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# Competing High-Temperature Deformation Mechanisms in Mo(Si,AI)<sub>2</sub>–Al<sub>2</sub>O<sub>3</sub> Composites



AINA EDGREN, ERIK STRÖM, and MAGNUS HÖRNQVIST COLLIANDER

 $Mo(Si,Al)_2-Al_2O_3$  composites were tested in four-point bending at 1300 °C. The addition of  $Al_2O_3$  led to a decrease in grain size, and a subsequent decrease in strength for materials containing up to 15 wt pct  $Al_2O_3$ . At higher  $Al_2O_3$  fractions, the decrease in grain size saturates and the strength is recovered as the  $Al_2O_3$  particles prevent grain boundary sliding.

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 $MO(SI,AL)_2$  is a ceramic material with high resistivity, high melting point and excellent oxidation properties in both oxidizing and reducing environments.<sup>[1-4]</sup> The main application is as heating elements in electrical furnaces. Therefore, the material is often considered to be a cornerstone in the ongoing process of reducing the emission of greenhouse gasses, facilitating the transition from fossil-gas-driven furnaces to electrical alternatives. However, an inherent challenge lies in the mechanical properties of Mo(Si,Al)<sub>2</sub>.

Mo(Si,Al)<sub>2</sub> has a high ductile to brittle transition temperature (DBTT), 1250 °C for polycrystalline C40, above which the yield stress decreases rapidly with an increase in temperature.<sup>[5,6]</sup> The low yield stress becomes problematic when scaling up the size of heating elements for industrial furnaces operating in the MW range, as the gravitational force on the elements increases, potentially leading to excessive deformation.

In order to make  $Mo(Si,Al)_2$  suitable for use as large heating elements, the mechanical properties need to be both understood and improved. A promising way to improve the high-temperature strength is the addition of a secondary phase, as this could provide a particle-strengthening effect. This strategy has proven successful in  $MoSi_2$ , a material similar to  $Mo(Si,Al)_2$ .<sup>[7–13]</sup> We have previously investigated the effects of particle additions on the mechanical properties of  $Mo(Si,Al)_2$ through compression testing of  $Mo(Si,Al)_2-Al_2O_3$  composites (containing 0 to 25 wt pct  $Al_2O_3$ ) at 1300 °C<sup>[14,15]</sup> using a Gleeble thermomechanical simulator.

The addition of  $Al_2O_3$  led to a decrease in strength for additions up to 15 wt pct, whereas higher  $Al_2O_3$ contents (20 and 25 wt pct) led to a recovery of the strength. The addition of  $Al_2O_3$  particles reduced the grain size, and the fine-grained  $Mo(Si,Al)_2-Al_2O_3$  composites did not show the same extent of intergranular misorientation as the coarse-grained  $Al_2O_3$ -free material in the deformed state. It was therefore suggested that the decreasing grain size caused a transition in the deformation mechanism from dislocation slip to diffusion-based creep. This could partly explain the initial reduction in strength when 5 wt pct  $Al_2O_3$  was added, but for higher additions, the measured grain size remained constant, while the strength continued to decrease until the minimum at 15 wt pct.

This suggests that there are other mechanisms at play, and it was hypothesized that electroplasticity, caused by the resistive heating used in the Gleeble, played a role. In both ceramics and metals, it has been shown that electroplasticity locally heats and creates charge imbalance over grain boundaries, thereby locally weakening bonds<sup>[16–19]</sup> and promoting grain boundary sliding. Given that the effective conductive area in a cross-section decreases with the addition of Al<sub>2</sub>O<sub>3</sub> with negligible electric conductivity, electroplasticity effects were proposed to become more pronounced with increasing additions. Simultaneously, however, the increased addition of particles, which primarily reside on grain boundaries due to the processing route, will lead to particle strengthening through pinning of the boundaries. At higher Al<sub>2</sub>O<sub>3</sub> contents (20 and 25 wt pct), the strengthening effect of the Al<sub>2</sub>O<sub>3</sub> particles outweighed the proposed electroplasticity-induced softening, resulting in improved performance compared to Al<sub>2</sub>O<sub>3</sub> lean materials.

Electroplasticity-induced softening could be detrimental to the use of Mo(Si,Al)<sub>2</sub> as resistive heating elements.

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Table I. Average Density of the Sintered Materials

| Material | Wt Pct Mo (Si,Al) <sub>2</sub> | Wt Pct Al <sub>2</sub> O <sub>3</sub> | Density (g $cm^{-3}$ ) | Pct of Theoretical Density |
|----------|--------------------------------|---------------------------------------|------------------------|----------------------------|
| A5       | 95                             | 5                                     | 5.75                   | 98.1                       |
| A15      | 85                             | 15                                    | 5.49                   | 98.2                       |
| A25      | 75                             | 25                                    | 5.21                   | 97.7                       |
| A30      | 70                             | 30                                    | 5.10                   | 97.5                       |

In order to test the electroplasticity hypothesis, mechanical testing of  $Mo(Si,Al)_2$ – $Al_2O_3$  composites with varying particle content must be performed without electric heating. Here we perform four-point bending tests of composites containing 5 to 30 wt pct  $Al_2O_3$  at 1300 °C. The specimens were heated by external radiative heating instead of resistive heating to avoid electroplasticity. The composites were prepared from the same  $Mo(Si,Al)_2$  and  $Al_2O_3$  powders as the composites investigated in References 15 and 14, and synthesized in an identical way.

Mo(Si,Al)<sub>2</sub> was synthesized by dry mixing of elemental Mo (99.9 pct purity, Cerac Inc.), Si (99.99 pct purity, Wacker) and Al (99.5 pct purity, GoodFellow) powders in a Mo-lined ball mill with Mo balls. The powder mixture was heated in inert Ar gas to initiate a self-propagating reaction in which Mo(Si,Al)<sub>2</sub>, as well as small amounts of Mo<sub>5</sub>(Si,Al)<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> (approximately 1.7 vol pct<sup>[14]</sup>), were formed. The reaction product underwent milling in an Mo metal ball mill for 228 hours to achieve a fine-grained powder with an average particle size of approximately 5  $\mu$ m.

Four Mo(Si,Al)<sub>2</sub>–Al<sub>2</sub>O<sub>3</sub> composites, containing 5, 15, 25 and 30 wt pct Al<sub>2</sub>O<sub>3</sub> respectively, were prepared by adding Al<sub>2</sub>O<sub>3</sub> particles (AKP-53, Sumitomo Chemical, purity: 99.99 pct) to the milled Mo(Si,Al)<sub>2</sub> powder. To prevent agglomeration of the Al<sub>2</sub>O<sub>3</sub> particles, the powders were milled for 1 minutes in a vibratory steel disc mill. The powders were compacted to rods using a cold isostatic press (CIP, EPSI) operating at 2000 bar, prior to sintering for 1 hour at 1650 °C in H<sub>2</sub> gas in a tube furnace. The as-sintered materials had densities (measured using Archimedes' method) of around 98 pct of the theoretical values, see Table I.

The rods were cut and ground to bars  $(3 \times 4 \times 50 \text{ mm}^3)$ . For each composite, at least five bars were subjected to high-temperature four-point bending tests at Fraunhofer IKTS in Dresden, Germany, in a vacuum of  $10^{-5}$  mbar at 1300 °C, using a Shimadzu AG-20kNG testing machine. The tests were carried out according to the DIN EN 820-1 standard. The cross-head speed was 0.5 mm min<sup>-1</sup> (initial strain rate was  $1.25 \times 10^{-4} \text{ s}^{-1}$ ), the loading span 20 mm and the support span 40 mm. The deflection was measured at the loading points. The maximum deflection was around 1 mm due to the geometric constraints of the test rig.

For materials characterization, an FEI Quanta 200 FEG ESEM scanning electron microscope (SEM) operating at 20 kV was used for microstructure imaging and chemical composition analysis using energy-dispersive X-ray spectroscopy (EDS). Electron backscatter diffraction (EBSD) was used for additional microstructural investigation in a Tescan GAIA 3 SEM operating at an acceleration voltage of 15 kV.

The chemical composition of  $Mo(Si,Al)_2$  was 32 at. pct Mo, 37 at. pct Si, 29 at. pct Al, as well as small amounts of O, C and Fe (< 0.03 at. pct). Phase maps acquired using EBSD are shown in Figure 1. The phase volume fractions of the composites are shown in Table II. Two  $Mo_5(Si,Al)_3$  phases, with  $D8_m$  and  $D8_8$ structure, were present in small amounts.  $D8_m$  is commonly reported in  $Mo(Si,Al)_2$  materials and is a result of local chemical variations in the unreacted powder,<sup>[4,20,21]</sup> whereas  $D8_8$  is stabilized by  $C^{[22-24]}$  and presumably a result of contaminations during synthesis. Although the volume fractions of the minority phases differed slightly between materials, the low volume fractions are not expected to significantly affect the mechanical properties of the composites.

The grain size histograms in Mo(Si,Al)<sub>2</sub> in Figure 1 show that A15, A25 and A30 have relatively similar grain sizes, while the grains in A5 are slightly larger because of grain growth during sintering. The grain sizes in this study should also be compared with those reported in References 15 and 14 as the materials were synthesized identically. The 5 wt pct  $Al_2O_3$  containing composite in Reference 15 was reported to have a grain size of 7.1  $\mu$ m, which is significantly smaller than that reported for 5 wt pct addition here. Additional EBSD investigations were therefore performed on the 5 wt pct sample. The average grain sizes from individual EBSD maps varied significantly, with values as high as 10.0  $\mu$ m. This indicates that an addition of 5 wt pct is not enough to obtain a homogeneous microstructure. The higher Al<sub>2</sub>O<sub>3</sub>-containing composites had a smaller and more even grain size, as grain boundary pinning by the oxide particles limits grain growth during sintering, although the distribution was somewhat broader in the material with 15 wt pct Al<sub>2</sub>O<sub>3</sub> compared to 25 and 30 wt pct, see Figure 1 and Reference 15.

All composites exhibited plastic deformation during four-point bending testing. A photo of a tested A5 specimen is shown in Figure 2(a). Optical microscopy (OM) did not show any cracks on the surface. The flexural stress,  $\sigma_f$ , was calculated using Eq. [1]<sup>[25]</sup>

$$\sigma_f = \frac{3}{4} \frac{FL}{bd^2}$$
[1]

where F is the force, b is the sample width and d is the thickness of the bending bar. The equation is valid for bending bars having a load span of 1/2 of the support

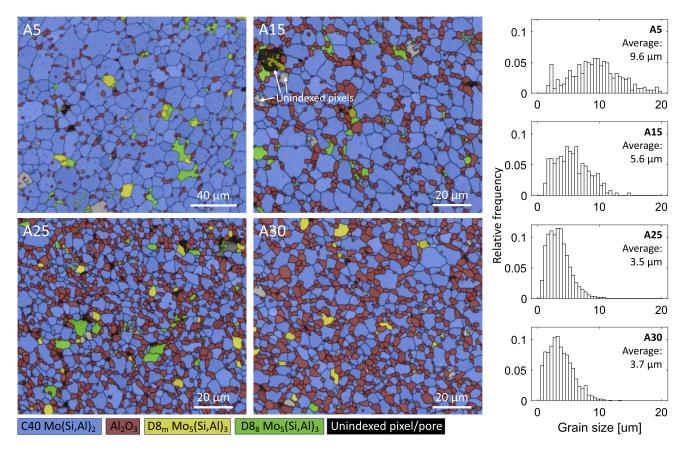


Fig. 1—EBSD phase maps and grain size histograms of A5, A15, A25, A30. Note the different magnification for the map of A5 compared to the other materials.

|          |                               | ]  |   |   |                         |  |
|----------|-------------------------------|--|---|---|-------------------------|--|
| Material | C40<br>Mo(Si,Al) <sub>2</sub> | $\alpha$ -Al <sub>2</sub> O <sub>3</sub> | D8 <sub>m</sub><br>Mo <sub>5</sub> (Si,Al) <sub>3</sub> | D8 <sub>8</sub><br>Mo <sub>5</sub> (Si,Al) <sub>3</sub> | Pores or Not<br>Indexed | -<br>Grain Size C40 [μm] (Standard<br>Deviation) |
| A5       | 84                            | 7.1                                      | 0.7   | 6.0   | 2.2                     | 9.6 (4.38)                                       |
| A15      | 69                            | 23                                       | 0.2   | 5.9   | 1.9                     | 5.6 (2.66)                                       |
| A25      | 62                            | 32                                       | 2.0   | 2.3   | 2.0                     | 3.5 (1.52)                                       |
| A30      | 57                            | 38                                       | 2.4   | 0.2   | 1.9                     | 3.7 (2.02)                                       |

Table II. Phase Volume Fraction and Grain Size, Acquired Using EBSD, of Sintered Composites

span (L) and positioned symmetrically between the supports. The resulting stress-displacement curves are shown in Figure 2(b). Small marks from the load and support rolls were visible on the tested specimens, see Figure 2(a). In the case of A5, only four curves are shown, the fifth was rejected because of misalignment of the specimen in the sample holder. It was noted that the load span was shifted by 1 mm towards one of the support rolls. This could be due to the mobility of the rollers and the rotatability of the upper punch, which are demands from the standard, in combination with thermal expansion. However, the same shift was observed for all specimens. Hence, the values in Figure 2(a) are not absolute, but still give a good estimation of the flexural stress. The data in Figure 2(a)has also been filtered using a band stop filter as the raw data was slightly affected by temperature fluctuations in the furnace. The raw data as well as further details on the data processing are found in the electronic supplementary material. The abrupt stress drops are the result of the setting of the rollers due to the thermal expansion. We note that after a stress drop, there is a "recovery" period before the stress returns to the response expected from the extrapolation of the curve before the drop.

Figure 2(b) shows that the stress levels decrease as the  $Al_2O_3$  content increases from 5 to 15 wt pct. Conversely, as  $Al_2O_3$  content increases from 15 to 25 and 30 wt pct, the stress increases. Figure 3 shows the flexural stress at two different deformation levels, corresponding to a permanent displacement of the loading rolls of 0.04 and 0.4 mm (equal to 0.2 and 2 pct of the loading span distance, respectively), as well as the maximum stress for

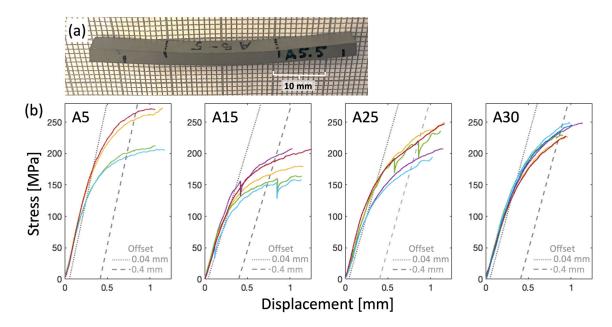


Fig. 2—(*a*) Photo of A5 specimen after deformation. The position of load and support rolls are indicated, (*b*) stress–displacement curves of the  $Mo(Si,Al)_2-Al_2O_3$  composites with lines corresponding to offsets of 0.04 and 0.4 mm, respectively.

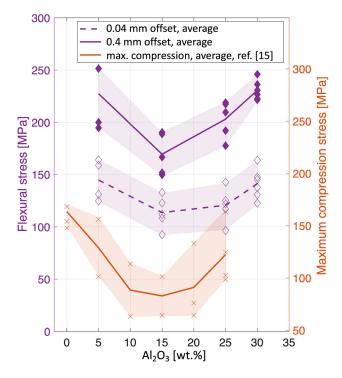


Fig. 3—Diamond marks: flexural stress values corresponding to a permanent deformation equal to a displacement of 0.04 mm (not filled) and 0.4 mm (filled) of the load span distance. Cross marks: maximum compression stress from Ref. [15]. The lines show the average stress values for the tested specimens.

the resistively heated samples from Reference 15. The same behavior, a gradual decrease in strength for composites containing up to 15 wt pct  $Al_2O_3$ , followed by an increase at higher  $Al_2O_3$  contents, is observed in both cases. As external heating, where electroplasticity cannot occur, was used in the present study, we

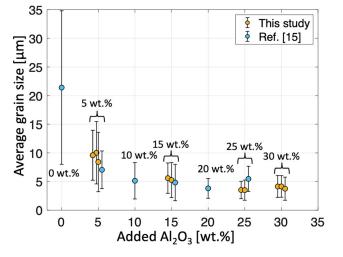


Fig. 4—Average  $Mo(Si,Al)_2$  grain size with error bars as a function of  $Al_2O_3$  content from this study and Ref. [15]. The data points have been shifted vertically for improved readability.

conclude that the deformation behavior is not controlled by electroplasticity. Instead, the decreasing strength with increasing particle fraction can be explained by the decreasing grain size (from 9.6 in A5 to 5.6  $\mu$ m in A15). Figure 4 shows the grain size as a function of wt pct Al<sub>2</sub>O<sub>3</sub> from both the current study and <sup>[15]</sup>, where the average grain size obtained from different EBSD maps is shown as separate data points. The grain size saturates around 10 to 15 wt pct, but due to the limited number of observed regions in Reference 15 we previously concluded that the saturation occurred already at around 5 wt pct, leading to the suggestion of the additional mechanism of electroplasticity. Above 15 wt pct, the grain size saturates and the particle strengthening effect dominates, where the Al<sub>2</sub>O<sub>3</sub> particles in grain

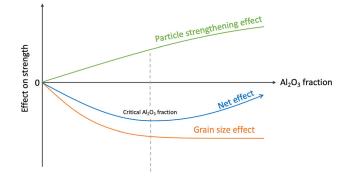


Fig. 5—Schematic illustration of the effect of grain size and  $\rm Al_2O_3$  particle strengthening on the strength.

boundaries inhibit sliding. Grain boundary sliding has been shown to be the dominating deformation mechanism in fine-grained  $MoSi_2$ ,<sup>[10,13]</sup> and is suggested to play an important role also in the deformation of  $Mo(Si,Al)_2$ , as only one slip system is active at high temperature.<sup>[26]</sup> The effect of grain size and particle strengthening on the strength as a function of added  $Al_2O_3$  is schematically shown in Figure 5.

An important consequence of the observed behavior is that, if particle additions are used solely to prevent excessive grain growth and strength is not a primary concern in the design, a volume fraction of approximately 10 to 15 pct is required. We also note that the large variation in the grain size between different regions in the sample for low fractions of Al<sub>2</sub>O<sub>3</sub> can introduce a dependence on the test method through the volume effect. In compression tests (e.g. Gleeble, used in our previous investigation<sup>[15]</sup>) the entire volume, comprising areas with both large and small grains, is subjected to a (nominally) uniform stress. During bending tests there is a stress gradient through the sample thickness, and only the outermost parts are subjected to the highest stress and will undergo plastic deformation. Consequently, while compression tests always measure the average response of regions with different grain size, the response of a bending test will depend on the grain size distribution in the limited volumes close to the outer surfaces. The presence or absence of volumes with large grains in the near-surface regions, which in the present case can be considered a statistical effect since the samples were machined from the interior of sintered rods, is expected to affect the measured strength. Hence, four-point bending might be more sensitive to an uneven grain size in the material. The volume effect is particularly important if test methods such as three-point bending are used, where there is also a gradient along the span length, and only a very small material volume experiences the maximum stress. Figure 2

While the stress trends (see Figure 3) are the same at low (0.04 mm offset) and high (0.4 mm offset) levels of deformation, the effect of  $Al_2O_3$  increases with increasing plastic deformation. At 0.04 mm offset, only the decrease between 5 and 15 wt pct was statistically significant (two-sample t-test, significance level 5 pct). For higher  $Al_2O_3$  contents, a significant difference in stress was observed only above an offset of 0.2 mm. This is reasonable as deformation primarily occurs by grain boundary sliding. To enhance understanding and model the behavior, it is important to identify the detailed deformation mechanism(s). This could be accomplished through additional experiments, such as testing the materials at different strain rates or in creep.

In summary, we have shown that:

- The dependence of the high temperature strength of Mo(Si,Al)<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> composites on the fraction of particle additions is a result of the competition between strength reduction due to grain refinement, and an increase due to grain boundary strengthening by particles. This leads to a strength minimum at intermediate fractions.
- Electroplasticity does not influence the mechanical properties of Mo(Si,Al)<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> composites, which is of importance for the use of the material as resistive heating elements.
- All Al<sub>2</sub>O<sub>3</sub> additions lead to a decrease in grain size; however, 5 wt pct is insufficient to achieve a material with a homogeneous grain size. The grain size saturates at additions of around 10 to 15 wt pct.

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## CONFLICT OF INTEREST

The authors declare the following financial interests/ personal relationships which may be considered as potential competing interests: Aina Edgren and Erik Ström are employees of Kanthal AB, a manufacturer of commercial heating elements.

### SUPPLEMENTARY INFORMATION

The online version contains supplementary material available at https://doi.org/10.1007/s11661-024-07520-7.

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