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TOI–757 b: an eccentric transiting mini–Neptune on a 17.5–d orbit

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ABSTRACT

We report the spectroscopic confirmation and fundamental properties of TOI–757 b, a mini–Neptune on a 17.5–d orbit transiting a bright star ($V = 9.7$ mag) discovered by the *TESS* mission. We acquired high–precision radial velocity measurements with the HARPS, ESPRESSO, and PFS spectrographs to confirm the planet detection and determine its mass. We also acquired space–borne transit photometry with the *CHEOPS* space telescope to place stronger constraints on the planet radius, supported with ground–based LCOGT photometry. WASP and KELT photometry were used to help constrain the stellar rotation period. We also determined the fundamental parameters of the host star. We find that TOI–757 b has a radius of $R_p = 2.5 \pm 0.1 R_\oplus$ and a mass of $M_p = 10.5^{+2.2}_{-2.1} M_\oplus$, implying a bulk density of $\rho_p = 3.6 \pm 0.8 \text{ g cm}^{-3}$. Our internal composition modelling was unable to constrain the composition of TOI–757 b, highlighting the importance of atmospheric observations for the system. We also find the planet to be highly eccentric with $e = 0.39^{+0.08}_{-0.07}$, making it one of the very few highly eccentric planets among precisely characterized mini–Neptunes. Based on comparisons to other similar eccentric systems, we find a likely scenario for TOI–757 b’s formation to be high eccentricity migration due to a distant outer companion. We additionally propose the possibility of a more intrinsic explanation for the high eccentricity due to star–star interactions during the earlier epoch of the Galactic disc formation, given the low metallicity and older age of TOI–757.

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Key words: techniques: photometric – techniques: radial velocities – planets and satellites: composition – planets and satellites: interiors – stars: individual: TOI-757 (TIC 130924120).

1 INTRODUCTION

There are two main populations of small planets, super-Earths and mini-Neptunes, separated by a gap known as the radius valley, centred around $R_p \approx 1.8 R_\oplus$ (Owen & Wu 2013; Fulton et al. 2017; Owen & Wu 2017; Ho & Van Eylen 2023). The location of the radius valley is predicted to be dependent on the internal composition of the planet, and the valley is expected to be shifted to a larger planetary radius ($R_p \approx 2.3 R_\oplus$) if the internal composition of these planets is icy rather than rocky (Jin & Mordasini 2018; Mordasini 2020). Potential explanations of the radius gap focus on atmospheric mass-loss mechanisms, which predict that the radius gap separates the super-Earth and mini-Neptune populations based on whether or not planets were able to retain their primordial hydrogen/helium atmosphere (H/He envelope). A possible explanation of the radius gap comes from thermally driven mass-loss mechanisms (also known as photoevaporation) induced by exposure to XUV irradiation from the host star (Lopez & Fortney 2013; Owen & Wu 2013). Photoevaporation models can reproduce the position of the radius valley assuming that super-Earth and mini-Neptune planets all have a rocky composition, with their different radii being a consequence of whether or not they lost their atmosphere. Another explanation proposed for the existence of the radius gap focuses on core-powered mass-loss mechanisms, which results from the internal heating of the planet (Ginzburg, Schlichting & Sari 2018; Gupta & Schlichting 2019, 2020). In the core-powered mass-loss scenario, energy escaping from the planet’s core heats up the H/He envelope and causes the atmospheric gases to escape, turning the planet into a stripped core.

We present the discovery, the confirmation, and the fundamental properties of TOI-757 b, a mini-Neptune planet located above the radius valley. The abundance of mini-Neptune planets that fall close to the radius valley is generally well-explained within the photoevaporation framework, where these planets are assumed to have rocky cores with a thin atmosphere (Bean, Raymond & Owen 2021). However, simply looking at the radius distribution of planets close to the radius valley does not give us clear insights about their densities or core compositions. For that, mass measurements and (in many cases) atmospheric observations are necessary to break the degeneracies of what the core compositions of the mini-Neptune population is comprised of (Bitsch, Raymond & Izidoro 2019). In particular, studies of their mass measurements are very important in helping constrain their densities, which could give us clues about their internal structure (Benneke & Seager 2013). In many cases however, constraints on the atmospheric chemical composition from transit spectroscopy are necessary in order to try to break the degeneracy of their internal composition (e.g. mini-Neptune versus water world).

Eccentric systems further complicate this scenario because they could suggest a different evolution path. Such planets could have become eccentric due to gravitational interactions with other planets and/or migration (Barnes et al. 2009). They may therefore have formed further out, or undergone a different migration history compared to other planets, and as such it would be interesting to see if that suggests a different photoevaporation history. To make strides towards a better understanding of the mini-Neptune population, it is important to follow them up and gain a more precise picture of their formation mechanism.

In this paper, we use multiple radial velocity (RV) monitoring campaigns to obtain a precise and accurate mass measurement of the planet, TOI-757 b. We also use space-based photometric follow-up observations of the system, allowing us to derive a more precise radius measurement of the planet, as well as additional ground-based photometric data of TOI-757. By studying the planet using both photometric and RV data, we were able to obtain a precise and accurate planet density and explore the implications of its composition. Determining the planet’s composition allows us to interpret whether TOI-757 b indeed fits within the scenario presented by atmospheric mass-loss models.

In Section 2, we describe the photometric data acquired from space-based telescopes, as well as the RV data acquired from ground-based telescopes. In Section 3, we discuss the stellar characterization of TOI-757 and present the newly derived stellar properties from this work. In Section 4, we describe how we validate the system using spaced-based astrometry as well as ground-based high-contrast imaging. In Section 5, we detail the methods for modelling and fitting the photometric and RV data sets. Finally, we present the discussions and conclusions in Section 6, with a summary of the work in Section 7.

2 OBSERVATIONS

Photometric data for TOI-757 were acquired through a combination of space-based and ground-based observations. We use four transits from the *Transiting Exoplanet Survey Satellite* (TESS) space mission, spanning three separate sectors with 120 s cadence light curves. Additionally, we acquired follow-up photometric observations of the system. We use two transits from the *CHEOPS* space telescope with 60 s cadence light curves, which allowed us to place stronger constraints on the planet radius, supported by ground-based LCOGT photometry. We also acquired WASP and KELT ground-based photometry to aid in constraining the stellar rotation period.

High-precision RV data for the exoplanetary system were collected from multiple instruments, including the HARPS, ESPRESSO, and PFS spectrographs. We acquired a total of 73 high-precision RV measurements between 2021 and 2022, to confirm the planetary nature of the transit signal detected by TESS and determine its mass measurement.

2.1 TESS

The TESS is a NASA mission aiming to discover transiting exoplanets by an all-sky survey (Ricker et al. 2015). The star TIC 130924120 was observed by TESS at a 2-min cadence in Sectors 10, 37, and 64, resulting in a total of four transit events. The raw images were reduced by the Science Processing Operations Center (SPOC) team at NASA Ames Research Center using the SPOC pipeline (Jenkins et al. 2016) and the photometry for all the 2-min target stars in the TESS field of view were extracted, resulting in light curves ready to be searched for transit signals.

The SPOC conducted a transit search for Sector 10 with a noise-compensating matched filter (Jenkins 2002; Jenkins et al. 2010, 2020) and detected the transit signature of TOI-757 b. An initial limb-darkened model fit was performed (Li et al. 2019) and

TOI–757 b was found to have a period of 17.4655 ± 0.0029 d, a radius ratio of 0.03 ± 0.01 , and a transit depth of 1064 ± 68 ppm, transiting the star over a duration of 0.16 ± 0.02 d. A suite of diagnostic tests were conducted to help make or break the planetary nature of the signal (Twicken et al. 2018). The candidate transit signature passed all these diagnostic tests including the difference image centroiding test, which constrained the location of the host star to within 2.5 ± 2.6 arcsec of the transit source. The TESS Science Office (TSO) reviewed the vetting information and issued an alert for TOI–757.01 on 2019 June 20 (Guerrero et al. 2021). In this work, we use the Presearch Data Conditioning–corrected Simple Aperture Photometry (PDCSAP) light curves of the system (Smith et al. 2012; Stumpe et al. 2012, 2014) for the transit modelling and analyses. These light curves are publicly available at the Mikulski Archive for Space Telescopes (MAST).¹

We independently analysed the *TESS* data using the Détection Spécial–isée de Transits algorithm (Cabrera et al. 2012) to confirm the presence of the candidate and ruled out any significant transit timing variations in the data. Our analysis shows that we can confidently detect planetary signals in the range of 250 to 450 ppm with orbital periods up to 20 d. This would correspond, for central transits, to planets in the range of 1.3 to 1.8 Earth radii.

2.2 Light-curve follow–up observations

The *TESS* pixel scale is approximately 21 arcsec pixel^{−1} and photometric apertures typically extend out to roughly 1 arcmin, generally causing multiple stars to blend in the *TESS* photometric aperture. To determine the true source of the *TESS* detection, we acquired ground–based LCOGT time–series follow–up photometry of the field around TOI–757 as part of the *TESS* Follow–up Observing Program (TFOP; Collins 2019).² The on–target follow–up light curves are also used to place constraints on the transit depth and the *TESS* ephemeris. We used the *TESS* TRANSIT FINDER, which is a customized version of the TAPIR software package (Jensen 2013), to schedule our transit observations. We also used WASP and KELT photometric data to search for activity signals and aid in constraining the stellar rotation period.

2.2.1 WASP

The Wide Angle Search for Planets (WASP) transit–search survey (Pollacco et al. 2006) is located at the Sutherland site of the South African Astronomical Observatory. The data were reduced using the pipeline described in Pollacco et al. (2006), with exposures that spanned 30 s (when observing with 200mm lenses) and 20 s (when observing with 85mm lenses). For data taken with the 200mm lenses, we used a broad-band 400– to 700–nm filter; with the 85mm lenses, we used an SDSS–r filter.

The field of TOI–757 was observed by WASP in six different years, first in 2007, 2008, 2011, and 2012, when WASP–South was equipped with 200–mm lenses, and then in 2013 and 2014, equipped with 85–mm lenses. In each year the observations spanned 150 to 180 d. A total of 66 000 data points were obtained, with TOI–757 being by far the brightest star in the photometric extraction aperture. The TOI–757 b transits are too shallow to be detected in the WASP photometry. As such, the WASP data were used to check for stellar variability (see Section 3.3).

¹<https://mast.stsci.edu/portal/Mashup/Clients/Mast/Portal.html>

²<https://tess.mit.edu/followup>

2.2.2 KELT

TOI–757 was observed by the Kilodegree Extremely Little Telescope (KELT) survey in field S24 by the southern telescope during the observing seasons of 2010, 2011, 2012, and 2013. The telescope includes an Apogee Alta U16M camera with a 4096×4096 , 9 μm pixel Kodak KAF–16803 front illuminated CCD. The optics include a Mamiya 645 80mm f/1.9 lens (42 mm effective aperture) and a Kodak Wratten #8 red–pass filter. The pixel scale of the detector is $\sim 23''\text{pix}^{-1}$ leading to a total field of view (hereafter FoV) of $26^\circ \times 26^\circ$ remarkably similar to the FoV of a single *TESS* camera. The KELT telescopes typically observe fields in two orientations (east and west) and the exposures are kept to 150 s. Any given KELT field can be expected to be observed between 5 and 50 times a night given the position of the Moon (Pepper et al. 2007, 2012).

Following the work of Oelkers et al. (2018) the east and west light curves were combined into a single light curve (with a total of 4540 exposures) and post–processed using the Trend–Filtering Algorithm (Kovács, Bakos & Noyes 2005) to remove common detector systematics. In practice, this algorithm has been found to remove large amplitude variability (such as stellar pulsations) and red–noise systematics while leaving most small amplitude variability (such as exoplanet transits and rotation signals) untouched.

2.2.3 LCOGT

We observed an egress window of TOI–757 b on UTC 2019 June 4 simultaneously in Pan–STARRS *z*–short (henceforth, *zs*) band ($\lambda_c = 8700 \text{ \AA}$, Width = 1040 \AA) and Pan–STARRS *Y*–band ($\lambda_c = 10040 \text{ \AA}$, Width = 1120 \AA), using the Las Cumbres Observatory Global Telescope (LCOGT; Brown et al. 2013) 1 m network node at South Africa Astronomical Observatory (SAAO). The *zs*–band and *Y*–band observations were observed simultaneously on two different LCO 1 m telescopes at SAAO. We also observed an ingress window in *zs*–band on UTC 2021 January 20 from the same LCOGT 1.0 m network node. The images were calibrated by the standard LCOGT BANZAI pipeline (McCully et al. 2018) and differential photometric data were extracted using AstroImageJ (Collins et al. 2017). The egress light curve in *Y*–band rules out Near–by Eclipsing Binaries (NEBs) within 2.5 of TOI–757 to more than $\pm 3\sigma$ in depth and more than $\pm 6\sigma$ in ephemeris. We used circular photometric apertures with radius 6.6 to 9.7 arcsec to extract the TOI–757 light curves. This excluded all of the flux from the nearest known neighbour in the *Gaia* DR3 catalogue that is bright enough in *TESS*–band to be capable of causing the *TESS* detection (*Gaia* DR3 6157753406083082112), which is ~ 16 arcsec east of TOI–757.

The 2019 *zs*–band observation was detrended using a linear fit to time, while the 2019 *Y*–band and 2021 *zs*–band observations were detrended using a linear fit to the total ensemble star counts. The detrend parameter for each light curve was selected using a joint detrend plus transit model fit. The detrend parameter selected minimized the BIC of the joint fit and was justified by a delta BIC > 2 compared to a transit model–only fit. The three light curves are included in the global photometric modelling described in Section 5.1.

2.2.4 CHEOPS

The Characterizing ExOPlanet Satellite (*CHEOPS*) is an ESA mission aiming to characterize known transiting exoplanets orbiting bright stars (Benz et al. 2021). The TOI–757 system was visited by *CHEOPS* in two different occasions during the Guaranteed Time

Table 1. *CHEOPS* observation log for TOI–757. The first column has the observation ID and the remaining columns show the unique file key of each *CHEOPS* visit, the start date of the observations, the duration, the exposure time, the efficiency, and the number of non–flagged data points on each visit.

ID	File key	Start date	Duration (h)	Exp. time (s)	Efficiency	No. points
1	CH_PR100024_TG013901_V0200	2021–3–31T15:26:09	28.06	60	76.8 per cent	1294
2	CH_PR100024_TG014401_V0200	2021–5–23T03:32:08	13.41	60	55.9 per cent	450

Observation programme 24, first on 2021 March 31 and then on 2021 May 23. The target was observed for a total of 1.72 d. We obtained a clear transit of TOI–757 b in the first visit, but since it was not centred with the observation window, we used the first *CHEOPS* transit together with the *TESS* transits to update the ephemerides and correct the time of the second visit. The observation log with additional details of each visit is provided in Table 1.

We used the *CHEOPS* data reduction pipeline (DRP; Hoyer et al. 2020) to reduce the raw light curves. The pipeline automatically processes the data and removes instrumental variability and environmental effects such as background and smearing. The DRP produces a file containing all the extracted light curves and additional data, including quality flags and the roll–angle and background time series that can be used for further corrections. The signal is extracted in four different apertures and for this analysis we chose to work with the OPTIMAL set, which calculates the optimal aperture radius based on the best signal–to–noise ratio (S/N).

We use the package *pycheops* (Maxted et al. 2022), which is publicly available,³ to correct and de–correlate the *CHEOPS* light curves. We use *pycheops* to download the light curves from the Data & Analysis Center for Exoplanets (DACE⁴) website, which is used to store *CHEOPS* observation data. DACE is a facility dedicated to extrasolar planets data visualization, exchange, and analysis hosted by the University of Geneva. We first subtract the contamination of nearby sources and perform an initial outlier clipping at 5σ . The de–correlation parameters are selected by calculated the Bayesian Information Criterion (BIC) value of the model for each combination of parameters, assuming that the lowest BIC corresponds to the combination that best describes the data. We de–correlate against time, position of the centroid, contamination, and smearing as well as the roll angle of the telescope. Some *CHEOPS* observations can be contaminated by observation–specific sources, such as the Moon. Therefore, we use *pycheops* to correct for this ‘glint’ effect as well. Then, we perform a preliminary least squares fit of the light curves, without any de–correlation and calculate the root mean square (RMS) error. We select Gaussian distributions centred at zero with a standard deviation of two times the RMS error from the previous fit, to use as priors for the de–correlation parameters. Finally, we perform a Markov Chain Monte Carlo (MCMC) fit of the *CHEOPS* light curves within *pycheops*, including a Gaussian Process (GP) regression method with a SHOTerm kernel to fit for the chosen de–correlation parameters. We then retrieve the light curves corrected with the GP and save them in a separate file, to be included in the photometric fit.

2.3 HARPS

We acquired 27 high–resolution ($R \approx 115\,000$) spectra of TOI–757 with the High Accuracy Radial velocity Planet Searcher (HARPS;

Mayor et al. 2003) spectrograph mounted at the ESO–3.6m telescope at the European Southern Observatory (ESO), La Silla, Chile. The observations were carried out between 2021 January 22 and May 30 (UT), as part of our HARPS large program for the RV follow–up of *TESS* transiting planet candidates (ID: 106.21TJ.001, PI: Gandolfi). We set the exposure time to 1500–1800 s leading to a median S/N ratio per pixel at 550 nm of ~ 87 on the extracted spectra and a median RV uncertainty of 0.98 m s^{-1} . We reduced the HARPS data using the Data Reduction Software (DRS; Lovis & Pepe 2007) available at the telescope and extracted the RV measurements by cross–correlating each Echelle spectrum against a G2 numerical mask (Baranne et al. 1996; Pepe et al. 2002). We also used the DRS to extract the Ca II H & K lines activity indicator $\log R_{\text{HK}}$, and the profile activity diagnostics of the cross–correlation function (CCF), namely, the full width at half–maximum (FWHM), the bisector inverse slope (BIS), and the contrast. We finally extracted relative RV measurements and additional activity indicators –– such as the H α and Na D lines indicators –– using the Template Enhanced Radial velocity Re–analysis Application (TERRA; Anglada-Escudé & Butler 2012). Table A1 lists the time stamps of our HARPS observations in Barycentric Julian Dates in Barycentric Dynamical Time (BJD_{TDB} – 2457000), along with the DRS and TERRA RV measurements and activity indicators.

2.4 ESPRESSO

We obtained 22 spectra of TOI–757 with the Echelle SPectrograph for Rocky Exoplanets and Stable Spectroscopic Observations (ESPRESSO; Pepe et al. 2021) at the 8.2 m ESO Very Large Telescope (VLT) array, at the Paranal Observatory in Chile. The observations were obtained from 2021 April 4 to 2021 August 6 for an ESPRESSO program designed to explore the densities of sub–Neptunes (Program ID: 105.20P7.001, PI: Bouchy). We observed TOI–757 in HR mode (1 UT, $R \sim 140\,000$) over a spectral range from ~ 380 to ~ 780 nm. ESPRESSO is contained in a temperature- and pressure-controlled vacuum vessel to avoid spectral drifts. ESPRESSO observations can be carried out with simultaneous calibration using a Fabry–Pérot etalon on a second calibration fibre, which was used for our observations.

The ESPRESSO RVs were processed using DACE. The RV and stellar activity indicators provided in DACE are computed by cross–correlating the calibrated spectra with stellar templates for the specific spectral type, using the latest version (3.0.0) of the publicly available ESPRESSO DRS.⁵ Stellar activity indicators such as the FWHM and the BIS are derived from the CCF, while other activity indicators (e.g. S-index, Na-index, etc.) are extracted from the spectra. The 22 ESPRESSO observations of TOI–757, listed in Table A1, had an exposure time of 600 s and a median RV uncertainty of 0.54 m s^{-1} .

³<https://github.com/pmaxted/pycheops>

⁴<https://dace.unige.ch>

⁵<https://www.eso.org/sci/software/pipelines/espreso/espreso-pipe-recipes.html>

2.5 Planet Finder Spectrograph

We obtained a total of 26 RV data points (15 epochs) using the Carnegie Planet Finder Spectrograph (PFS; Crane, Shectman & Butler 2006; Crane et al. 2008, 2010) on the 6.5-m Magellan II Clay telescope. PFS is an optical high-resolution echelle spectrograph covering 391–784 nm, and uses an iodine cell for wavelength calibration. The observations presented here were taken with the 0.3 arcsec \times 2.5 arcsec slit, resulting in a resolving power of $R \sim 130\,000$ and a median RV uncertainty of 0.89 m s^{-1} . Individual exposure times for TOI–757 ranged from 600 to 1500 s and were often taken $\times 2$ per night separated by a few hours (to average over granulation) and binned on a nightly basis. The time stamps were converted from JD to BJD in Barycentric Dynamical Time using the tools provided by Eastman, Siverd & Gaudi (2010). The extraction of stellar spectra and the measurement of radial velocities were conducted with an IDL pipeline customized for PFS (Butler et al. 1996). The PFS data presented here (see Table A1) were collected as part of the Magellan *TESS* Survey (MTS), described in detail in Teske et al. (2021), although they were not included/published in that paper. An update to MTS with this and additional TOI–757 data is forthcoming.

3 STELLAR CHARACTERIZATION OF TOI–757

We characterize the stellar properties of TOI–757 (TIC 130924120) using the HARPS and ESPRESSO spectra. A summary of the stellar parameters, including the *Gaia* astrometry, are listed in Table 2. The HARPS–derived stellar parameters give consistent results with their ESPRESSO counterparts. Hence, we decided to use the ESPRESSO stellar parameters in our final analysis, given that they are slightly more precise. The reported values of our work in Table 2 thus correspond to the ESPRESSO–derived stellar parameters.

Based on the derived T_{eff} for TOI–757, we find that it is most likely a K0 V type star (Pecaut & Mamajek 2013). The following subsections describe the different properties of the system and how we derived its basic parameters listed in Table 2.

3.1 Stellar atmospheric properties and abundances

The spectroscopic stellar parameters (T_{eff} , $\log g$, microturbulence, [Fe/H]) were estimated using the ARES+MOOG methodology. The methodology is described in detail in Santos et al. (2013), Sousa (2014), and Sousa et al. (2021). This was done using the latest version of ARES⁶ (Sousa et al. 2007, 2015) to consistently measure the equivalent widths (EWs) of selected iron lines on the combined ESPRESSO spectrum. We used the list of iron lines presented in Sousa et al. (2008). A minimization process is then used in this analysis to find the ionization and excitation equilibrium and converge for the best set of spectroscopic parameters. This process uses a grid of Kurucz model atmospheres (Kurucz 1993) and the radiative transfer code MOOG (Snedden 1973). We also derived a more accurate trigonometric surface gravity using recent *Gaia* data following the same procedure as described in Sousa et al. (2021) which provided a very consistent value when compared with the spectroscopic surface gravity.

Abundances of Mg, Si, and Ti were derived using the same tools and models as for stellar parameter determination. Although the

Table 2. Identifiers, equatorial coordinates, parallax, distance, optical and infrared magnitudes, and stellar fundamental parameters for TOI–757. The parameters reported for this work were derived using the ESPRESSO spectra.

Parameter	Value	Reference
<i>Identifiers</i>		
CD	–34 8236	
TIC	130924120	
2MASS	J12315870–3533177	
APASS	18 444 726	
<i>Gaia</i> DR3	6157753406084087168	
TOI	757	
TYC	7242–01598–1	
UCAC4	273–064695	
WISE	J123158.74–353316.5	
<i>Equatorial coordinates</i>		
RA (J2000) [deg]	187.99	1
Dec (J2000) [deg]	–35.55	1
Parallax [mas]	16.58 \pm 0.02	1
Distance [pc]	60.4 ^{+0.3} _{–0.2}	1
RUWE	0.97	1
<i>Apparent magnitudes</i>		
<i>Gaia</i> G [mag]	9.5615 \pm 0.0001	1
<i>Gaia</i> BP [mag]	9.9566 \pm 0.0005	1
<i>Gaia</i> RP [mag]	8.9937 \pm 0.0003	1
<i>TESS</i> T [mag]	9.048 \pm 0.006	2
B [mag]	10.56 \pm 0.06	2
V [mag]	9.743 \pm 0.004	2
J [mag]	8.35 \pm 0.03	4
H [mag]	7.98 \pm 0.04	4
Ks [mag]	7.87 \pm 0.02	4
WISE 3.4 μm [mag]	7.81 \pm 0.03	5
WISE 4.6 μm [mag]	7.88 \pm 0.02	5
WISE 12 μm [mag]	7.83 \pm 0.02	5
WISE 22 μm [mag]	7.67 \pm 0.13	5
<i>Stellar parameters</i>		
R_* [R_\odot]	0.773 \pm 0.005	6
M_* [M_\odot]	0.80 \pm 0.04	6
ρ_* [g cm^{-3}]	2.4 \pm 0.1	6
T_{eff} [K]	5278 \pm 63	6
$\log g$ (<i>Gaia</i>) [cm s^{-2}]	4.54 \pm 0.03	6
$\log g$ (spec) [cm s^{-2}]	4.5 \pm 0.1	6
L_* [L_\odot]	0.42 \pm 0.02	6
Age [Gyr]	7.5 \pm 3.0	6
$v \sin(i)$ [km s^{-1}]	2.4 \pm 0.4	6
[Fe/H]	–0.27 \pm 0.04	6
[M/H]	–0.21 \pm 0.05	6
[Mg/H]	–0.2 \pm 0.03	6
[Si/H]	–0.23 \pm 0.04	6
[Ti/H]	–0.14 \pm 0.05	6
$[\alpha/\text{Fe}]$	0.08 \pm 0.05	6

Note. References: (1) *Gaia* Collaboration (2023); (2) Paegert et al. (2022); (3) Høg et al. (2000); (4) Cutri et al. (2003); (5) Cutri et al. (2021); (6) This work.

EWs of the spectral lines were automatically measured with ARES, we performed careful visual inspection of the EWs measurements. For the derivation of abundances, we closely followed the methods described in Adibekyan et al. (2012, 2015). Considering the mean of the abundances of Mg, Si, and Ti as $[\alpha/\text{H}]$, we calculated the α enhancement of the star relative to iron and its metallicity ($[\text{M}/\text{H}]$) following Yi et al. (2001). These parameters are presented in Table 2.

⁶The last version, ARES v2, can be downloaded at <https://github.com/sousasag/ARES>.

3.2 Stellar radius, mass, and age

We determined the stellar radius of TOI–757 via an MCMC-modified infrared flux method (Blackwell & Shallis 1977; Schanche et al. 2020) to build spectral energy distributions (SEDs) using stellar atmospheric models from two catalogues (Kurucz 1993; Castelli & Kurucz 2003) with priors coming from our spectral analysis described above. We compute synthetic photometry from these SEDs that are compared to the observed broad-band photometry in the following bandpasses: *Gaia*G, G_{BP} , and G_{RP} , 2MASS J , H , and K , and *WISE* $W1$ and $W2$ (Skrutskie et al. 2006; Wright et al. 2010; Gaia Collaboration 2023) to derive the stellar bolometric flux of TOI–757. Using known physical relations, we convert this flux into effective temperature and angular diameter that is subsequently translated into stellar radius using the offset–corrected *Gaia* parallax (Lindgren et al. 2021). To correct for model uncertainties between the two atmospheric catalogues we used a radius posterior distribution Bayesian modelling averaging and report the weighted average in Table 2 (Fragoso & Louzada Neto 2015). Thus, we obtain $R_{\star} = 0.773 \pm 0.005 R_{\odot}$.

We finally derived both the stellar mass M_{\star} and age t_{\star} according to stellar evolutionary models. In detail, we inputted T_{eff} , $[M/H]$, and R_{\star} in the isochrone placement algorithm (Bonfanti et al. 2015; Bonfanti, Ortolani & Nascimbeni 2016), which is designed to interpolate the input set of values along with their uncertainties within pre-computed grids of PARSEC⁷ v1.2S (Marigo et al. 2017) isochrones and tracks. We inflate the mass and age uncertainties by 4 per cent and 20 per cent, respectively, by adding them in quadrature to their respective internal uncertainties. This is done to account for isochrone systematics (see Bonfanti et al. 2021). After inflating the internal uncertainties, we obtained $M_{\star} = 0.80 \pm 0.04 M_{\odot}$ and $t_{\star} = 7.5 \pm 3.0$ Gyr.

3.3 Stellar variability and rotation period

To measure the rotational period of the star, we searched our WASP light curves for any rotational modulation using the methods outlined in Maxted et al. (2011), analysing both individual years of data and combined years. We found no significant periodicity over the range 1 to 100 d, with a 95 per cent–confidence upper limit on the amplitude of 2 mmag.

Using KELT time–series photometry, which spans 5 and 9–yr baselines (depending on the instrument used), Oelkers et al. (2018) found a significant rotation period signal of ~ 14.2 d for TOI–757, above a false alarm probability (FAP) level of 0.1 per cent (see Fig. 1). The amplitude of the KELT modulation (around 1 mmag) is consistent with the WASP upper limit. The WASP data show no modulation stronger than 2 mmag (at the 95 per cent confidence level), whereas the KELT data exhibit a 1 mmag modulation. Thus, the two data sets are consistent. To further verify the stellar signal we see from the periodogram analysis of the KELT photometry, we fit a GP to the KELT light curves, which have the trend–filtering–algorithm (TFA) applied to it. These were the same TFA light curves used in the Oelkers et al. (2018) paper to calculate the rotation period of TOI–757. We use the `celerite2` RotationTerm kernel (Foreman-Mackey et al. 2017) for the KELT GP, and additionally fit for the instrumental jitter term (which is added in quadrature to the errors of the data) and the systemic mean magnitude. We use wide, Uniform priors for all parameters, with the rotation term P_{GP} prior being $\mathcal{U}[1,$

⁷Padova and TRieste Stellar Evolutionary Code: <http://stev.oapd.inaf.it/cgi-bin/cmd>.

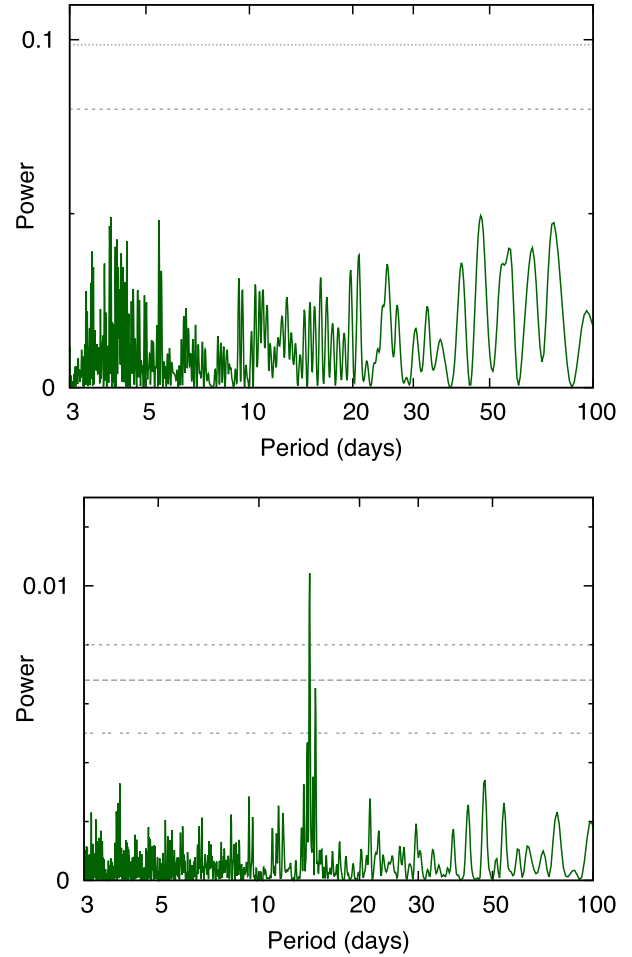


Figure 1. *Top:* a sample periodogram of the WASP–South photometric time series data on TOI–757, being from 2011 and 2012 combined, showing no significant periodicities over the range 1 to 100 d, with a 95 per cent–confidence upper limit on the amplitude of 1 mmag. The dashed horizontal lines are the estimated 1 per cent and 10 per cent FAP levels. *Bottom:* periodogram of the KELT data for TOI–757, accumulated from 2010 to 2013, showing a 14.2–d periodicity. The horizontal lines mark the false–alarm levels at 10 per cent, 1 per cent, and 0.1 per cent likelihood, estimated using methods from Maxted et al. (2011). The amplitude of the KELT modulation (around 1 mmag) is sufficiently consistent with the WASP upper limit, which is also about that level.

40]. We find a well–constrained P_{GP} with a best–fitting mean value of 14.18 ± 0.04 d, which is consistent with the results reported in the Oelkers et al. (2018) paper.

We also computed the Generalized Lomb–Scargle (GLS) periodograms (Astropy Collaboration 2013, 2018, 2022)⁸ of the HARPS and ESPRESSO activity indicators (Section 2). We found repeated peaks across different activity indicators for ~ 15 and ~ 30 d (Fig. 2). To check the significance of these peaks, we computed their FAP

⁸We note that the `ASTROPY` package defines the `LombScargle` class under the `timeseries` module as a ‘LombScargle Periodogram’. However, the application of this is the same as the Generalized Lomb–Scargle Periodogram when using the `fit_mean=True` argument, which is what we did for all our periodograms.

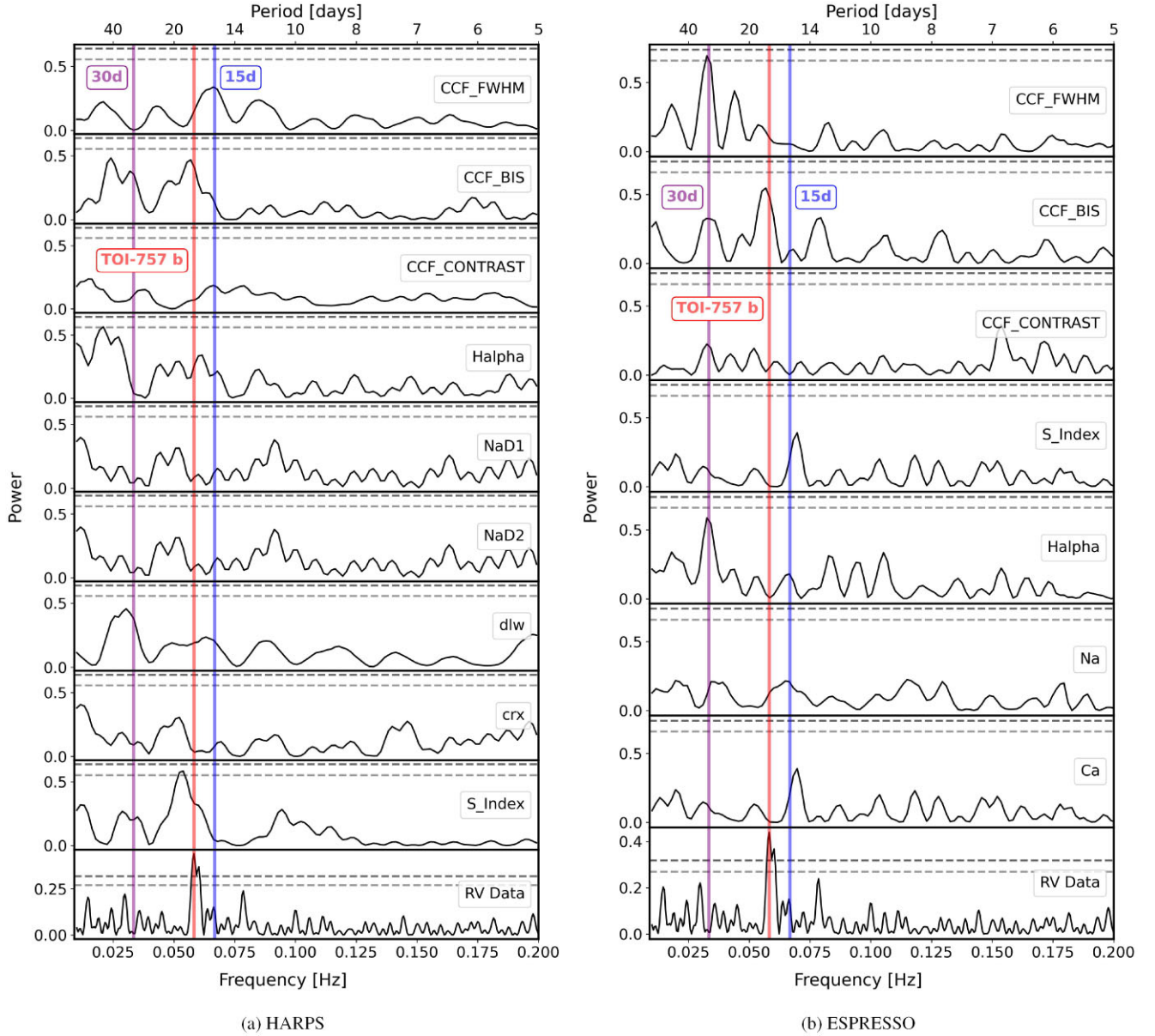


Figure 2. GLS periodograms of the HARPS and ESPRESSO RV activity indicators. The last panel at the bottom of each figure is the periodogram of the combined HARPS, ESPRESSO, and PFS RV data. The solid vertical lines correspond to the 15-d (blue) and 30-d (purple) rotation signals of the star, overplotted across the entire figure for comparison. The planet signal of TOI-757 b from the RV periodogram is shown in red solid lines across both figures. The dashed grey lines represent the FAP significance at the 0.1 per cent (dark grey) and 1 per cent (light grey) levels. *Left:* HARPS periodograms of the activity indicators. Starting from the top, we show the CCF_{FWHM}, CCF_{BIS}, CCF_{CONTRAST}, H_α Index, Na D₁ Index, Na D₂ Index, dlw Index, crx index, and S-Index activity indicators. *Right:* ESPRESSO periodograms of the activity indicators. Starting from the top, we show the CCF_{FWHM}, CCF_{BIS}, CCF_{CONTRAST}, S-Index, H_α Index, Na Index, and Ca Index activity indicators.

using the bootstrap method (see e.g. Kuerster et al. 1997; Hatzes 2019). Briefly, we computed the LS periodogram of 10 000 simulated time-series obtained by randomly shuffling the measurements and their error bars while keeping the observation time-stamps fixed, and defined the FAP as the fraction of those periodograms whose highest power exceeds the power of the signal found in the original data at any frequency. We considered a peak to be significant if it has an FAP > 0.1 per cent, and found that the majority of the peaks are not significant at the 0.1 per cent level.

We also used the chromospheric activity index $\log R'_{\text{HK}}$ of the Ca II H & K lines to estimate the rotation period of the star. We found

a mean $\log R'_{\text{HK}}$ value of about -4.82 and -5.04 for the HARPS and ESPRESSO spectra, respectively. The $P_{\star} - \log R'_{\text{HK}}$ empirical relation from fig. 13 in Suárez Mascareño et al. (2015) suggests a rotation period P_{\star} of ~ 30 d for TOI-757. If this is the case, the 15-d period found in the KELT photometry, as well as in the periodograms of the spectroscopic activity indicators, would be the first harmonic of the rotation period.

We also estimated the stellar rotation period using the projected equatorial rotational velocity $v \sin(i)$ as derived from the HARPS and ESPRESSO spectra (Section 3.1), and found a value of $v \sin(i) = 2.4 \pm 0.4 \text{ km s}^{-1}$. Using the stellar radius (Section 3.2) and assuming the

star is seen equator-on, we found a rotation period of $P_* = 16.3_{-2.3}^{+1.2}$ d, which is in agreement with the 14.2-d period found by Oelkers et al. (2018) as well as the 15-d signal seen in the activity indicators. However, due to the well-known degeneracy between $v \sin(i)$ and the macroturbulent velocity v_{mac} for slowly rotating stars (see e.g. Sundqvist et al. 2013; Simón-Díaz & Herrero 2014), it is possible that the v_{mac} has been underestimated and, consequently, the $v \sin(i)$ overestimated.

We finally fitted the RV time-series using GP regression to account for the stellar activity, as described in detail in Section 5.2. Using a wide Uniform prior of $\mathcal{U}[10, 50]$ for $P_{\text{RV,GP}}$, the solution finds a bimodal distribution in the posteriors with a primary peak at 30-d and a secondary peak at 15-d. To test how this affects our analysis, we constrained the $P_{\text{RV,GP}}$ prior to be centred around 15-d ($\mathcal{U}[1, 22]$) and 30-d ($\mathcal{U}[20, 50]$), and we found no significant difference within $1-\sigma$ in the final planet parameters derived from the fits.

It does not seem clear which of the 15-d or 30-d signals represent the true rotation period of the star from this analysis alone. Since we could not verify the validity of the periodogram signals with certainty, we looked at evidence from other independent measurements using photometric data (WASP, KELT), the projected equatorial rotational velocity of the star $v \sin(i)$, and the chromospheric activity index $\log R'_{\text{HK}}$. However, these avenues also did not provide a conclusive picture of the rotation period. The photometric variability amplitude in the WASP and KELT data is also found to be low, providing no definitive clues. One possible explanation that could account for these two stellar signals is that the star rotates at ~ 30 -d and has two active regions at opposite longitudes, producing power at the first harmonic at ~ 15 -d. The ambiguity of the stellar rotation does not affect the main results and conclusions of the paper. We verified this by adopting tighter priors for the GP `RotationTerm` kernel in our RV fit centred around 15-d and 30-d, and both yielded consistent results within 1σ for our planet parameters. Given that it causes no significant difference in our final planet parameters, we decided to adopt a prior of $\mathcal{U}[20, 50]$ for the $P_{\text{RV,GP}}$ in our RV fitting (see Section 5.2).

4 PLANET CONFIRMATION

In this section, we describe how we confirmed the planetary nature of our transiting system and ruled out the presence of nearby stellar companions. We performed periodogram analyses of the RV data, and used precise *Gaia* astrometric measurements, as well as high-contrast speckle imaging. The system was also previously analysed by Giacalone et al. (2021) using TRICERATOPS, a vetting and validation tool that is capable of modelling transits for *TESS* planet candidates from the target star as well as nearby contaminant stars. The study reported TOI-757 b as a ‘*Likely Planet*’.

4.1 Periodogram analysis

To verify the transiting planet candidate, we first computed the GLS periodograms of the full RV data set, which independently found the planet signal at $P \approx 17.2$ d (see the bottom panel of Fig. 2, which shows the periodogram of the combined HARPS, ESPRESSO, and PFS RV data). To test the significance of the signal, we estimated its FAP using the bootstrap method described in Section 3.3, and found that the peak is significant at the 0.1 per cent level. This period agrees with the period found from the photometric transit fitting ($P \approx 17.5$ d), described in Section 5.1 and with no counterpart of statistical significance in any of the periodograms of

the activity indicators (Fig. 2). The clear presence of the Doppler reflex motion of the planet in the power spectrum of the radial velocities spectroscopically confirms the planetary nature of the transit signal found by *TESS*.

4.2 Gaia astrometry

We checked the *Gaia* archive to determine whether TOI-757 is a single star or whether it might be part of a binary system. The Renormalized Unit Weight Error (RUWE) calculated for each *Gaia* source is a good indicator of the multiplicity of the system (Lindgren et al. 2018; Stassun & Torres 2021). *Gaia* defines stars being likely well-defined, single systems if the RUWE parameter is less than 1.4. Additionally, if the single-star model is well fitted to the astrometric observations of a source, the RUWE parameter is expected to be close to 1.0. We checked the *Gaia* astrometric measurements of TOI-757, which we found to be precise and well-fitted, and we also found the errors of the parallax measurement to be very small (see Table 2). The RUWE value of TOI-757 is 0.968, which is also very close to 1.0. To check for a wide-separation binary companion, we also searched through the El-Badry, Rix & Heintz (2021) binary candidate catalogue, and we did not find anything reported for TOI-757. This, along with the precise astrometric measurements of the system, indicates that our star is not likely to be part of a binary system with a long-period stellar companion.

4.3 Speckle imaging

To confirm whether TOI-757 is a single-star system, we also used speckle imaging observations, to check for the presence of nearby stars that could either potentially be the sources of false positive scenarios, or contaminate the transit signal.

On the night of 2019 July 14 (UTC), TOI-757 was observed with the High-Resolution Camera (HRCam) instrument on the Southern Astrophysical Research (SOAR) 4.1-m telescope (Sebring, Krabbendam & Heathcote 2003; Tokovinin & Cantarutti 2008). HRCam has a 15 arcsec FoV and observations are taken using an exposure time of 0.2 s. A minimum of two data cubes (each consisting of 400 frames) are recorded and processed independently for every target, and the final results are averaged across the cubes (Tokovinin 2018). We process the data as described in Tokovinin, Mason & Hartkopf (2010) by computing the power spectrum, which relates to the Fourier transform of the per-frame intensity distribution, averaged over all cube frames.

On the night of 2020 February 17 (UT), TOI-757 was observed with the ‘Alopeke speckle imager (Scott et al. 2021), mounted on the 8.1 m Gemini North telescope on Mauna Kea. ‘Alopeke simultaneously acquires data in two bands centred at 562 and 832 nm using high-speed electron-multiplying CCDs (EMCCDs). We collected and reduced the data following the procedures described in Howell et al. (2011). The resulting reconstructed image achieved a contrast of $\Delta\text{mag} = 7$ at a separation of 1 arcsec in the 832 nm band (see Fig. 3).

From our imaging observations, we do not find evidence of nearby stellar companions that might be the source of false positives, or that could be diluting the transit signal.

5 PHOTOMETRIC AND RADIAL VELOCITY ANALYSIS

We use the `exoplanet` toolkit (Foreman-Mackey et al. 2021a, b) and its dependencies (Astropy Collaboration 2013; Kipping 2013;

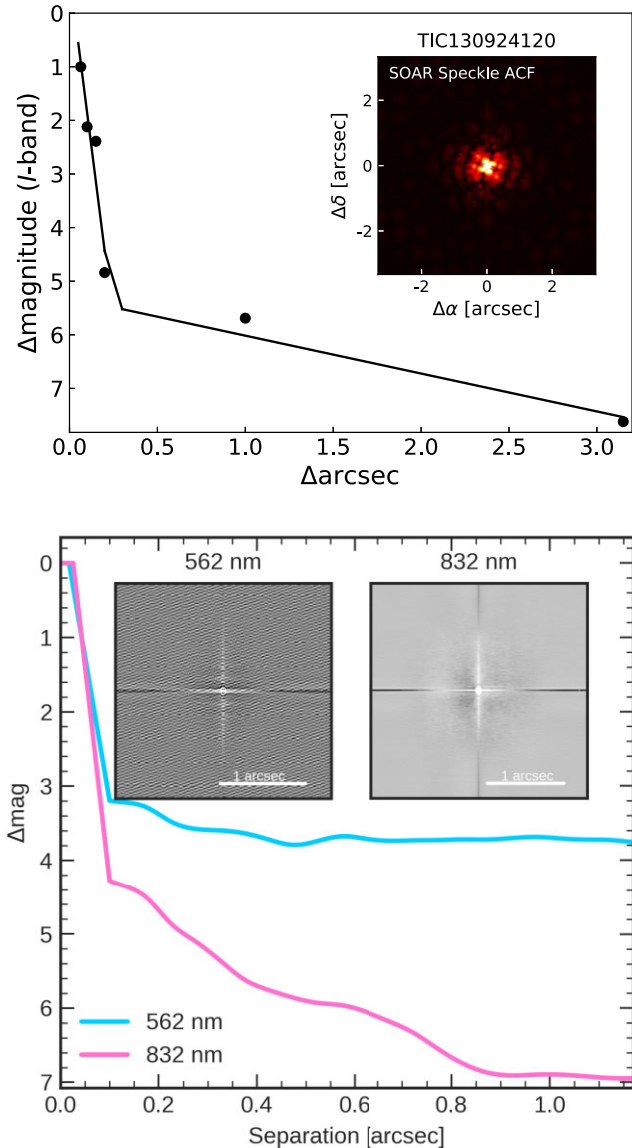


Figure 3. Speckle imaging sensitivity curves resulting from the high-contrast imaging instruments listed in Section 4.3. *Top:* SOAR/HRCam reconstructed images, showing no signs of stellar companions out to 3.0 arcsec and within $\Delta\text{mag } 7$. *Bottom:* Gemini North/Alopeke reconstructed images, showing no signs of stellar companions out to 1.2 arcsec and within $\Delta\text{mag } 7$ in the 832 nm filter.

Salvatier, Wiecki & Fonnesbeck 2016; Theano Development Team 2016; Foreman-Mackey et al. 2017; Astropy Collaboration 2018; Foreman-Mackey 2018; Kumar et al. 2019; Luger et al. 2019; Agol, Luger & Foreman-Mackey 2020) in the analyses described in this section. We perform separate MCMC fits for the photometric and RV data to derive independent radius and mass measurements of the planet. We describe the fitting method for each case in the subsections below. For each case, prior to running the MCMC, we initially run the defined global model through a custom non-linear optimizer using the `pymc3-ext` library. This enables us to optimize certain parameters and check that the model looks reasonable before running the MCMC sampler. We then explore the parameter space using the gradient-based Hamiltonian Monte Carlo sampler from `PyMC3`, which is more efficient than the traditional Metropolis-Hastings

MCMC and also uses the No U-Turn Sampling (NUTS) algorithm described in Hoffman, Gelman et al. (2014).

We use Gaussian priors the stellar parameters R_* and M_* in all fits described below. By extension, this applies a Gaussian prior to ρ_* , and particularly helps with constraining the transit model. For the MCMC fits, we inflate the errors on the stellar mass (~ 5 per cent) and stellar radius (~ 4 per cent) as described in Tayar et al. (2022) to achieve realistic uncertainties for the purpose of fitting. For clarity, the final planet parameters reported in the results, such as planet radius and planet mass, are not extracted using the inflated errors and are calculated using the precise stellar errors derived from the spectra. All time stamps for the photometric and RV data are given in *TESS* BJD time (BTJD), which is defined as $\text{BJD} - 2457000$.

The complete list of the best-fitting results from the transit and RV analyses can be found in Table 3, including the priors used as well as the posterior results from the MCMC fit. The reported best-fitting posterior values represent the 50th percentile from the MCMC fit, and the upper and lower uncertainties of the results reflect the 16th and 84th percentiles, respectively. We also performed a joint fit of the RV and transit data using `pyaneti` (Barragán, Gandolfi & Antoniciello 2019), and we found that the results yielded consistent planet parameters with the separate fits done using `exoplanet`. Consequently, performing a joint or separate fit made no difference in the final results and conclusions of the paper.

5.1 Photometric fit

In this section, we describe how we perform the global photometric transit fitting of space-based (*TESS*, *CHEOPS*) and ground-based (LCOGT) data acquired for TOI–757 b. We treat LCOGT data taken with different filters (*Y* band and *zs* band) separately when fitting the light curves, henceforth referred to as LCO–*Y* and LCO–*zs*, respectively.

5.1.1 Transit model and MCMC fit

We define a global transit model in `exoplanet` to fit over stellar, planetary, and telescope-dependent parameters, as described below. We use the full, unbinned *TESS* light curves with the out-of-transit data, which enables us to simultaneously detrend the light curves using a GP component while performing the transit fitting. The *CHEOPS* and LCOGT light curves are pre-processed and detrended as described in Sections 2.2.4 and 2.2.3, respectively. As such, no GPs were used on these light curves while performing the fitting.

For the stellar and planetary parameters, we use the built-in Keplerian orbit model and fit for the stellar radius R_* , the stellar mass M_* , the planet period P , the transit centre time t_0 , the planet eccentricity e , the argument of periastron of the planetary orbit ω_p , the impact parameter b , and the radius ratio R_p/R_* . The R_p/R_* parameter is used to set the bounds on b via the `ImpactParameter` distribution from `exoplanet` based on physical considerations, since the impact parameter cannot exceed the sum of the planet and star radii, which places a Uniform distribution prior in the range $[0, 1 + R_p/R_*]$. Since e and ω_p are correlated, we also parametrize them using $\sqrt{e} \sin(\omega_p)$ and $\sqrt{e} \cos(\omega_p)$ when performing the fitting (Anderson et al. 2011; Eastman, Gaudi & Agol 2013). Additionally, we fit over the limb-darkening coefficients u_1 and u_2 . We fit for this separately for each telescope (due to instrumentation and observing differences between them) using the Kipping (2013) parametrization for quadratic limb darkening. This follows the form described in equation (1), using Uniform priors in the range $[0, 1]$, and constrained by the boundary conditions on u_1 and u_2 . We fit over u_1 and u_2

Table 3. Summary of fitted parameters, priors, and the best–fitting results from the posteriors for the photometric and RV fitting. Parameters that are left blank for the distribution and prior entries are either derived using correlated parametrization (e.g. e and ω_p) or calculated using the results of the orbit model. The upper and lower uncertainties of the best–fitting posterior values reflect the 16th and 84th percentiles from the MCMC fit, respectively, while the reported best–fitting value is the 50th percentile. \mathcal{U} refers to a Uniform distribution, \mathcal{N} a Normal, $\mathcal{N}[\mathcal{U}]$ a Bounded Normal, and \mathcal{C} is a fixed constant.

Parameter	Distribution	Prior	Posterior
Stellar parameters			
$M_\star [M_\odot]$	$\mathcal{N}[\mathcal{U}]$	[0.797, 0.05], [0, 3]	0.80 ± 0.05
$R_\star [R_\odot]$	$\mathcal{N}[\mathcal{U}]$	[0.773, 0.04], [0, 3]	0.78 ± 0.03
$\rho_\star [\text{g cm}^{-3}]$	---	---	2.4 ± 0.3
$u_{1,TESS}$	---	---	0.6 ± 0.3
$u_{2,TESS}$	---	---	$-0.07^{+0.40}_{-0.26}$
$u_{1,CHEOPS}$	---	---	$0.5^{+0.2}_{-0.3}$
$u_{2,CHEOPS}$	---	---	$0.1^{+0.4}_{-0.3}$
$u_{1,LCO-Y}$	---	---	$0.4^{+0.5}_{-0.3}$
$u_{2,LCO-Y}$	---	---	$0.08^{+0.41}_{-0.36}$
$u_{1,LCO-zs}$	---	---	0.7 ± 0.5
$u_{2,LCO-zs}$	---	---	$-0.02^{+0.49}_{-0.43}$
Planet parameters			
<i>Transit</i>			
P [d]	\mathcal{U}	[16.97, 17.97]	17.46819 ± 0.00002
t_0 [BJD – 2457000]	\mathcal{U}	[2304.53, 2306.53]	2305.5322 ± 0.0006
b	\mathcal{U}	[0, 1.03]	0.3 ± 0.2
R_p/R_\star	\mathcal{U}	[0.024, 0.034]	$0.0299^{+0.0009}_{-0.0006}$
$R_p [R_\oplus]$	---	---	2.5 ± 0.1
a [AU]	---	---	0.122 ± 0.002
i [°]	---	---	$89.5^{+0.4}_{-0.3}$
t_{dur} [d]	---	---	0.155 ± 0.002
<i>Radial velocity</i>			
K [m s ⁻¹]	\mathcal{N}	[2.07, 3]	3.3 ± 0.6
$M_p [M_\oplus]$	---	---	$10.5^{+2.2}_{-2.1}$
e	---	---	$0.39^{+0.08}_{-0.07}$
ω_p [°]	---	---	-36^{+14}_{-10}
<i>Derived properties</i>			
T_{eq} [K]	---	---	641 ± 10
$\rho_p [\text{g cm}^{-3}]$	---	---	3.6 ± 0.8
Instrument parameters			
<i>Transit</i>			
Systemic mean flux μ_{TESS} [ppt]	\mathcal{N}	[0, 10]	0.019 ± 0.009
Systemic mean flux μ_{CHEOPS} [ppt]	\mathcal{N}	[0, 10]	0.002 ± 0.009
Systemic mean flux μ_{LCO-Y} [ppt]	\mathcal{N}	[0, 10]	-0.25 ± 0.1
Systemic mean flux μ_{LCO-zs} [ppt]	\mathcal{N}	[0, 10]	-0.1 ± 0.1
Jitter σ_{TESS} [ppt]	\mathcal{N}	[0.62, 10]	$0.616^{+0.002}_{-0.002}$
Jitter σ_{CHEOPS} [ppt]	\mathcal{N}	[0.5, 10]	0.228 ± 0.009
Jitter σ_{LCO-Y} [ppt]	\mathcal{N}	[1.62, 10]	$0.003^{+0.270}_{-0.003}$
Jitter σ_{LCO-zs} [ppt]	\mathcal{N}	[2, 10]	1.69 ± 0.07
<i>Radial velocity</i>			
Systemic mean velocity μ_{HARPS} [m s ⁻¹]	\mathcal{N}	[1.04, 10]	0.8 ± 0.6
Systemic mean velocity μ_{HARPS_FWHM} [m s ⁻¹]	\mathcal{N}	[6591.91, 2.01]	$6592.4^{+1.8}_{-1.9}$
Systemic mean velocity $\mu_{ESPRESSO}$ [m s ⁻¹]	\mathcal{N}	[1.65e-13, 10]	0.20 ± 0.5
Systemic mean velocity $\mu_{ESPRESSO_FWHM}$ [m s ⁻¹]	\mathcal{N}	[6886.15, 1.22]	6887.0 ± 1.1
Systemic mean velocity μ_{PF5} [m s ⁻¹]	\mathcal{N}	[1.83, 10]	$-0.5^{+1.4}_{-1.7}$
Jitter σ_{HARPS} [m s ⁻¹]	\mathcal{U}	[0, 5]	$0.4^{+0.4}_{-0.3}$
Jitter σ_{HARPS_FWHM} [m s ⁻¹]	\mathcal{U}	[0, 5]	$3.9^{+0.8}_{-1.4}$
Jitter $\sigma_{ESPRESSO}$ [m s ⁻¹]	\mathcal{U}	[0, 5]	$1.2^{+0.6}_{-0.7}$
Jitter $\sigma_{ESPRESSO_FWHM}$ [m s ⁻¹]	\mathcal{U}	[0, 5]	$4.0^{+0.8}_{-1.3}$
Jitter σ_{PF5} [m s ⁻¹]	\mathcal{U}	[0, 5]	0.8 ± 0.5
GP parameters			
<i>Transit</i>			
$P_{\text{PHOT,GP}}$ [d]	\mathcal{U}	[1, 50]	2.0 ± 0.3

Table 3 – *continued*

Parameter	Distribution	Prior	Posterior
$Q_{\text{PHOT,GP}}$	\mathcal{C}	$1/\sqrt{2}$	—
$\sigma_{\text{TESS,GP}}$ [ppt]	\mathcal{U}	[0, 10]	$0.072^{+0.006}_{-0.005}$
<i>Radial velocity</i>			
$P_{\text{RV,GP}}$ [d]	\mathcal{U}	[20, 50]	$31.0^{+1.4}_{-1.7}$
Q_0 RV,GP	\mathcal{U}	$[\pi, 10000]$	$4.13^{+2.03}_{-0.76}$
$\delta Q_{\text{RV,GP}}$	\mathcal{U}	[0.001, 10000]	$1.9^{+295.4}_{-1.9}$
$f_{\text{RV,GP}}$	\mathcal{U}	[0, 1]	$0.7^{+0.2}_{-0.3}$
$\sigma_{\text{HARPS,GP}}$ [m s ⁻¹]	\mathcal{U}	[0, 10]	$2.8^{+1.0}_{-0.7}$
$\sigma_{\text{HARPS,FWHM,GP}}$ [m s ⁻¹]	\mathcal{U}	[0, 100]	$30.4^{+12.5}_{-8.9}$
$\sigma_{\text{ESPRESSO,GP}}$ [m s ⁻¹]	\mathcal{U}	[0, 10]	$1.9^{+1.0}_{-0.9}$
$\sigma_{\text{ESPRESSO,FWHM,GP}}$ [m s ⁻¹]	\mathcal{U}	[0, 100]	$14.2^{+4.5}_{-3.3}$
$\sigma_{\text{PFS,GP}}$ [m s ⁻¹]	\mathcal{U}	[0, 10]	$4.0^{+2.0}_{-1.3}$

directly, which are constrained by the parametrization of q_1 and q_2 .

$$\begin{cases} \text{Parametrization} & \text{Boundary Conditions} \\ q_1 = (u_1 + u_2)^2 & u_1 + u_2 < 1 \\ q_2 = 0.5 u_1 (u_1 + u_2)^{-1} & u_1 > 0 \\ & u_1 + 2 u_2 > 0 \end{cases} \quad (1)$$

From the orbit model, we track other planetary parameters such as the implied stellar density ρ_* , the semimajor axis a/R_* , and the inclination angle i . To calculate the transit duration time t_{dur} , we approximate it using the following equation (see Winn 2010 for more details):

$$t_{\text{dur}} = \frac{P}{\pi} \times \arcsin \left(\frac{R_*}{a} \frac{\sqrt{(1 - R_p/R_*)^2 - b^2}}{\sin(i)} \right) \times \left(\frac{\sqrt{1 - e^2}}{1 + e \sin(\omega)} \right) \quad (2)$$

This describes the full transit duration, which is defined as the time between the second and third contact (when the planetary disc is completely in front of the stellar disc), also commonly referred to as t_{23} .

For each of the *TESS*, *CHEOPS*, LCO–Y, and LCO–zS light curves, we define sets of telescope–dependent parameters: the systemic mean flux μ and a jitter term σ . For the *TESS* data, we use an additional GP component for the data residuals to account for any additional instrumental noise and stellar activity signals. The kernel used for the *TESS* GP component is the `celerite2` SHOTerm, a stochastically driven, damped harmonic oscillator (Foreman-Mackey et al. 2017). This kernel includes three free hyperparameters that we fit: the amplitude of the noise model σ , a rotation term ρ representing the star’s periodicity, and the complexity term Q , which is related to the decay time-scale of stellar activity signals. The planet parameters are shared across all the photometric data when fitting, but the stellar and telescope–dependent parameters are fit separately for each instrument. We use loose, uninformative priors when fitting all our parameters.

When running the MCMC, we used two chains with 8000 tuning steps and 8000 draws, resulting in a total of 16 000 independent samples for each parameter. For convergence diagnostics, we checked the Gelman–Rubin statistic for our resulting MCMC chains, and we found them all to be < 1.01 for all our sampled parameters, indicating that there were no major issues during sampling. We also checked the number of effective samples for each parameter, and all were well

above 1000 samples per chain, indicating that a sufficient number of samples were independently drawn for every parameter.

5.1.2 Transit–only fit results

We find that TOI–757 b has an orbital period of $P = 17.46819 \pm 0.00002$ d, with a best–fitting planet–to–star radius ratio of $R_p/R_* = 0.0299^{+0.0009}_{-0.0006}$, resulting in a planetary radius of $R_p = 2.5 \pm 0.1 R_\oplus$. The full transit parameters are listed in Table 3. Since the measurements for e and ω are not well constrained from transit modelling, we rely on the RV fitting for a more robust result of the planet’s eccentricity, described in the next section.

In the top panel of Fig. 4, we show the original PDCSAP *TESS* light curves with the best–fitting GP model overplotted. The middle panel of the figures show the detrended photometric data by subtracting the GP model as well as the systemic mean flux μ of the light curve, with the best–fitting planet model overplotted. The bottom panel of the plot shows the residuals of the detrended data after subtracting the planet model. Fig. 5 shows a similar plot for the *CHEOPS* data, but without any GP component, since the *CHEOPS* data were already pre–processed and detrended prior to fitting. Fig. 6 displays the same detrended *TESS* and *CHEOPS* data, as well as the detrended LCO–Y and LCO–zS light curves, folded over the best–fitting orbital period. We overplot the best–fitting planet model for each folded light curve along with the posterior constraints corresponding to the 16th and 84th percentiles.

5.2 Radial velocity fit

In this section, we describe how we perform the RV fitting of the HARPS, ESPRESSO, and PFS data. The RV data for all instruments can be found in Table A1.

5.2.1 RV model and MCMC fit

We define a global RV model in `exoplanet` to fit over stellar, planetary, and instrument–dependent parameters, as described below. The stellar and planet parameters are shared between the HARPS, ESPRESSO, and PFS data when fitting, but the instrument–dependent parameters are fit separately.

For the stellar and planetary parameters, we use the built–in Keplerian orbit model and fit for the stellar radius R_* , the stellar mass M_* , the planet period P , the transit centre time t_0 , the planet eccentricity e ,

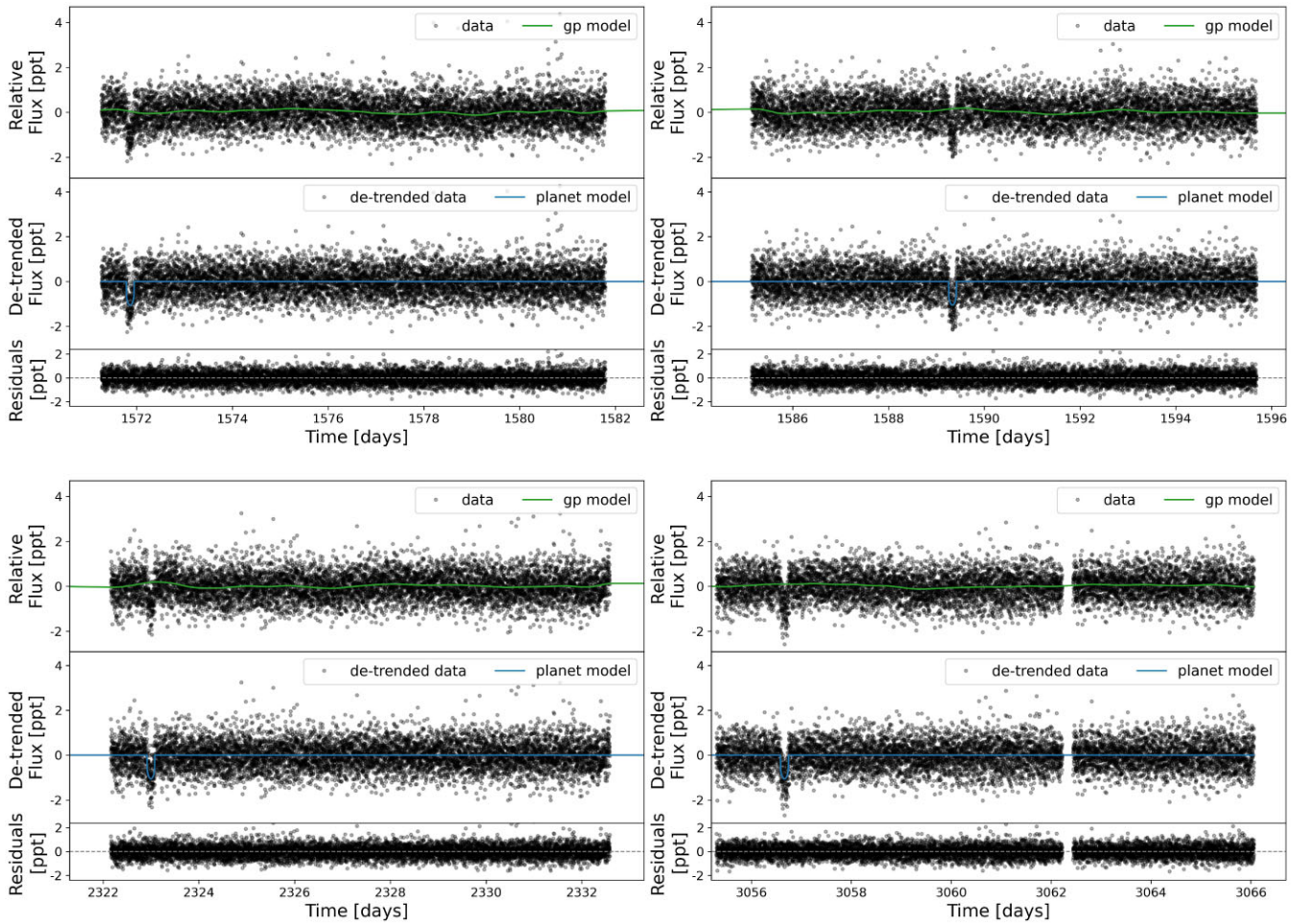


Figure 4. *TESS* SPOC–PDCSAP light-curve data of TOI–757 (see Section 2.1) taken from Sectors 10 (top two figures), 37 (bottom left figure), and 64 (bottom right figure). In the top panel of each figure, we show the raw light curves in black dotted points along with the best–fitting GP model plotted on top in a solid green line. The middle panel of the figures shows the detrended data in black dotted points (where the GP model as well as the systemic mean flux μ of the light curve were subtracted out), along with the best–fitting planet model plotted on top in a solid blue line (see Section 5.1). The bottom panel of the figures shows the residuals of the detrended data after subtracting the planet model.

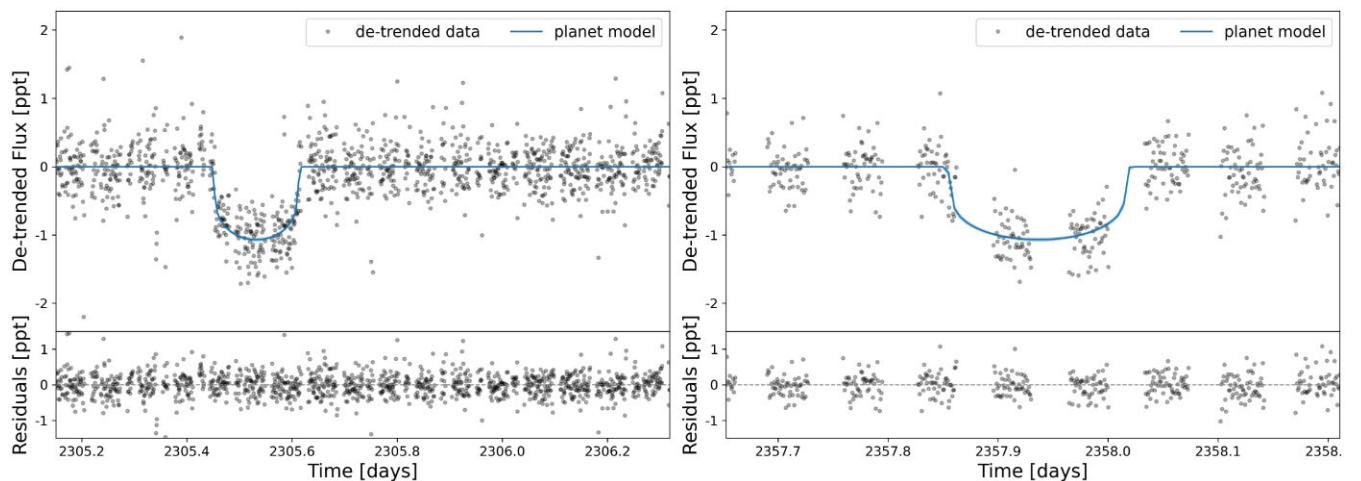


Figure 5. *CHEOPS* light-curve data of TOI–757 (see Section 2.2.4). In the top panel of each figure, we show the detrended data in black dotted points, along with the best–fitting planet model plotted on top in a solid blue line (see Section 5.1). The bottom panel of the figures shows the residuals of the detrended data after subtracting the planet model.

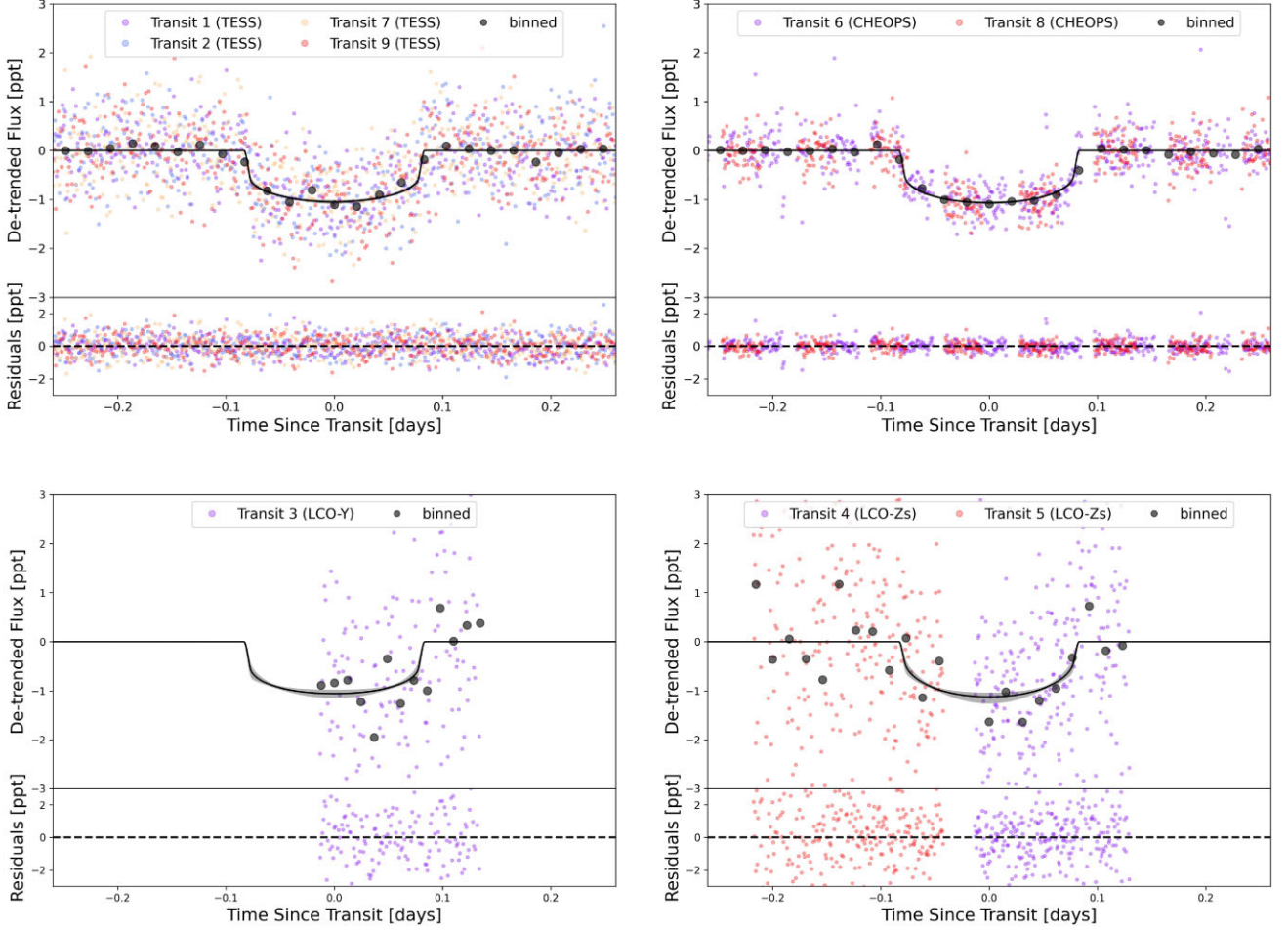


Figure 6. Detrended photometric light curves, folded over the best-fitting orbital period P , along with the best-fitting planet model and the posterior constraints corresponding to the 16th and 84th percentiles (see Section 5.1). The dotted data points are colour-coded to show the individual transits for each telescope. For clarity, we also overplot the binned detrended data in black dots. *Top panel:* TESS (left) and CHEOPS (right) folded light curves. *Bottom panel:* LCO-Y (left) and LCO-Zs (right) folded light curves.

the argument of periastron of the planetary orbit ω_p , the inclination i , and the planet mass M_p . We use the best-fitting MCMC values from the results of the photometric transit fit in Section 5.1 to set priors on P , i , and t_0 when performing the RV fit. Since e and ω_p are correlated, we also parametrize them using $\sqrt{e} \sin(\omega_p)$ and $\sqrt{e} \cos(\omega_p)$ when performing the fitting. From the orbit model, we track other planetary parameters such as the implied stellar density ρ_* .

For each of the HARPS, ESPRESSO, and PFS instruments, we define sets of instrument-dependent parameters, including the systemic mean velocity μ , a jitter term σ , and a GP component for the data residuals to account for any additional instrumental noise and stellar activity signals. We also fit GPs to the HARPS and ESPRESSO CCF_{FWHM} activity indicators to simultaneously model the stellar activity along with the RV data. The kernel used for the RV GP components described in this section is the `celerite2` `RotationTerm`, which is a combination of two `SHOTerms` that can be used to model stellar rotation using two modes in Fourier space, giving us $\text{SHO}(P_*) + \text{SHO}(P_*/2)$. It includes five free hyperparameters that we fit for: the amplitude of the noise model σ , a rotation term P_* representing the star’s periodicity, the complexity term Q_0 for the secondary oscillation, a term representing the difference between the quality factors (Q_1 and Q_2) of the two modes δQ , and the fractional amplitude of the second mode compared to the first f . Four of the hyperparameters

(P_* , Q_0 , δQ , and f) are shared between the activity indicator GPs and the RV GPs, while the fifth hyperparameter σ (corresponding to the amplitude of the noise model) is fit separately for each data set. This is to help constrain the RV data better using the stellar rotation period and any additional activity signals that could be contaminating the RV data. Apart from the priors placed on P , i , and t_0 from the photometric MCMC results, we use loose, uninformative priors on all other parameters. When running the MCMC, we used two chains with 8000 tuning steps and 8000 draws, resulting in a total of 16 000 independent samples for each parameter. For convergence diagnostics, we checked the Gelman–Rubin statistic for our resulting MCMC chains, and we found them all to be <1.01 for all our sampled parameters, indicating that there were no major issues during sampling. We also checked the number of effective samples for each parameter, and all were well above 1000 samples per chain, indicating that a sufficient number of samples were independently drawn for every parameter.

5.2.2 Model comparison

We initially tested running the fit for different sets of models to see which one is best suited to use for our analysis. Examples of tests include the inclusion or exclusion of GPs, whether to use

Table 4. A list of the different model combinations we tested for RV fitting, along with their corresponding BIC values. The BIC value for the preferred model was 361.6, which we subtract from the BIC values of the other models and report under the column labeled ΔBIC .

GP	Kernel (celerite2)	Activity indicator	BIC value	ΔBIC
All	Rotation Term	FWHM	361.60	0
All	SHO Term	FWHM	385.68	24.08
All	Matern34 Term	FWHM	397.20	35.6
All	SHO Term	FWHM + S-Index	427.04	65.44
HARPS only	SHO Term	FWHM + S-Index	455.04	93.44
PFS only	SHO Term	FWHM + S-Index	490.03	128.43
None	None	None	508.90	147.3
ESPRESSO only	SHO Term	FWHM + S-Index	707.37	345.77

any given set(s) of activity indicators during fitting, and adjusting the different GP kernels that could be used. We then performed a model comparison test by comparing the BIC value for each model case. We define $\Delta\text{BIC} = \text{BIC}_{\text{new}} - \text{BIC}_{\text{old}}$. A smaller ΔBIC signifies that the model is less complex and favoured while still providing a good fit to the data. A more complex model could still have a lower BIC if it fits the data sufficiently better than simpler models. We found that including GPs for all RV instruments, using only the CCF_{FWHM} activity indicator from HARPS and ESPRESSO, and using the RotationTerm kernel for the GP analysis, was the favoured model. Table 4 shows a list of the different model combinations we tested, along with their corresponding BIC values. The BIC value for the preferred model was 361.6, which we subtract from the BIC values of the other models and report under the column labeled ΔBIC .

5.2.3 RV-only fit results

From the RV-only MCMC fit, we find that TOI-757 b is on a highly eccentric orbit with an eccentricity of $e = 0.39^{+0.08}_{-0.07}$ with an argument of periastron for the planetary orbit of $\omega_p = -36.02^{\circ}_{-10.10}^{+13.69}$. The RV semi-amplitude is found to be $K = 3.27^{+0.63}_{-0.61} \text{ m s}^{-1}$, resulting in a planetary mass of $M_p = 10.45^{+2.18}_{-2.09} M_{\oplus}$. The full RV best-fitting parameters are listed in Table 3.

We plot the detrended RV data by subtracting the GP model as well as the systemic mean velocity μ of the instrument in Fig. 7. The detrended data are shown along with the best-fitting planet model and the posterior constraints for the 16th and 84th percentiles in the top panel, while the lower panel displays the same data folded over the orbital period, along with the best-fitting planet model and the posterior constraints. Fig. 8 shows the mean-subtracted RV data points for each instrument, along with separate curves for the planet model, the GP model, and the full planet+GP model. In Fig. 9, we show the GP models of the CCF_{FWHM} activity indicators with the posterior constraints for the 16th and 84th percentiles, which were used to help constrain the GP hyperparameters of the RV data.

5.3 Results comparison

5.3.1 Stellar density tests

We checked what solution the MCMC finds when we placed wide uniform priors versus tighter Gaussian priors on the stellar parameters, R_* and M_* (and by extension, on the stellar density).

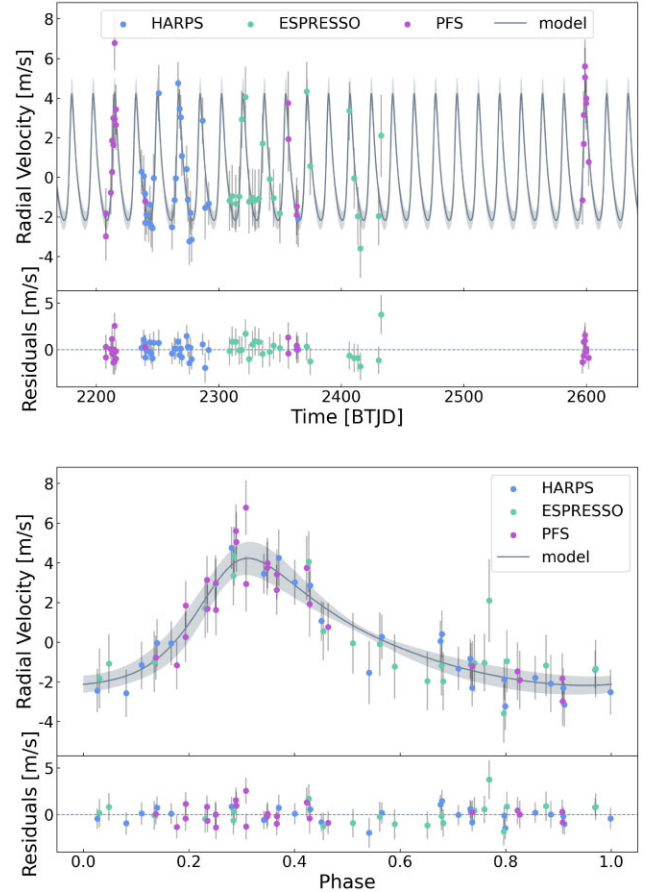


Figure 7. RV data of the HARPS (blue dots), ESPRESSO (green dots), and PFS (magenta dots) instruments. The error bars include the jitter component σ for each instrument, which was added in quadrature to the RV error for each data point. The data were detrended by subtracting the GP model as well as the systemic mean velocity μ of the instrument (see Section 5.2). The best-fitting planet model is plotted on top in a grey solid line, along with the posterior constraints for the 16th and 84th percentiles in the grey shaded region. The top panel shows the data across the full time baseline, while the lower panel displays the same detrended data folded over the best-fitting orbital period P .

For a proper comparison, we ran this test for all of our MCMC fits: the transit fit as well as the RV fit. We find that in the case of the transit-only fit, the eccentricities derived when we test the stellar density with ($e = 0.3 \pm 0.2$) and without ($e = 0.5 \pm 0.3$) informative stellar priors are both poorly constrained by the photometric data alone. When testing the case of the RV-only fit, we find a well-constrained eccentricity of $e = 0.4 \pm 0.1$, with a narrower posterior distribution compared with the transit-only fit, regardless of whether we applied a prior on the stellar density or not. As expected, the RV data alone are able to constrain the eccentricity much better than the photometric data, and independently predicts a significantly high eccentricity.

5.3.2 GP tests

To test whether our RV GPs are overfitting the planet signal or contributing to the high eccentricity, we placed a tighter prior on all the GP σ terms (which correspond to the amplitude of the noise model). More specifically, we changed the σ_{GP} priors from wide

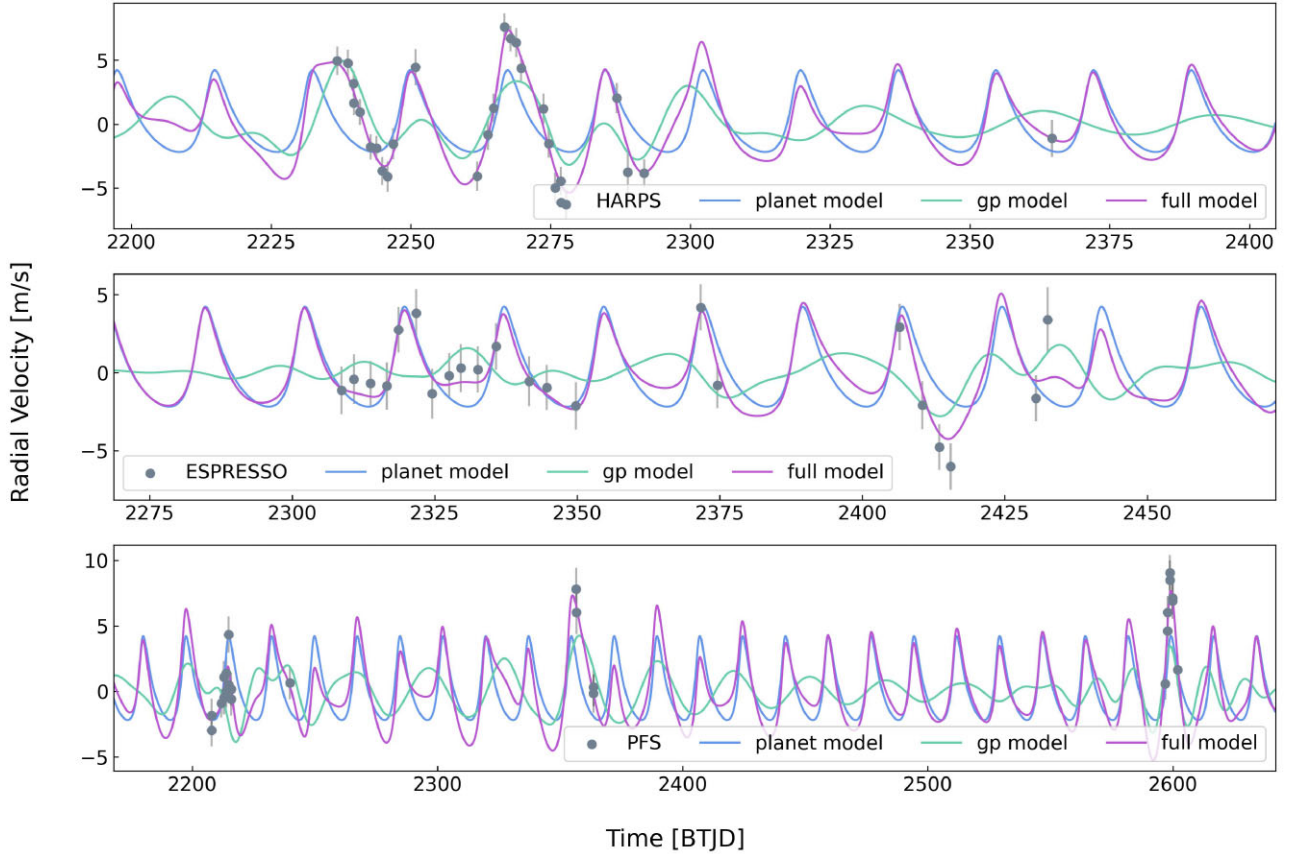


Figure 8. Mean-subtracted RV data plotted in grey dotted points for each of the HARPS (*top panel*), ESPRESSO (*middle panel*), and PFS (*bottom panel*) instruments, along with separate model curves for the planet model (*blue solid line*), the GP model (*green solid line*), and the full planet + GP model (*magenta solid line*). The error bars include the jitter component σ for each instrument, which was added in quadrature to the RV error for each data point.

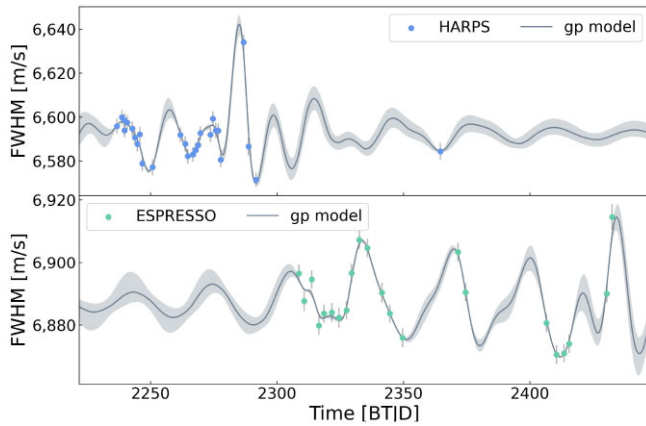


Figure 9. GP models, shown in grey solid lines, of the CCF_{FWHM} activity indicators from HARPS (*top panel*, represented by the blue dots) and ESPRESSO (*bottom panel*, represented by the green dots). The shaded regions are the posterior constraints for the 16th and 84th percentiles of the GP models. The error bars include the jitter component σ for each instrument, which was added in quadrature to the error for each data point.

($\mathcal{U}[0, 10]$) to narrow ($\mathcal{U}[0, 1]$) priors and reran the MCMC fit. We additionally tested fitting all the RVs using a single-GP (while still using wide priors for σ_{GP}), and we also do not fit over any activity indicators in this test case for simplicity. Finally, we tested fitting without any RV-related GP components, including the exclusion of

Table 5. Comparison of resulting planet parameters in the RV-only fit when testing different priors for σ_{GP} . For the wide-priors case, we use a Uniform distribution of $\mathcal{U}[0, 10]$ for all the σ_{GP} terms of the RV instrument GPs. For the narrow-priors case, we use a Uniform distribution of $\mathcal{U}[0, 1]$. For the single-GP case, we use wide priors for σ_{GP} as done in the wide-priors case, and we also do not fit over any activity indicators for simplicity. For the no-GP case, we remove all RV-related GP components, including activity indicators. The reported values correspond to the mean best-fitting value from the MCMC fit, with the standard deviation as the error.

Parameter	Wide priors	Narrow priors	Single GP	No GP
K [m s^{-1}]	3.3 ± 0.6	3.3 ± 0.4	3.8 ± 0.7	3.1 ± 0.5
$M_{\text{p}} [M_{\oplus}]$	10.5 ± 2.2	10.6 ± 1.4	12.3 ± 2.4	9.8 ± 1.6
e	0.39 ± 0.08	0.39 ± 0.06	0.36 ± 0.07	0.39 ± 0.08
$\omega_{\text{p}} [^{\circ}]$	-34 ± 14	-36 ± 13	-28 ± 15	-26 ± 24

activity indicators. A summary of the results can be found in Table 5. The planet parameters resulting from each test case did not change significantly compared to the results from the wide σ_{GP} priors case (which is what is used in the final analysis of this paper), and the mean best-fitting values are all within the 1σ error limits. Moreover, the eccentricity measurement does not appear to be affected using narrow σ_{GP} priors, using a single GP, or by having no RV GP components at all. This shows that the high eccentricity of 0.4 from the RV fit is most likely not an artefact of the GP behaviour. Additionally, the fact that we do not find an argument of periastron ω_{p} near 90° or -90° provides further confidence to our eccentricity result. Obtaining a

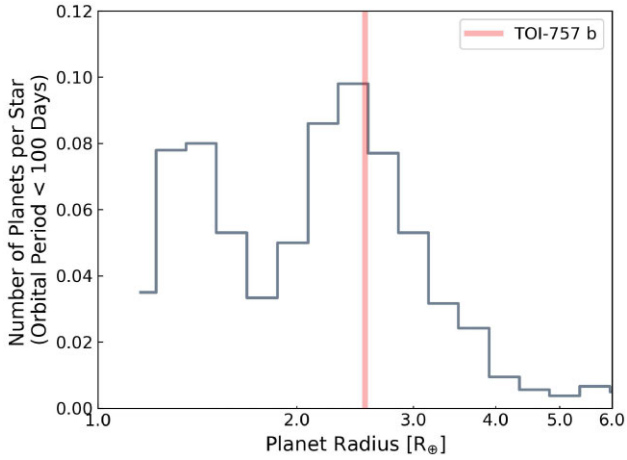


Figure 10. The observed planet radius distribution adapted from Fulton et al. (2017). The well-known radius gap feature of the exoplanet population is apparent from 1.5 to 2.0 R_{\oplus} . The overplotted red line represents the radius of TOI-757 b, showing that the planet lies above the valley and is among the abundant population of mini-Neptunes.

spurious eccentricity is more likely when ω_p is close to such values, given the shape (and similarity to a circular orbit) of the RV curve for these orientations.

6 DISCUSSION

From our analysis, we clearly detect TOI-757 b in the photometric data from *TESS* and *CHEOPS*, supported by the transits acquired from ground-based telescopes. We also spectroscopically confirm the transiting planet by significantly detecting the Doppler reflex motion induced by TOI-757 b in our HARPS, ESPRESSO, and PFS RV data. The photometric and RV fitting yield a planet radius of $R_p = 2.5 \pm 0.1 R_{\oplus}$, a mass of $M_p = 10.5^{+2.2}_{-2.1} M_{\oplus}$, and an eccentricity of $e = 0.39^{+0.08}_{-0.07}$ for TOI-757 b.

6.1 Radius valley

The composition of mini-Neptunes plays an important role in our understanding of the radius valley. Whether super-Earths and mini-Neptunes are the same population that evolved differently, or are two distinct populations that formed differently, is still widely debated. In Fig. 10, we plot the observed planet radius distribution adapted from Fulton et al. (2017). The well-known radius gap feature of the exoplanet population is apparent from 1.5 to 2.0 R_{\oplus} . The overplotted red line represents the radius of TOI-757 b, showing that the planet lies to the right of the valley and is among the abundant population of mini-Neptunes. With our newly characterized mass measurement of TOI-757 b, we are able to derive a density measurement of the planet and understand its potential composition better, giving us clues as to whether it belongs to the mini-Neptune population or whether it could be a water world.

6.2 Mass–radius relation

To understand the possible internal composition of TOI-757 b, we calculate the expected density of the planet based on the mass and radius measurements derived from MCMC fits, giving us an implied density of $\rho_p = 3.6 \pm 0.8 \text{ g cm}^{-3}$. It is unclear whether the planet could harbour any water/ice components or whether it has a fraction of a H/He envelope. The composition of TOI-757 b might include

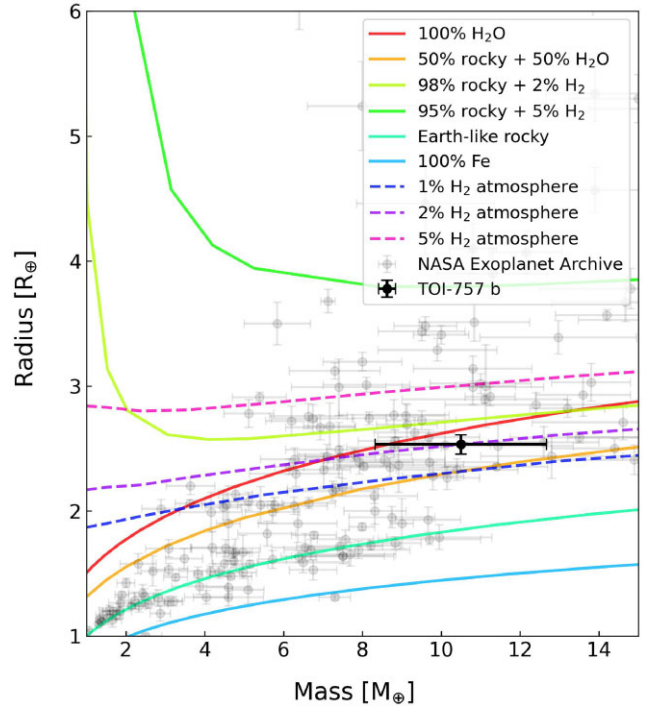


Figure 11. Mass–radius diagram showing composition tracks from Zeng et al. (2019) in solid lines, assuming a temperature of 500 K and a surface pressure level of 1 mbar. We also show composition tracks from Lopez & Fortney (2014) in dashed lines, assuming an insolation flux of 10 on the planet (relative to the solar constant) and a stellar age of 10 Gyr. The black dot represents TOI-757 b, and the grey dots show confirmed exoplanets with mass and radius uncertainties <20 per cent, taken from the NASA Exoplanet Archive.

a significant fraction of water/ice, since water-rich worlds form outside the snow line and later migrate inwards, while rocky planets are expected to form within the snow line (Armitage, Eisner & Simon 2016). This raises questions about the formation mechanisms of the mini-Neptune population, and might allude to possible migration scenarios in the evolutionary history of these planets, particularly in the case of TOI-757 b. In such cases, atmospheric studies may be needed to distinguish between water-rich planets and H/He atmospheres.

To investigate this, we plot TOI-757 b on a mass–radius diagram in Fig. 11, with composition tracks from Zeng et al. (2019) in solid lines, assuming a temperature of 500 K and a surface pressure level of 1 mbar. While the Zeng et al. (2019) composition tracks have been widely used in the exoplanet community, they assume a constant specific entropy. This could pose issues when determining the inner composition of small planets, such as TOI-757 b. Thus, following the suggestion from Rogers, Schlichting & Owen (2023), we also show composition tracks from Lopez & Fortney (2014), which assume a constant planet age. These tracks are shown in Fig. 11 using dashed lines, assuming an insolation flux of 10 on the planet (relative to the solar constant) and a stellar age of 10 Gyr. The black dot represents TOI-757 b, and the grey dots show confirmed exoplanets with mass and radius uncertainties <20 per cent, taken from the NASA Exoplanet Archive⁹ (Akeson et al. 2013) as of 2024 January 25.

⁹<https://exoplanetarchive.ipac.caltech.edu>

Normally, there is a clear degeneracy between composition models when trying to separate H/He envelopes and water–rich atmospheres for mini–Neptunes. This becomes particularly difficult to constrain for single–planet systems, even with well–characterized mass and radius measurements (Rogers et al. 2023). While the position of TOI–757 b on the mass–radius diagram falls with other known mini–Neptunes (see Fig. 11), the planet composition remains vague due to the aforementioned model degeneracy. Looking at the Zeng et al. (2019) models, the composition of TOI–757 b appears to be consistent with a 100 per cent water world. However, we note that some studies indicate that a planet entirely made of water is not considered to be physically realistic (see e.g. Marboeuf et al. 2014). The Lopez & Fortney (2014) models seem to suggest a composition of a rocky core with a 2 per cent hydrogen atmosphere for TOI–757 b. To further investigate which composition is more likely for our system, we performed internal composition modelling described in Section 6.3. While a H/He gas layer was found to be well constrained for the system, we were unable to rule out the presence of a significant water fraction.

To be able to more confidently characterize TOI–757 b’s composition, atmospheric observations would be necessary in order to break the degeneracy between planet composition models for mini–Neptunes and water–rich worlds. This could potentially make TOI–757 b an exciting target for *JWST* observations, and the host star is also bright, making it favourable for atmospheric follow-up. To evaluate whether TOI–757 b is suitable for atmospheric characterization or not, we use the two metrics introduced by Kempton et al. (2018), the transmission spectroscopy metric (TSM) and the emission spectroscopy metric (ESM). We find that TOI–757 b has a TSM of 44.75 and an ESM of 3.19. Considering the recommended metric thresholds of $TSM > 90$ and $ESM > 7.5$ for small mini–Neptunes (Kempton et al. 2018), this makes TOI–757 b a challenging (albeit still interesting) target for atmospheric observations given these guidelines.

6.3 Internal structure modelling and atmospheric evolution

We used the method introduced in Leleu et al. (2021) and based on Dorn et al. (2017) to model the internal structure of TOI–757 b. The planet is modelled as a fully spherically symmetric structure consisting of an inner iron core with up to 19 per cent sulphur (Hakim et al. 2018), a silicate mantle made up of Si, Mg, and Fe (Sotin, Grasset & Mocquet 2007), a condensed water layer (Haldemann et al. 2020), and a fully separately modelled H/He envelope (Lopez & Fortney 2014). We assume that the Si/Mg/Fe ratios of the planet match those of the star exactly (Thiabaud et al. 2015).

A Bayesian inference scheme is then used to infer posterior distributions for the composition and interior structure of the planet, with the radius ratio, period, and RV semi–amplitude of the planet, along with the stellar parameters (radius, mass, age, effective temperature, and Si, Mg and Fe abundances) as input parameters. We chose priors that are uniform in log for the mass of the H/He envelope and uniform on the simplex for the mass fractions of the inner iron core, silicate mantle, and water layer (all with respect to the solid part of the planet without the H/He envelope). In agreement with Thiabaud et al. (2014) and Marboeuf et al. (2014), we chose an upper limit of 50 per cent for the water mass fraction. We do note that results of our analysis do depend to some extent on the chosen priors, as determining the internal structure of a planet is a highly degenerate problem.

Fig. 12 shows the results of our analysis. While the presence of a water layer remains unconstrained with a tendency towards larger water mass fractions, the mass of the H/He layer of TOI–757 b is

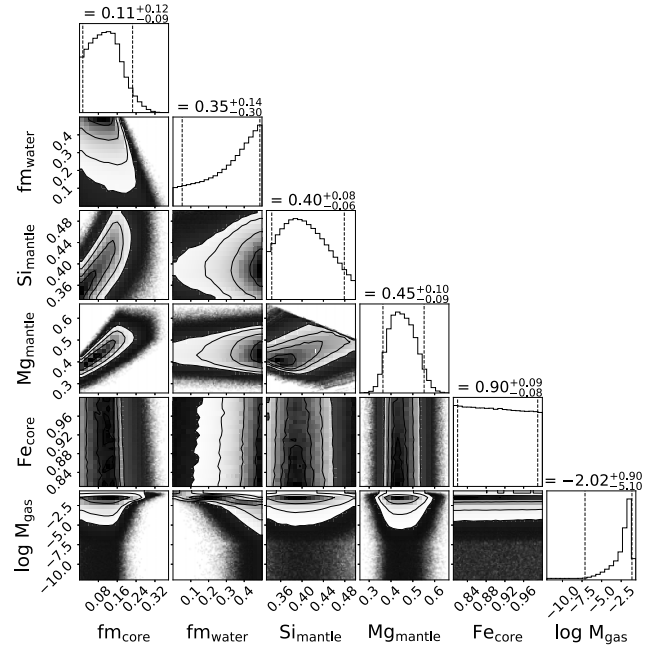


Figure 12. Posterior distributions of the most relevant internal structure parameters for TOI–757 b. The values above the histograms are the median and the 5th and 95th percentiles of the distributions, same as the dashed lines. The plotted internal structure parameters are the iron core and water mass fractions of the solid planet without gas, the molar fraction of Si and Mg within the mantle and of Fe in the core and the \log_{10} of the absolute gas mass in Earth masses.

quite well constrained with a median value of $M_{\text{gas}} = 0.01^{+0.07}_{-0.01} M_{\oplus}$, where the uncertainties correspond to the 5th and 95th percentiles of the posterior. This corresponds to a thickness of $R_{\text{gas}} = 0.28^{+0.38}_{-0.27} R_{\oplus}$ of the gas layer.

6.4 Tidal damping of the eccentricity and its consequences

We estimate the current time-scale for the decay of the eccentricity of TOI–757 b adopting the model by Hut (1981). To apply that model, we express the product of their constant tidal time lag Δt_p by the Love number of the planet $k_{2,p}$ as a function of the modified tidal quality factor Q'_p of the planet itself as $k_{2,p} \Delta t_p = 3/(2Q'_p n)$, where $n = 2\pi/P$ is the orbit mean motion with P being the orbital period.

The rheology of mini–Neptune planets is unknown, thus we investigate two extreme cases. The former assumes $Q'_p = 10^5$ that is comparable with the modified tidal quality factor of Uranus or Neptune as estimated by, e.g. Tittlemore & Wisdom (1990) and Ogilvie (2014), and is appropriate for a body where the dissipation of the tidal energy occurs in a fluid interior. The latter assumes that tides are mainly dissipated inside a rocky core encompassing the whole mass of the planet $4.4 M_{\oplus}$, but with a radius of $1.3 R_{\oplus}$ that corresponds to the peak of the smaller radius component of the distribution of the transiting planets as observed by Kepler (Fulton et al. 2017). In the latter case, we adopt $Q'_p = 300$ as in the case of our Earth (Henning, O’Connell & Sasselov 2009) and neglect the small mass and tidal dissipation in the fluid outer envelope of the planet in comparison with those in its rocky core. The present eccentricity tidal decay time-scale is found to be $\tau_e \equiv |e/(de/dt)| \sim 1040$ Gyr in the former case, or $\tau_e \sim 90$ Gyr in the latter case, much longer than the Hubble time in both the cases. Therefore, we conclude that the present eccentricity may well be the result of processes that happened

during the formation of the planet and/or its migration to the present distance from its host star. We find that tidal dissipation inside the star has a negligible effect on the evolution of the eccentricity because of the relatively large separation of the planet and its small mass.

An interesting consequence of the eccentric orbit of TOI-757 b is its expected pseudosynchronization with the orbital motion, that is, its rotation is predicted to be faster than the orbital mean motion n because tides tend to synchronize planet rotation with the orbital velocity at periastron where they are stronger. Using the formalism of Leconte et al. (2010), we predict a rotation period of the planet of 8.8 d, that is, 1.99 times shorter than its orbital period. Such a state of pseudosynchronization is reached after a time-scale of ~ 6 Myr for $Q'_p = 10^5$ or ~ 0.14 Myr for $Q'_p = 300$, either of which is significantly shorter than the estimated age of the host star.

We expect tides to dissipate energy inside the planet due to its eccentric orbit and pseudosynchronous rotation. The maximum dissipated power is predicted for $Q'_p = 300$ and is of $\sim 2.3 \times 10^{16}$ W giving a heat flux of ~ 7.1 W m $^{-2}$ at the top of its atmosphere with a radius of $2.5 R_\oplus$. Such a flux is larger than that measured in the case of Jupiter where the heat flux from the interior of the planet is of ~ 5.4 W m $^{-2}$ (Guillot et al. 2004). Therefore, it may play a relevant role in the atmospheric dynamics of the planet. On the other hand, adopting $Q'_p = 10^5$, we find a dissipated power of 1.9×10^{15} W and a surface flux of only ~ 0.6 W m $^{-2}$.

6.5 High-eccentricity and formation mechanisms

Our findings reveal that TOI-757 b is a transiting single-planet system on a highly eccentric orbit of $e = 0.39^{+0.08}_{-0.07}$. It has one of the highest eccentricities among all precisely known exoplanets (with mass and radius uncertainties < 20 per cent) in the period, radius, and mass ranges of the mini-Neptune population ($P < 100$ d, $5 < M_p [M_\oplus] < 40$, $2 < R_p [R_\oplus] < 5$), as can be seen in Fig. 13. Van Eylen et al. (2019) report that, on average, single-planet systems appear to exhibit higher eccentricities than multiplanet systems for transiting planets. Using transit durations to estimate orbital eccentricities, Van Eylen et al. (2019) find that the typical eccentricity of single-planet systems is $e = 0.32 \pm 0.06$. Xie et al. (2016) also find an average eccentricity of ~ 0.3 for single transiting planet systems. So perhaps within this context, it is not too surprising that TOI-757 b is highly eccentric. While TOI-757 b sits among the abundant population of mini-Neptunes in relation to the radius valley, it is uniquely one of the very few highly eccentric mini-Neptunes, as can be seen in Fig. 13. This makes it an interesting target within the context of the eccentricity distribution of small planets, and poses important questions regarding its formation history.

Petigura et al. (2017) studied a sample of four sub-Saturn-sized planets showing a wide range of masses measured using Keck/HIRES RV data, which implies that their core and envelope masses are diverse in nature. Looking at Fig. 11 from their study, we can see that the majority of planets from the sub-Saturn population within a similar planet mass and equilibrium temperature range to TOI-757 b are all found to be non-eccentric ($e < 0.1$). So, even looking at planets larger in size in comparison to the mini-Neptune population, TOI-757 b stands out as a unique case.

The high eccentricity of TOI-757 b suggests that the history of the planet might be different in comparison with other mini-Neptunes, owing to an evolution path involving eccentricity excitation induced by the gravitational interactions with a companion. As such, we might expect different atmospheric properties in such scenarios. Additionally, when we modelled the tidal dissipation time-scale

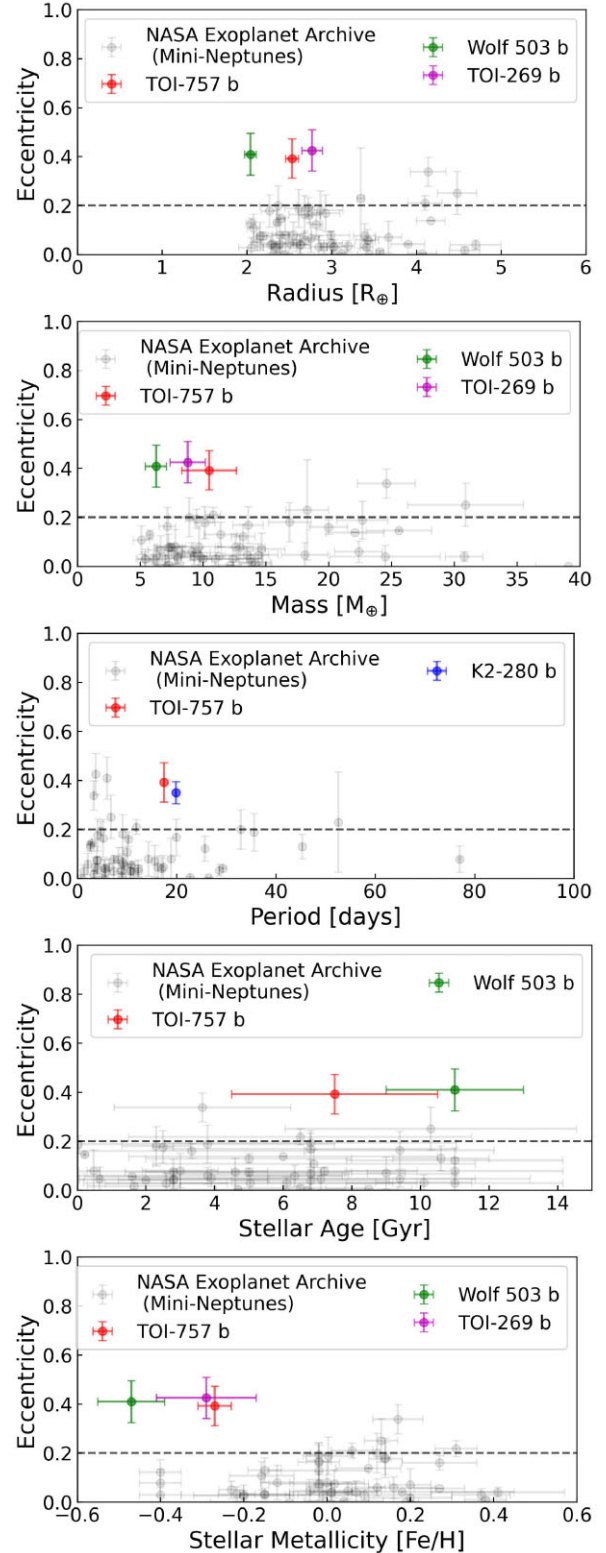


Figure 13. From top to bottom (with Eccentricity on the y-axis), we plot the radius, mass, period, stellar age, and stellar metallicity [Fe/H] for precisely characterized mini-Neptunes. The red dot represents TOI-757 b, the blue dot represents K2-280 b, the green dot represents Wolf 503 b, and the magenta dot represents TOI-269 b. The grey dots show confirmed exoplanets taken from the NASA Exoplanet Archive with mass and radius uncertainties < 20 per cent, filtered for the mini-Neptune population ($P < 100$ d, $5 < M_p [M_\oplus] < 40$, $2 < R_p [R_\oplus] < 5$).

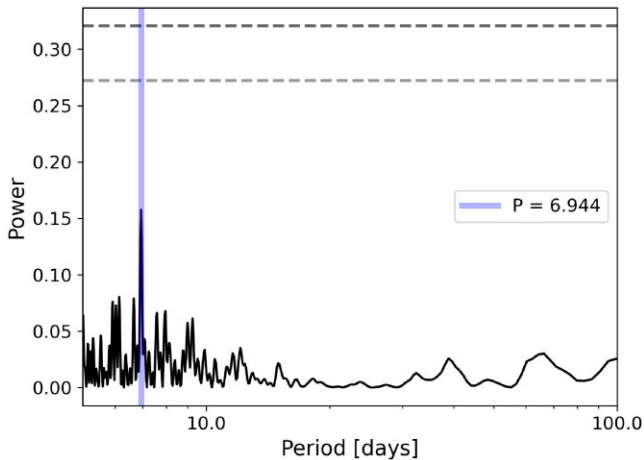


Figure 14. GLS periodogram of the RV residuals (after subtracting the orbit of TOI-757 b as well as the GP noise model). The dashed horizontal lines represent the FAP significance at the 0.1 per cent (dark grey) and 1 per cent (light grey) levels.

for the system (see Section 6.4), even across extreme cases, the circularization time-scale was found to be much longer than the age of the system. As such, the planet’s present-day eccentricity is consistent with a number of plausible scenarios. One possibility is that, regardless of whether the eccentricity developed intrinsically or whether it was induced by a perturber, the planet could have attained its eccentricity close to the formation period of the system. Given this scenario, it is also possible that a potential perturber would have been ejected from the system earlier on and can no longer be detected. However, we would like to point out that a long circularization time-scale does not necessarily prove that the eccentricity arose in the distant past.

To further investigate this scenario, we searched the residuals of the RV data for any signs of periodicity, which could indicate further stellar activity or possibly an outer companion. We found no significant peaks in the GLS periodograms (see Fig. 14), even out to an FAP level of 10 per cent, as well as a lack of evidence for any companions in the high-contrast imaging and the *Gaia* data. The absence of the peak likely suggests that the outer planet (assuming it is responsible for the large eccentricity of TOI-757 b) is very small in mass or it has a much longer period (or it has been ejected from the system already).

However, it is important to note that TOI-757 b’s properties are in agreement with the scenario presented by Huang, Petrovich & Deibert (2017), which showed that planetary systems that were able to survive scattering due to a giant outer companion exhibited higher eccentricity and lower multiplicity. This would put TOI-757 b amongst an exciting population of exoplanets for further study and would make it an interesting system for follow-up. In particular, to verify whether high eccentricity tidal migration due to planet-planet interactions is the correct scenario for TOI-757 b’s evolutionary history, further RV measurements over a longer baseline would aid in searching for the existence of a possible distant giant perturber. Another possible mechanism for the high eccentricity of the planet is self-excitation, where the planet migrates via planet-disc interactions. However, planets are expected to have lower eccentricities in this scenario ($e < 0.3$), so this is unlikely to be the mechanism for TOI-757 b’s formation history given its high eccentricity (e.g. Petrovich, Tremaine & Rafikov 2014; Matsumoto, Nagasawa & Ida 2015; Van Eylen et al. 2019).

To attempt to further understand the planet’s formation history and evolution given its high eccentricity, we compare TOI-757 b to other similar eccentric mini-Neptunes that have been previously studied and well characterized. In Fig. 13, we plot TOI-757 b against the confirmed mini-Neptune population ($P < 100$ d, $2 < R_p < 5 R_\oplus$, $5 < M_p < 40 M_\oplus$), taken from the NASA Exoplanet Archive with mass and radius uncertainties < 20 per cent. When looking at relatively small exoplanets with longer periods, the closest planet to TOI-757 b is K2-280 b. From the $M_p - e$, $R_p - e$, and $[\text{Fe}/\text{H}] - e$ plots, we jointly find two planets with similar properties to TOI-757 b, namely, TOI-269 b and Wolf 503 b.

K2-280 b was analysed by Nowak et al. (2020), who characterized the planet as a warm sub-Saturn with a radius of $7.5 \pm 0.4 R_\oplus$ and a mass of $37.1 \pm 5.6 M_\oplus$, yielding a low planet density of $0.5^{+0.1}_{-0.1} \text{ g cm}^{-3}$. While the planet sits in a different parameter space on the mass-radius diagram, it is a transiting single-planet system with a similar long-period orbit (~ 19.9 d) and eccentricity ($0.35^{+0.05}_{-0.04}$) to TOI-757 b, which could indicate a similar formation mechanism that resulted in the high eccentricity of our system (e.g. migration). The study attributes the moderate eccentricity of K2-280 b to a formation pathway due to planet-planet gravitational interactions.

TOI-269 b was characterized by Cointepas et al. (2021), who report a radius of $2.8 \pm 0.1 R_\oplus$, and a mass of $8.8 \pm 1.4 M_\oplus$, resulting in a planet density of $2.3^{+0.5}_{-0.4} \text{ g cm}^{-3}$. The host star is reported to have a low metallicity of $[\text{Fe}/\text{H}] = -0.3 \pm 0.1$, which is very similar to TOI-757. This study discusses the possibility of planet-planet migration as the source of the planet’s high eccentricity ($e = 0.4 \pm 0.1$). While it is a short-period planet ($P \approx 3.7$ d) orbiting an M2 dwarf star, and as such the host star conditions would affect the planet formation slightly differently, it is interesting that it might possibly share a similar formation history to TOI-757 b that led it to obtain an eccentric orbit.

Lastly, we note the properties of Wolf 503 b, a mini-Neptune that was studied by Peterson et al. (2018), Polanski et al. (2021), and Bonomo et al. (2023). This is possibly the most similar system to TOI-757 b, orbiting a K-dwarf host star. The planet is eccentric (0.4 ± 0.1), with a radius of $2.04 \pm 0.07 R_\oplus$ and a mass of $6.3 \pm 0.7 M_\oplus$, giving a bulk density of $2.9^{+0.5}_{-0.4} \text{ g cm}^{-3}$. Wolf 503 is similar to TOI-757 in that it is an old system (11 ± 2 Gyr) that is also metal-poor ($[\text{Fe}/\text{H}] = -0.5 \pm 0.1$), which indicates it might share a similar evolution history to our star. Despite initial predictions of the existence of a long-period companion as the main driving source of the planet’s high eccentricity, the system was later followed up over a long RV campaign, where no outer planet companions were found (Bonomo et al. 2023). The interior composition modelling done in Polanski et al. (2021) shows that their reported density is consistent with an Earth-like core combined with either a significant water mass fraction (45^{+19}_{-16} per cent), or a 0.5 ± 0.3 per cent H/He atmosphere. The study also suggests that Wolf 503 b would be a good target to test XUV-driven mass-loss mechanisms due to the predicted low H/He mass fraction, as well as the old age of the host star. The system’s strikingly similar properties to our planet suggest that TOI-757 b might also be favourable for testing theories of XUV-driven mass-loss.

Based on the plots in Fig. 13, we can see that TOI-757 b stands out as part of a sparsely populated group of eccentric mini-Neptune planets. The $M_p - e$ plot in particular highlights that low-mass planets do not often appear to be eccentric. This could in part be because systems like TOI-757 b are hard to observe. Eccentric planet systems are most likely at longer periods, and such systems often lack precise mass measurements and are also less likely to transit.

The Age– e plot does not show any visible trends, but stellar ages are also harder to estimate and have much larger uncertainties, so we cannot make any reliable conclusions from this plot. The $[\text{Fe}/\text{H}]$ – e plot on the other hand is intriguing because it shows two separate sub-groups of planets. There is a large group of planets (but not highly eccentric) between $\sim 0 < [\text{Fe}/\text{H}] < 0.2$. Then, we observe a very small subset of planets (three planets, including TOI–757 b) that are completely isolated from this large population, and all of them have much higher eccentricities ($e > 0.4$). Two out of the three planets in this subset (TOI–757 b and Wolf 503 b) are part of systems that are old in age and low in metallicity, while the third system (TOI–269 b) is low in metallicity but does not have a well-constrained age measurement. All three of these cases are single-planet systems, with the source of their eccentricity still unknown.

While TOI–757 b’s high eccentricity is unlikely due to self-excitation, and studies of eccentric systems focus on scenarios involving gravitational interactions with an outer companion, we propose the possibility of a more intrinsic explanation for the high eccentricity due to star–star interactions during the earlier epoch of the Galactic disc formation, given the low metallicity and the older age of TOI–757. More specifically, the high eccentricity of TOI–757 b could be due to star–star interactions during the earlier epoch of the Galactic disc formation. Our star is old in age (7.5 ± 3.0 Gyr) and is also placed during the transition period between thick and thin discs based on its α/Fe (0.08 ± 0.05) and Fe/H (-0.27 ± 0.04) measurements (Ciucă et al. 2021). During this epoch, the Milky Way disc has a higher gas fraction, and the star formation rate is higher as well. Stars in this period may be forming in the denser molecular clouds, which could increase the probability of star–star interactions (Portegies Zwart & Jilková 2015), and this alternative effect may become important for these old stars. This might be another, more intrinsic explanation for the high eccentricity of TOI–757 b coming from the initial conditions of the environment in which the planet was formed, given the older age of the system. As such, the discovery of high-eccentricity mini-Neptunes around old metal-poor stars could open up the new possibility of the Milky Way environment affecting the formation of the exoplanet, which has not been previously well studied as a potential scenario for the evolution path of eccentric systems.

7 SUMMARY AND CONCLUSIONS

In this paper, we present the confirmation and the planet properties of TOI–757 b, a transiting mini-Neptune that was discovered by the *TESS* mission. We clearly detect TOI–757 b in the *TESS* light curves, and we also use the *CHEOPS* photometric follow-up observations of the system, allowing us to derive a more precise radius measurement of the planet, along with ground-based photometry from WASP, KELT, and LCOGT. We present multiple RV monitoring campaigns that have been carried out using the HARPS, ESPRESSO, and PFS high-resolution spectrographs to measure the mass of TOI–757 b, where we find a clear confirmation of the planet.

Through the photometric and RV analyses, we find that TOI–757 b has a radius of $R_p = 2.5 \pm 0.1 R_\oplus$ and a mass of $M_p = 10.5^{+2.2}_{-2.1} M_\oplus$, giving us an implied density of $\rho_p = 3.6 \pm 0.8 \text{ g cm}^{-3}$. It is unclear whether TOI–757 b harbours any water/ice components or whether it has a fraction of a H/He envelope. Our internal composition modelling reveals that, while the existence of some quantity of H/He was found to be required, the actual quantity is degenerate with the amount of water, and neither scenario is well constrained. We highlight the importance of acquiring atmospheric observations to break the degeneracy between planet composition models for

mini-Neptunes and water-rich worlds, which would particularly be useful for TOI–757 b given its location on the M–R diagram.

We find the planet to be highly eccentric with $e = 0.39^{+0.08}_{-0.07}$, making it one of the very few highly eccentric mini-Neptunes among all precisely known exoplanets from the mini-Neptune population. Additionally, the tidal circularization time-scale of the planet was found to be much longer than the age of the system, indicating that the planet likely attained its eccentricity very early on during the formation stages of the system. Based on comparisons to other similar eccentric systems, we find a likely scenario for TOI–757 b’s formation to be high eccentricity excitation due to a distant outer companion. We additionally propose the possibility of a more intrinsic explanation for the high eccentricity due to star–star interactions during the earlier epoch of the Galactic disc formation, given the low metallicity and the older age of TOI–757.

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DATA AVAILABILITY

The photometric and radial velocity data used in this work are publicly available at CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <https://cdsarc.cds.unistra.fr/viz-bin/cat/JMNRAS/533/1>. The coding scripts used for the analyses can be made available upon reasonable request.

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APPENDIX A: RADIAL VELOCITY DATA SETS

Table A1. Radial velocities, spectral activity indicators, and exposure times for the HARPS, ESPRESSO, and PFS measurements. The times are given in *TESS* BJD time (BTJD), which is defined as BJD – 2457000.

Telescope	Time (BTJD)	RV (m s ⁻¹)	σ_{RV} (m s ⁻¹)	BIS (m s ⁻¹)	σ_{BIS} (m s ⁻¹)	FWHM (m s ⁻¹)	σ_{FWHM} (m s ⁻¹)	S-index	$\sigma_{S-Index}$	H α	$\sigma_{H\alpha}$	log R' _{HK}	$\sigma_{\log R'_{HK}}$	T _{exp} (s)
HARPS	2236.80	5.78	1.00	-20.5	2.0	6595.88	2.0	0.22	0.001	0.9	---	-4.8	0.006	1800.0
HARPS	2238.75	5.6	0.91	-16.36	1.81	6599.89	1.81	0.23	0.001	0.89	---	-4.81	0.005	1800.0
HARPS	2239.73	4.0	0.85	-21.2	1.69	6598.55	1.69	0.23	0.001	0.89	---	-4.8	0.005	1800.0
HARPS	2239.79	2.47	0.77	-17.76	1.55	6593.97	1.55	0.23	0.001	0.89	---	-4.8	0.004	1800.0
HARPS	2240.85	1.77	0.88	-19.32	1.75	6597.62	1.75	0.23	0.001	0.89	---	-4.8	0.004	1500.0
HARPS	2242.81	-0.95	0.84	-17.01	1.68	6594.76	1.68	0.23	0.001	0.9	---	-4.8	0.004	1800.0
HARPS	2243.86	-1.05	0.80	-17.79	1.6	6590.69	1.6	0.23	0.001	0.9	---	-4.81	0.004	1600.0
HARPS	2244.86	-2.82	0.96	-20.25	1.93	6587.7	1.93	0.23	0.001	0.9	---	-4.81	0.004	1800.0
HARPS	2245.81	-3.29	1.06	-24.3	2.12	6592.22	2.12	0.23	0.002	0.9	---	-4.81	0.008	1500.0
HARPS	2246.83	-0.71	1.09	-17.21	2.18	6578.91	2.18	0.23	0.001	0.9	---	-4.81	0.006	1500.0
HARPS	2250.86	5.27	1.32	-26.68	2.64	6577.18	2.64	0.22	0.001	0.9	---	-4.83	0.006	1800.0
HARPS	2261.84	-3.25	1.02	-24.61	2.04	6591.91	2.04	0.23	0.002	0.9	---	-4.79	0.006	1500.0
HARPS	2263.79	0.0	1.09	-23.9	2.17	6587.85	2.17	0.23	0.002	0.9	---	-4.79	0.006	1500.0
HARPS	2264.77	2.1	0.98	-24.25	1.97	6582.24	1.97	0.22	0.001	0.9	---	-4.81	0.005	1500.0
HARPS	2266.77	8.44	0.93	-19.67	1.86	6582.97	1.86	0.22	0.001	0.9	---	-4.82	0.005	1500.0
HARPS	2267.83	7.52	0.85	-22.06	1.71	6585.02	1.71	0.22	0.001	0.91	---	-4.84	0.005	1500.0
HARPS	2268.86	7.21	1.01	-24.65	2.03	6587.25	2.03	0.22	0.001	0.91	---	-4.83	0.006	1500.0
HARPS	2269.74	5.2	0.86	-25.0	1.71	6592.71	1.71	0.22	0.001	0.9	---	-4.83	0.004	1500.0
HARPS	2273.73	2.03	1.06	-19.3	2.13	6592.05	2.13	0.23	0.002	0.9	---	-4.8	0.007	1500.0
HARPS	2274.69	-0.7	0.97	-15.44	1.94	6599.29	1.94	0.23	0.002	0.9	---	-4.81	0.006	1500.0
HARPS	2275.82	-4.16	1.08	-17.52	2.16	6593.96	2.16	0.22	0.002	0.89	---	-4.82	0.009	1500.0
HARPS	2276.82	-3.63	0.98	-16.25	1.96	6593.83	1.96	0.23	0.002	0.9	---	-4.8	0.008	1500.0
HARPS	2277.78	-5.45	0.99	-17.14	1.98	6580.53	1.98	0.22	0.001	0.9	---	-4.82	0.004	1500.0
HARPS	2286.84	2.87	1.05	-25.27	2.11	6634.04	2.11	0.21	0.002	0.89	---	-4.85	0.007	1500.0
HARPS	2288.79	-2.93	1.50	-21.62	3.01	6586.59	3.01	0.21	0.002	0.9	---	-4.85	0.01	1500.0
HARPS	2291.75	-3.02	0.96	-21.93	1.91	6571.49	1.91	0.22	0.001	0.91	---	-4.83	0.006	1500.0
HARPS	2364.67	-0.29	1.35	-12.28	2.7	6584.38	2.7	0.21	0.002	0.91	---	-4.85	0.01	1500.0
ESPRESSO	2308.65	-0.94	0.61	-73.03	1.21	6896.45	1.21	0.17	0.0002	0.24	0.00007	-5.11	0.001	600.0
ESPRESSO	2310.82	-0.22	0.76	-70.83	1.51	6887.61	1.51	0.16	0.0004	0.24	0.00008	-5.19	0.002	600.0
ESPRESSO	2313.75	-0.49	0.40	-71.49	0.8	6894.54	0.8	0.20	0.0001	0.24	0.00004	-4.96	0.0005	600.0
ESPRESSO	2316.61	-0.66	0.64	-71.03	1.28	6879.84	1.28	0.18	0.0003	0.24	0.00007	-5.08	0.001	600.0
ESPRESSO	2318.64	2.95	0.43	-68.77	0.86	6883.65	0.86	0.20	0.0001	0.24	0.00005	-4.99	0.0006	600.0
ESPRESSO	2321.73	4.02	0.65	-72.8	1.31	6884.01	1.31	0.17	0.0003	0.24	0.00007	-5.12	0.002	600.0
ESPRESSO	2324.57	-1.15	0.83	-76.38	1.66	6882.39	1.66	0.16	0.0004	0.24	0.00009	-5.19	0.003	600.0
ESPRESSO	2327.54	0.008	0.44	-76.2	0.87	6884.69	0.87	0.20	0.0002	0.24	0.00005	-4.96	0.0006	600.0
ESPRESSO	2329.58	0.49	0.69	-76.38	1.38	6896.57	1.38	0.18	0.0003	0.24	0.00007	-5.07	0.001	600.0
ESPRESSO	2332.58	0.4	0.54	-68.78	1.07	6907.25	1.07	0.20	0.0002	0.24	0.00006	-4.98	0.0008	600.0
ESPRESSO	2335.77	1.89	0.53	-67.36	1.07	6904.64	1.07	0.20	0.0002	0.24	0.00006	-4.98	0.0008	600.0
ESPRESSO	2341.54	-0.36	0.80	-67.41	1.6	6890.32	1.6	0.16	0.0004	0.23	0.00009	-5.19	0.002	600.0
ESPRESSO	2344.68	-0.77	0.41	-73.07	0.81	6883.64	0.81	0.20	0.0001	0.24	0.00004	-4.99	0.0005	600.0
ESPRESSO	2349.73	-1.93	0.60	-74.55	1.2	6875.9	1.2	0.15	0.0003	0.23	0.00006	-5.24	0.002	600.0
ESPRESSO	2371.66	4.38	0.52	-63.3	1.03	6903.33	1.03	0.22	0.0002	0.24	0.00006	-4.9	0.0006	600.0
ESPRESSO	2374.61	-0.61	0.45	-68.73	0.9	6890.44	0.9	0.22	0.0002	0.24	0.00005	-4.91	0.0005	600.0
ESPRESSO	2406.57	3.12	0.53	-72.97	1.06	6880.69	1.06	0.20	0.0002	0.24	0.00006	-4.97	0.0008	600.0
ESPRESSO	2410.53	-1.89	0.64	-69.47	1.28	6870.54	1.28	0.16	0.0003	0.23	0.00007	-5.18	0.002	600.0
ESPRESSO	2413.52	-4.56	0.48	-74.56	0.96	6870.99	0.96	0.20	0.0002	0.23	0.00005	-4.97	0.0007	600.0
ESPRESSO	2415.52	-5.82	0.51	-78.36	1.02	6874.03	1.02	0.19	0.0002	0.23	0.00005	-5.0	0.0008	600.0
ESPRESSO	2430.46	-1.44	0.47	-73.78	0.94	6890.0	0.94	0.23	0.0002	0.24	0.00005	-4.88	0.0005	600.0
ESPRESSO	2432.51	3.58	1.55	-75.34	3.1	6914.51	3.1	0.18	0.001	0.24	0.0002	-5.06	0.005	600.0
PFS	2207.84	-2.49	0.89	---	---	---	---	0.23	0.01	---	---	---	---	751.0
PFS	2207.85	-3.64	0.81	---	---	---	---	0.22	0.01	---	---	---	---	750.0
PFS	2211.86	-1.58	0.62	---	---	---	---	0.21	0.01	---	---	---	---	1200.0
PFS	2212.84	-1.15	0.89	---	---	---	---	0.24	0.01	---	---	---	---	600.0
PFS	2212.85	0.43	0.84	---	---	---	---	0.24	0.01	---	---	---	---	600.0
PFS	2213.84	0.73	0.82	---	---	---	---	0.25	0.01	---	---	---	---	901.0
PFS	2213.85	-0.63	0.90	---	---	---	---	0.24	0.01	---	---	---	---	900.0
PFS	2214.84	3.68	1.03	---	---	---	---	0.25	0.01	---	---	---	---	600.0
PFS	2214.84	-0.17	1.05	---	---	---	---	0.26	0.01	---	---	---	---	600.0
PFS	2215.86	-1.26	0.85	---	---	---	---	0.24	0.01	---	---	---	---	600.0
PFS	2215.87	-0.48	0.88	---	---	---	---	0.25	0.01	---	---	---	---	600.0
PFS	2239.80	0.0	0.88	---	---	---	---	0.24	0.01	---	---	---	---	1200.0
PFS	2356.59	7.15	1.32	---	---	---	---	0.22	0.01	---	---	---	---	1001.0

Table A1 – continued

Telescope	Time (BTJD)	RV (m s ⁻¹)	σ_{RV} (m s ⁻¹)	BIS (m s ⁻¹)	σ_{BIS} (m s ⁻¹)	FWHM (m s ⁻¹)	σ_{FWHM} (m s ⁻¹)	S-index	$\sigma_{S-Index}$	H α	$\sigma_{H\alpha}$	log R' _{HK}	$\sigma_{\log R'_{HK}}$	T _{exp} (s)
PFS	2356.69	5.36	1.36	---	---	---	---	0.24	0.01	---	---	---	---	1501.0
PFS	2363.57	-0.34	1.14	---	---	---	---	0.21	0.01	---	---	---	---	900.0
PFS	2363.65	-0.83	1.15	---	---	---	---	0.22	0.01	---	---	---	---	1201.0
PFS	2596.85	-0.08	0.81	---	---	---	---	0.22	0.01	---	---	---	---	1001.0
PFS	2597.85	5.38	0.79	---	---	---	---	0.22	0.01	---	---	---	---	1201.0
PFS	2597.86	3.94	0.80	---	---	---	---	0.21	0.01	---	---	---	---	1001.0
PFS	2598.81	8.38	0.98	---	---	---	---	0.24	0.01	---	---	---	---	1201.0
PFS	2598.82	7.82	1.19	---	---	---	---	0.27	0.01	---	---	---	---	1200.0
PFS	2599.84	6.22	0.98	---	---	---	---	0.25	0.01	---	---	---	---	900.0
PFS	2599.85	6.47	0.88	---	---	---	---	0.24	0.01	---	---	---	---	900.0
PFS	2601.86	0.99	0.80	---	---	---	---	0.22	0.01	---	---	---	---	901.0

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