = \frac{(\mathbf{r}_1^{\top} \mathbf{v}_{\text{AB}}) \mathbf{r}_2 - (\mathbf{r}_2^{\top} \mathbf{v}_{\text{AB}}) \mathbf{r}_1}{(\mathbf{r}_1^{\top} \mathbf{v}_{\text{AB}})^2 + (\mathbf{r}_2^{\top} \mathbf{v}_{\text{AB}})^2},
$$
(581)

$$
\frac{\partial \phi_{\text{RB}}^{(\text{el})}}{\partial \phi_{\text{RB}}^{(\text{el})}} = -\frac{\mathbf{r}_3}{\sqrt{1-\mathbf{r}_3}}
$$

$$
\frac{\partial \varphi_{RB}}{\partial \mathbf{v}_{AB}} = -\frac{\mathbf{I}3}{\sqrt{1 - (\mathbf{r}_3^T \mathbf{v}_{AB})^2}}, \qquad (58m)
$$
\n
$$
\partial \phi_{BB}^{(az)} = (\mathbf{r}_1^T \mathbf{v}_{AB}) \mathbf{v}_{AB} \mathbf{u}_2^T - (\mathbf{r}_2^T \mathbf{v}_{AB}) \mathbf{v}_{AB} \mathbf{u}_1^T
$$

$$
\frac{\partial \phi_{RB}^{(az)}}{\partial \mathbf{R}} = \frac{(\mathbf{r}_1^{\top} \mathbf{v}_{AB}) \mathbf{v}_{AB} \mathbf{u}_2^{\top} - (\mathbf{r}_2^{\top} \mathbf{v}_{AB}) \mathbf{v}_{AB} \mathbf{u}_1^{\top}}{(\mathbf{r}_1^{\top} \mathbf{v}_{AB})^2 + (\mathbf{r}_2^{\top} \mathbf{v}_{AB})^2}, \qquad (58n)
$$

$$
\frac{\partial \phi_{\text{RB}}^{(\text{el})}}{\partial \mathbf{R}} = -\frac{\mathbf{v}_{\text{AB}} \mathbf{u}_3^{\top}}{\sqrt{1 - (\mathbf{r}_3^{\top} \mathbf{v}_{\text{AB}})^2}} , \qquad (58o)
$$

$$
\frac{\partial \theta_{\text{\tiny{RU}}}^{\text{(az)}}}{\partial \mathbf{R}} = \frac{(\mathbf{r}_1^\top \mathbf{v}_{\text{du}}) \mathbf{v}_{\text{du}} \mathbf{u}_2^\top - (\mathbf{r}_2^\top \mathbf{v}_{\text{du}}) \mathbf{v}_{\text{du}} \mathbf{u}_1^\top}{(\mathbf{r}_1^\top \mathbf{v}_{\text{du}})^2 + (\mathbf{r}_2^\top \mathbf{v}_{\text{du}})^2}, \qquad (58p)
$$

$$
\frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{R}} = -\frac{\mathbf{v}_{\text{DU}} \mathbf{u}_3^{\top}}{\sqrt{1 - (\mathbf{r}_3^{\top} \mathbf{v}_{\text{DU}})^2}} , \qquad (58q)
$$

The latter expressions are used to compute the following elements of
$$
T
$$
 (with those remaining being zero):

$$
\mathbf{T}(4,1:3) = \frac{\partial \theta_{_{\text{BR}}}^{(az)}}{\partial \mathbf{p}_{\text{R}}} = \frac{\partial \theta_{_{\text{BR}}}^{(az)}}{\partial \mathbf{u}_{_{\text{DR}}}} \frac{\partial \mathbf{u}_{_{\text{DR}}}}{\partial \mathbf{p}_{\text{R}}},
$$
(59a)

$$
\mathbf{T}(5,1:3) = \frac{\partial \theta_{\text{BR}}^{(\text{el})}}{\partial \mathbf{p}_{\text{R}}} = \frac{\partial \theta_{\text{BR}}^{(\text{el})}}{\partial \mathbf{u}_{\text{DR}}} \frac{\partial \mathbf{u}_{\text{DR}}}{\partial \mathbf{p}_{\text{R}}},
$$
(59b)

$$
\mathbf{T}(6, 4:6) = \frac{\partial \theta_{BU}^{(az)}}{\partial \mathbf{p}_U} = \frac{\partial \theta_{BU}^{(az)}}{\partial \mathbf{u}_{DU}} \frac{\partial \mathbf{u}_{DU}}{\partial \mathbf{p}_U},
$$
(59c)

$$
\mathbf{T}(7,4:6) = \frac{\partial \theta_{BU}^{(el)}}{\partial \mathbf{p}_U} = \frac{\partial \theta_{BU}^{(el)}}{\partial \mathbf{u}_{DU}} \frac{\partial \mathbf{u}_{DU}}{\partial \mathbf{p}_U},
$$
(59d)

$$
\mathbf{T}(8,1:3) = \frac{\partial \theta_{\text{RU}}^{(ax)}}{\partial \mathbf{p}_{\text{R}}} = \frac{\partial \theta_{\text{RU}}^{(ax)}}{\partial \mathbf{v}_{\text{DU}}} \frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{R}}},
$$
(59e)

$$
\mathbf{T}(9,1:3) = \frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{p}_{\text{R}}} = \frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{v}_{\text{DU}}} \frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{R}}},
$$
(59f)

$$
\mathbf{T}(8,4:6) = \frac{\partial \theta_{\text{RU}}^{(ax)}}{\partial \mathbf{p}_{\text{U}}} = \frac{\partial \theta_{\text{RU}}^{(ax)}}{\partial \mathbf{v}_{\text{DU}}} \frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{U}}},
$$
(59g)

$$
\mathbf{T}(9,4:6) = \frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{p}_{\text{U}}} = \frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{v}_{\text{DU}}} \frac{\partial \mathbf{v}_{\text{DU}}}{\partial \mathbf{p}_{\text{U}}},
$$
(59h)

$$
\mathbf{T}(10,1:3) = \frac{\partial \phi_{_{RB}}^{(az)}}{\partial \mathbf{p}_{R}} = \frac{\partial \phi_{_{RB}}^{(az)}}{\partial \mathbf{v}_{_{AB}}} \frac{\partial \mathbf{v}_{_{AB}}}{\partial \mathbf{p}_{R}},
$$
(59i)

$$
\mathbf{T}(11,1:3) = \frac{\partial \phi_{\text{RB}}^{(\text{el})}}{\partial \mathbf{p}_{\text{R}}} = \frac{\partial \phi_{\text{RB}}^{(\text{el})}}{\partial \mathbf{v}_{\text{AB}}} \frac{\partial \mathbf{v}_{\text{AB}}}{\partial \mathbf{p}_{\text{R}}},
$$
(59j)

$$
\mathbf{T}(8,9:17) = \frac{\partial \theta_{\text{RU}}^{(\text{az})}}{\partial \mathbf{R}}, \quad \text{and } \mathbf{T}(9,9:17) = \frac{\partial \theta_{\text{RU}}^{(\text{el})}}{\partial \mathbf{R}}, \tag{59k}
$$

$$
\mathbf{T}(10,9:17) = \frac{\partial \phi_{_{\mathbf{RB}}}^{(\text{az})}}{\partial \mathbf{R}}, \quad \text{and } \mathbf{T}(11,9:17) = \frac{\partial \phi_{_{\mathbf{RB}}}^{(\text{el})}}{\partial \mathbf{R}}.
$$
 (591)

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