



THE OKA PRINCIPLE FOR TAME FAMILIES OF STEIN MANIFOLDS

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Magneto-optical Kerr effect in an A-type antiferromagnet

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Magneto-optic Kerr effect (MOKE) is a powerful probe of broken time-reversal symmetry ($\mathcal{T}$), typically used to study ferromagnets. While MOKE has been observed in some antiferromagnets (AFMs) with vanishing magnetization, it is often associated with structures whose symmetry is lower than basic collinear, bipartite order. In contrast, theory predicts a mechanism for MOKE intrinsic to all AFMs of A-type, i.e. layered AFMs in which ferromagnetic layers are antiferromagnetically aligned. Here we report the experimental confirmation of this mechanism in a bulk AFM. We achieve this by measuring the imaginary component of MOKE as a function of photon energy in MnBi_2Te_4 , an A-type AFM where $\mathcal{T}$ is preserved in combination with a translation, and comparing the experimental results with model calculations. Our model suggests that observable MOKE should be expected in all collinear A-type AFMs with out-of-plane spin order, thus enabling optical detection of AFM domains and expanding the scope of MOKE to few-layer AFMs.

The detection of broken time-reversal symmetry ($\mathcal{T}$) in quantum materials is of fundamental interest and practical relevance. Recent advances in the synthesis and exfoliation of van der Waals magnets have highlighted the critical role of optical techniques in detecting $\mathcal{T}$ -breaking in samples just a few atomic layers thick^{1–9}, whose small mass poses a challenge for bulk probes of magnetism. The magneto-optic Kerr effect (MOKE), which is the difference in reflectivity for left and right circularly polarized (LCP and RCP) light, is routinely used for detection of ferromagnetic (FM) order. Which classes of antiferromagnetic (AFM) order yield a measurable MOKE signal, and the underlying mechanism in each case, are questions of long-standing fascination. Here we show that MOKE is a more powerful and general probe of AFM order than previously thought, with implications for research and applications of both bulk and few-layer AFMs.

Time reversal flips the direction of spin, turning a ferromagnet into its time-reversed counterpart (Fig. 1a). The two configurations with opposite magnetization M , called domains, enable the storage,

processing, and retrieval of information in the form of a classical 0 or 1. Antiferromagnetic (AFM) order is also characterized by degenerate ground states related by $\mathcal{T}$, but $M = 0$ in each domain. In the simplest example neighboring spins are antiparallel (Fig. 1b). AFMs play an integral role in critical technologies^{10,11}, and interest in their properties has continued to grow^{12–15}. Zero magnetization can be a feature, as the absence of the long-range magnetic dipolar interaction leads to enhanced scalability.

A non-zero M induces a difference in the index of refraction of LCP and RCP light, yielding a mechanism for MOKE that is essentially the same in all FMs. MOKE is therefore a reliable technique for distinguishing FM domains with high-spatial resolution. In contrast, domains have been detected through MOKE only in a few AFMs^{16–18}, and the mechanism that underlies this signal has been attributed to specific properties of individual compounds.

Here, we focus on a class of AFMs in which the time-reversed states are related by translation by half the magnetic unit cell, $S_{1/2}$,

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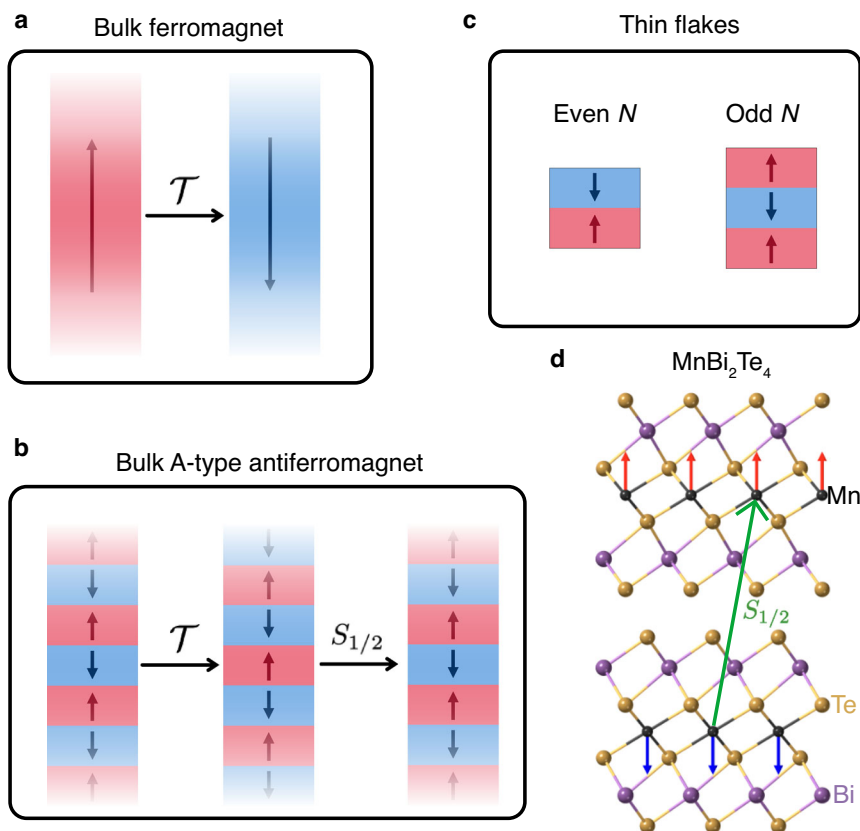


Fig. 1 | Schematics of representative magnetic structures. **a** Ferromagnet, where T reverses the sign of the order parameter; **b** A-type antiferromagnet, where the sign reversal by T can be undone by a translation by half a magnetic unit cell ($S_{1/2}$); **c** Thin flakes of an A-type antiferromagnet: flakes of odd layer number N have a net

magnetic moment, while those with even N do not. **d** Two layers of the MnBi_2Te_4 crystal and magnetic structure, demonstrating the A-type AFM phase. Opposite spins are related by $S_{1/2}$.

illustrated in bulk and thin flake forms in Fig. 1b, c, respectively. We choose this class because the product $TS_{1/2}$ ensures that the index of refraction of LCP and RCP light is the same as they propagate through an unbounded medium, a condition that at first sight seems to stipulate the absence of MOKE, since it is the difference of the two indices that causes MOKE in FMs. However, this conclusion is incorrect: MOKE by its nature involves a bounding surface that breaks $TS_{1/2}$, unless $S_{1/2}$ is parallel to the surface. Therefore, $TS_{1/2}$ imposes no constraints on MOKE at surfaces that break translational invariance described by $S_{1/2}$.

We investigate MnBi_2Te_4 , a layered topological AFM with a Néel temperature of 25 K¹⁹, as an example of a $TS_{1/2}$ -symmetric AFM. Spins in individual Mn layers in MnBi_2Te_4 are parallel to each other, and antiparallel to the spins in neighboring layers (Fig. 1d). This order, called A-type, persists to the surface of MnBi_2Te_4 ²⁰. MOKE was recently reported in the wavelength range of 500–1000 nm in thin flakes of MnBi_2Te_4 , in samples with an odd number of layers (N), which have a net magnetization, and in samples with an even N , which do not^{21–24}. While symmetry permits MOKE for all N , it does not identify the underlying mechanism.

Axion electrodynamics associated with topology was proposed as the mechanism for MOKE in MnBi_2Te_4 ^{23,25}. The discontinuity in the topological Z_2 invariant at the sample/vacuum interface manifests as a quantized surface Hall conductance, which is indistinguishable from a quantized trace of the magnetoelectric (ME) tensor in the static limit²⁶. The surface conductance gives rise to a traceful, non-quantized ME tensor above zero frequency^{25,27}. Optical phenomena associated with a traceful ME tensor (collectively known as axion electrodynamics²⁸), provide a mechanism for MOKE^{25,29,30}, as demonstrated in studies of the non-topological ME Cr_2O_3 ¹⁶.

A distinct mechanism for MOKE in $TS_{1/2}$ symmetric AFMs was proposed by Dzyaloshinskii and Papamichail³¹. They treated the layered AFM as a stack of FMs with alternating spin direction. The dielectric tensor of each layer is assumed to be the same as in an unbounded medium with the same FM order, and MOKE arises due to the variation in dielectric properties as the wave propagates. In the alternating FM framework, the optical response arises from the bulk magnetic structure, and the surface conductance does not play a special role, unlike in the axion electrodynamics mechanism, where the surface contribution is essential. The alternating FM mechanism is allowed in all collinear AFMs whose spins are oriented perpendicular to the layers, regardless of the number of layers, band topology or symmetry. To the best of our knowledge, MOKE arising from the alternating FM effect has not been experimentally recognized prior to this work.

In this work we report measurements of MOKE in an optically thick sample of MnBi_2Te_4 (~136 nm thick, Fig. S3), which we refer to as infinite layer MnBi_2Te_4 , as a function of magnetic field, H , wavelength of the optical probe, λ , and the position on the sample. We find that non-zero MOKE appears in the $M = 0$ state, and that its spectrum is quantitatively captured by the alternating FM model³¹, opening the door for MOKE studies of a broader class of AFMs than was previously considered feasible.

Results

The experiment: magnetic field, position, and wavelength dependence

The complex MOKE angle is defined by the relation, $\theta \equiv -i\delta r/r$, where the reflectivities of incident LCP and RCP light are given by $r = r_0 \pm \delta r$

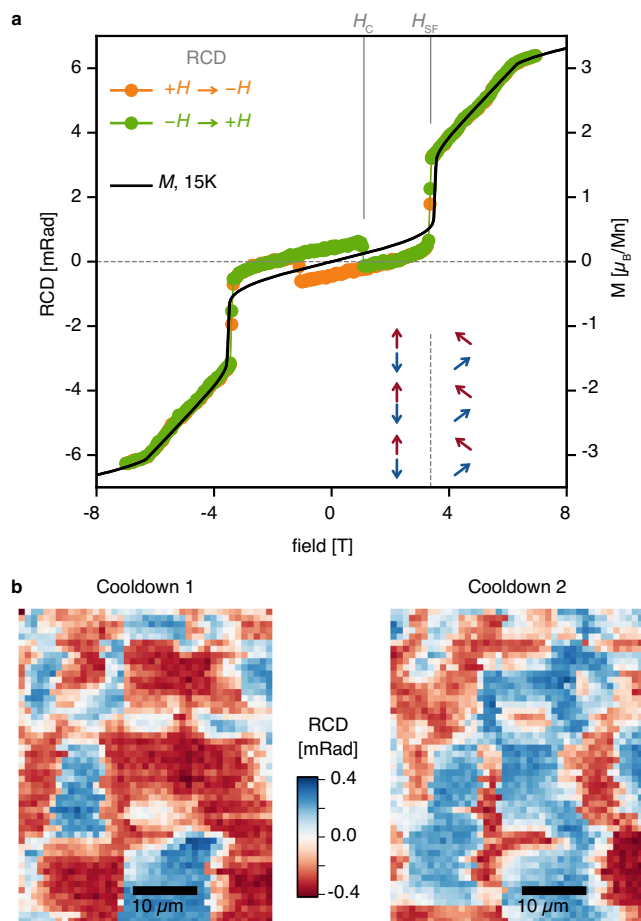


Fig. 2 | Magneto-optical measurements of MnBi₂Te₄. **a** Reflection circular dichroism (RCD) measured at 525 nm as a function of magnetic field, showing a jump at the spin-flop transition ($H_{SF} \approx 3.4$ T) and a hysteresis loop with a coercive field of $H_C \approx 1$ T. A small setup-induced background contribution has been subtracted (Fig. S7). RCD is compared with bulk magnetization measurements taken at 15 K with the field applied along the crystallographic c -axis (black line). The inset illustrates the bulk spin-flop transition. **b** Spatially resolved RCD measurements at $H = 0$, revealing AFM domain structures that change between cooldowns.

(the sign and polarization conventions are defined in the Methods section). Throughout this paper, we show measurements of the imaginary part of Θ , which is known as reflection circular dichroism (RCD). We measure RCD using a photoelastic modulator to vary the helicity of the incident light at 50 kHz, using a setup illustrated in Fig. S4. The change in reflectivity synchronous with the helicity modulation is proportional to RCD (see Methods for details of the experiment).

In Fig. 2a, we compare the magnetic field dependence of RCD to that of bulk magnetization at 15 K, measured on a sample from the same batch. RCD reveals two discontinuous features: a jump at $H_{SF} \approx 3.4$ T and a hysteresis loop with a coercive field of $H_C \approx 1$ T. The jump corresponds to a spin-flop (SF) transition, illustrated in the inset, which is also seen in magnetization. The corresponding magnetization increase is $\Delta M_{SF} \approx 1.2 \mu_B/\text{Mn} \approx 0.4 M_s$, where $M_s = 3 \mu_B/\text{Mn}$ is the ordered moment at 15 K³². The hysteresis loop has no counterpart in bulk magnetization measurements, which find $M = 0$ for $H < H_{SF}$. Therefore, the two non-zero values of RCD at $H = 0$ correspond to time-reversed states, each with $M = 0$. Further evidence for this interpretation is provided by spatially resolved measurements (Fig. 2b) that reveal spontaneous formation of domains with positive and negative RCD values in zero field, with distinct structures in different $H = 0$ cooldowns.

The existence of two discontinuities in RCD vs H provides an unusual opportunity to compare the MOKE spectrum in a phase with

$M \neq 0$, that is the spin-flop (SF) phase, and a $TS_{1/2}$ -symmetric AFM ($M = 0$) phase in the same material. We measured the magnetic field dependence of RCD in the photon energy range from 1.34 eV (925 nm) to 3.22 eV (385 nm) (Fig. S8), and extracted RCD spectra in the two phases. In Fig. 3a, we compare the RCD spectrum corresponding to the SF transition with the RCD spectrum in the AFM phase. The AFM spectrum is half of the difference between RCD at $H = 0^+$ and $H = 0^-$, where $H = 0^+$ and $H = 0^-$ denote zero field as approached from positive and negative fields. The SF spectrum, corresponding to the jump in magnetization across the transition, is given by $\Theta_{SF} = \Theta(3.4 \text{ T}) - [\Theta(3.2 \text{ T}) - \Theta(0^+)]$, because $\Theta(3.2 \text{ T})$ is a sum of the antiferromagnetic and magnetization contributions, while in the spin flop phase, at 3.4 T, there is no antiferromagnetic contribution.

The two spectra are strikingly different, ruling out a small uncompensated bulk ferromagnetic moment as a trivial explanation for RCD at $H = 0$. Further, in the SI (Fig. S2) we consider whether modified surface properties could account for this observation, and we conclude that such explanation is inconsistent with the data. This leaves us with the following conclusion: MOKE at $H = 0$ arises from the bulk antiferromagnetic structure. The fact that the two spectra are rich in features creates an opportunity to constrain theories: a suitable theoretical model should simultaneously reproduce both of them.

Lorentz model: infinite layer and finite samples

The RCD spectrum measured in the SF state is consistent with resonant MOKE in a FM. Both the magnitude and zero crossing can be reproduced by a Lorentz oscillator whose resonant photon energy differs for LC and RC polarized light. The corresponding dielectric function is:

$$\varepsilon_{\pm}(\omega) = \varepsilon_{\infty} + \frac{f}{(\omega_0 \pm \delta\omega)^2 - \omega^2 - i\gamma\omega}, \quad (1)$$

where f , ω_0 , and γ are oscillator strength, resonant frequency, and damping. These parameters, together with a background contribution, ε_{∞} , are chosen to reproduce the measured optical conductivity in the spectral range of interest, reported in ref. 33. The good agreement between the measured quantities and those calculated from the Lorentz model is shown in Fig. S5. Finally, $\delta\omega$, the difference in resonance frequency for LC and RC polarized light, is chosen to fit the magnitude of the measured RCD. The purple curve in Fig. 3b shows that the single oscillator model captures the main features of the observed ferromagnetic RCD spectrum (Fig. 3a).

Our quantitative description of RCD in the ferromagnetic phase of MnBi₂Te₄ leads us to consider the alternating FM model for the RCD in its AFM state: a stack of FM layers in which the sign of $\delta\omega$ alternates in neighboring layers. We use the transfer matrix formalism³⁴, following the approach in ref. 35, to calculate the reflection coefficient from the stack. The number of layers is 100, and the thickness of each layer, $d = 1.3$ nm, corresponds to the separation between spins in MnBi₂Te₄. The simulated RCD spectra for the two T -reversed AFM domains (Fig. 3d), are shown in red and blue in Fig. 3b. Remarkably, this minimal model captures the spectral shape and the magnitude of RCD in the AFM phase of MnBi₂Te₄, without introducing free parameters beyond those that describe the FM phase. In the SI we extend this analysis by using a dielectric function computed from a density functional theory (DFT) calculation to construct the alternating FM model, and we find that this approach also yields the correct magnitude of RCD in the AFM phase (Fig. S6). To the best of our knowledge, this is the first experimental evidence for an RCD arising from an alternating FM model in a bulk AFM.

Next, we show that the key features of RCD and transmission circular dichroism (TCD) that are seen in few layer crystals in ref. 23 can be understood within the same model. We performed a series of revealing transfer matrix calculations, varying the number of layers while keeping the thickness of individual layers fixed. In Fig. 4a, b we

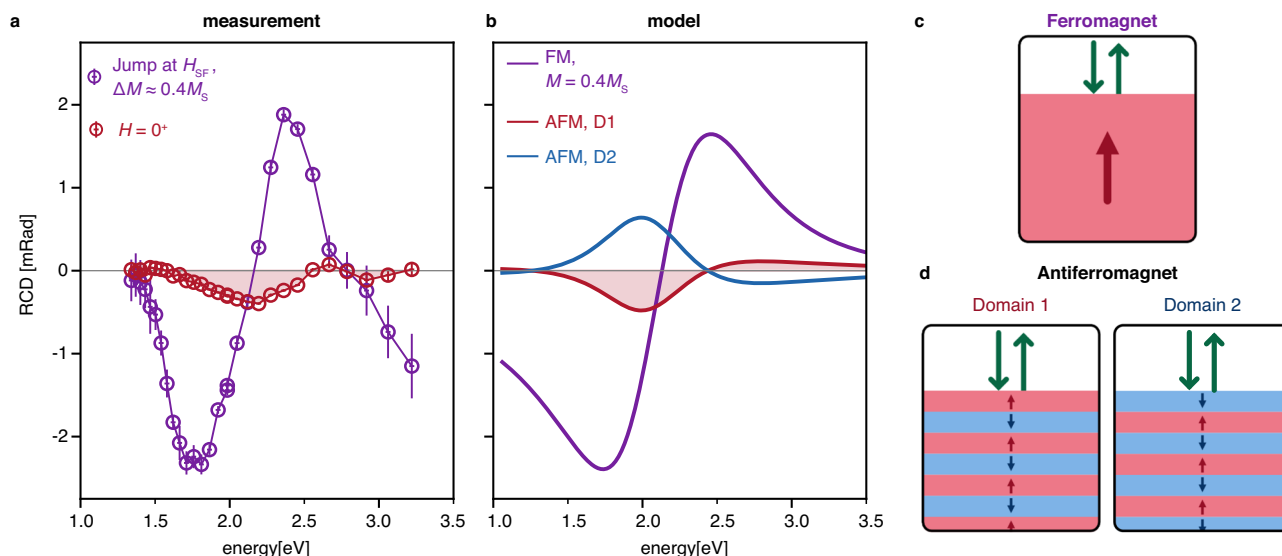


Fig. 3 | Spectroscopic signature of MOKE in antiferromagnetic MnBi₂Te₄.

a Measured RCD spectrum at the spin-flop transition (purple) and at zero field (red), showing distinct spectral shapes. For each photon energy, we measured the magnetic field dependence of RCD (Fig. S8). The AFM spectrum is half of the difference between RCD on the downward ($H = 0^+$) and upward ($H = 0^-$) field sweep, averaged across the hysteresis loop, between ± 0.9 T. The SF spectrum is given by $\Theta_{SF} = \Theta(3.4\text{ T}) - [\Theta(3.2\text{ T}) - \Theta(0^+)]$. The error bars for the $H = 0^+$ measurement represent the standard deviation across this field range. The larger error bars for the SF spectrum reflect the fact fewer measurements were used to extract the corresponding RCD value ($H = 3.4$ T and $H = 3.2$ T). Laser power fluctuations do not

contribute to these error bars, since the RCD is normalized by the simultaneously measured reflectivity (the same detector voltage is demodulated at two frequencies). The only relevant systematic uncertainty is from the PEM calibration, which for our Hinds PEM-100 is $\leq 5\%$, corresponding to < 0.1 mrad on the RCD scale. **b** RCD spectra computed from the Lorentz model (Eq. (1), with parameters from Table M1) for a ferromagnet (purple, schematic in **c**) and two antiferromagnetic domains (red and blue, schematics in **d**). The ferromagnetic RCD is scaled by a factor of 0.4 from that calculated for a saturated moment, to be directly comparable to the measured RCD jump at the spin-flop transition.

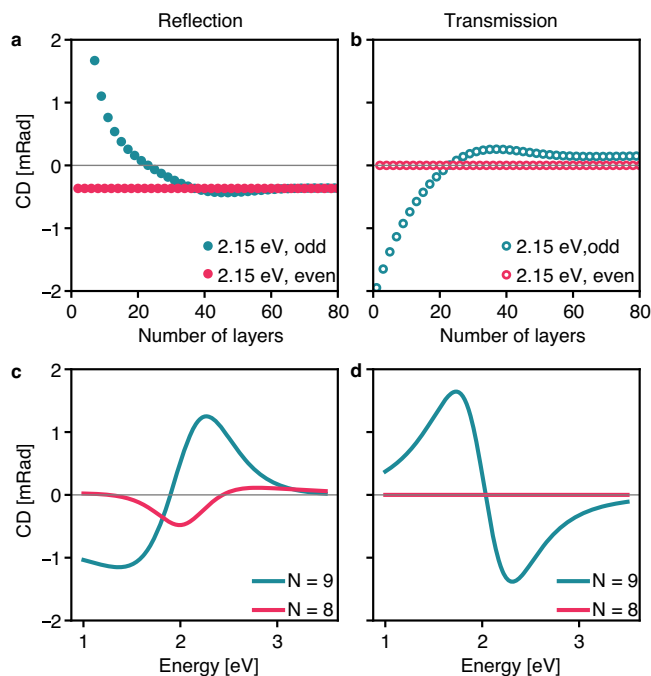


Fig. 4 | Dependence of circular dichroism on the number of layers. **a, b** Calculated reflection (RCD) and transmission (TCD) circular dichroism as a function of layer number for even and odd layer stacks, using the same model and parameters as in Fig. 3. **c, d** RCD and TCD spectra for 8-layer (8L) and 9-layer (9L) AFM stacks.

plot the calculated RCD and TCD, respectively, as a function of layer number at fixed photon energy. We find that both RCD and TCD depend strongly on N if it is odd, but are independent of N when it is even, consistent with the findings of ref. 31. When the slab thickness Nd

far exceeds the optical penetration depth, RCD in even and odd layer samples converge to the same value, as expected. TCD vanishes for all even layer stacks, a phenomenon that can be understood from a symmetry perspective: even layer stacks are symmetric under a product of inversion and time-reversal symmetry, which prohibits circular dichroism in transmission^{23,36–38}.

Further, the dichroism spectra for even and odd layer stacks are strikingly different (Fig. 4c, d). For $N = 8$, the RCD spectrum is identical to the spectrum of the bulk AFM crystal (Fig. 3b), while spectrum for $N = 9$ resembles that of the bulk SF phase, as $M \neq 0$ for odd layer stacks. The maximum RCD is about three times larger for $N = 9$ than for $N = 8$. However, these calculations assume that samples are suspended in vacuum, which is not a realistic experimental scenario. The transfer matrix approach allows us to include the substrate in the calculation of reflectivity³⁵, and we find that doing so preferentially suppresses dichroism in odd-layer samples. In Fig. S9 we show that the maximum magnitude of RCD for samples on sapphire and diamond substrates, used in ref. 23, is approximately equal in magnitude for even and odd layer stacks, while they maintain the characteristic spectral shapes shown in Fig. 4c. We therefore find that the alternating FM model with realistic parameters captures the main experimental results on N -even and N -odd flakes of MnBi₂Te₄ reported in ref. 23, as well as on infinite layer flakes reported here.

Bilayer: the exact solution and the physical picture

While the numerical results shown in the above section capture the experimental results, the underlying physics is somewhat mysterious, and poses the following questions: why does MOKE arise in $\mathcal{TS}_{1/2}$ -symmetric AFMs within the alternating FM model, and what influences its magnitude? Why is its value independent of the (even) number of layers? Why does TCD vanish? To address these questions, we first consider the analytical solution for MOKE in a bilayer, and then

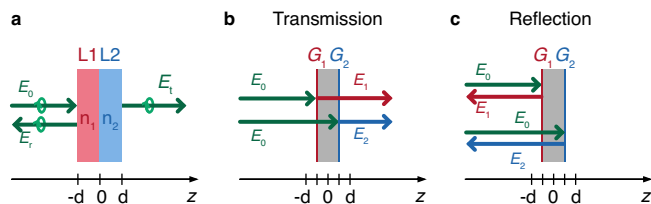


Fig. 5 | Illustration of the model for MOKE in an antiferromagnetic bilayer. **a** Schematic representation of a bilayer, consisting of two layers of indices of refraction $n_{1,2} = n \pm \delta n$ when probed with circularly polarized light. δn is induced by the opposite magnetization in the two layers, $\pm M_z$. **b, c** Simplified representation of a bilayer, where the layers are replaced by two infinitesimally thin sheets of conductances $G_{1,2} = G_0 \pm \delta G$, separated by a dielectric medium of thickness d and index of refraction n . The propagation-induced differences between fields emitted from the two sheets cancel in **(b)** transmission, but not in **(c)** reflection, leading to vanishing TCD and non-zero RCD.

offer an intuitive physical picture, shedding light on the experimental, numerical and analytical findings.

We consider a single bilayer of oppositely oriented FMs. Each layer is characterized by the index of refraction $n + \delta n$, where the sign of δn is opposite for the two layers (Fig. 5a). First, we utilize the transfer matrix approach to reproduce the expressions for the transmission and reflection coefficients of such a bilayer, derived in ref. 31. MOKE in the physically relevant limit ($k_0 d \ll 1$ and $\delta n \ll n$) is given by

$$\Theta_{AFM} = -k_0 n d \frac{2\delta n}{n^2 - 1} = (-ik_0 n d) \Theta_{FM}, \quad (2)$$

where Θ_{FM} is the Kerr angle of the corresponding bulk ferromagnet, $k_0 = \omega/c$ the wavevector in vacuum, and n the average index of refraction of the two layers. The expression for arbitrary layer thickness and δn is given in the Supplementary Information.

Eq. (2) showcases the common microscopic origin of the MOKE response of an AFM bilayer and that of the corresponding ferromagnet, but it also reveals a surprising aspect of the link between them. It is natural to assume that a $TS_{1/2}$ -symmetric type-A AFM can exhibit nonzero MOKE only if strong absorption (governed by the imaginary part of n) leads to disproportionate sampling of the top layer. However, Eq. (2) shows that this is not correct: the magnitude of Θ_{AFM} depends on the absolute value of the index, $|n|$, and is nonzero even in the absence of dissipation. The phase of n appears in the phase shift between Θ_{AFM} and Θ_{FM} , which manifests as the difference in the spectrum of RCD between AFM and FM structures, as seen for example in Fig. 3a.

To gain further insight into the physical mechanism behind the alternating FM scenario, we analyze a toy model (Fig. 5b, c) in which each of the two layers is replaced by an infinitesimally thin ferromagnetic sheet of optical conductance $G_{1,2}$, where 1, 2 are layer indices. The sheets are separated by a non-magnetic medium of thickness d and index of refraction n . For illustrative purposes we analyze a single reflection from each sheet.

We consider a circularly polarized plane wave propagating in the positive z direction with amplitude E_0 . The electric field generates sheet currents,

$$K_{1,2} = G_{1,2} E_0 e^{\mp ik_0 n d/2}, \quad (3)$$

where we have taken $z = 0$ as the midpoint between the sheets for convenience. The currents $K_{1,2}$ radiate, emitting electric fields,

$$E_{1,2}(z) = \frac{\mu_0 c}{2} K_{1,2} e^{ik_0 |z \pm d/2|}, \quad (4)$$

where c is the speed of light and μ_0 the vacuum permeability.

The total transmitted electric field, given by the sum of $E_1(z)$ and $E_2(z)$ for $z > d/2$, is,

$$E_T(z) = \mu_0 c E_0 \left(\frac{G_1 + G_2}{2} \right) e^{ik_0 z} = \mu_0 c E_0 G_0 e^{ik_0 z}. \quad (5)$$

As $E_T(z)$ depends only on the average conductance G_0 , the TCD is zero. The toy model shows that this is a consequence of cancellation of propagation factors. The incident wave propagates an additional distance d in the medium beyond layer 1 to induce currents layer 2. However, the wave emitted by layer 1 must propagate through the medium to reach a given point $z > d/2$. The total propagation factor, $e^{ik_0 z}$, for waves transmitted through the bilayer is the same, and independent of d (Fig. 5b). The sum of fields emitted from the two sheets therefore depends only on the sum of the currents, $G_1 + G_2$.

In contrast, the propagation factors for fields radiated in the $-z$ direction add, rather than cancel: the incident EM wave travels further to excite current in layer 2 and its radiated field propagates further before reaching an observer at $z < -d/2$ (Fig. 5c). The total reflected electric field is given by,

$$E_R(z) = \frac{\mu_0 c E_0}{2} e^{-ik_0 z} (G_1 e^{-ik_0 n d} + G_2 e^{ik_0 n d}) \approx \mu_0 c E_0 e^{-ik_0 z} (G_0 - \delta G i k_0 n d), \quad (6)$$

where we used $|k_0 n d| \ll 1$ in the expansion of the exponential. The term proportional to δG gives rise to Θ_{AFM} .

The toy model for a bilayer identifies the origin of nonzero Θ_{AFM} as the change in the electric field as it propagates, regardless of whether it is dominated by the real or imaginary component of n . We see that absorption does not play a special role in generating MOKE. Further, RCD does not depend on the layer number for even layers (Fig. 4a) because of the exponential nature of propagation: the ratio of fields in two neighboring layers is $\exp(ik_0 n d)$, independent of the number of layers. Thus the effects that yield RCD in two atomic layers and in a semi-infinite AFM crystal are the same. These qualitative features found in the toy model are retained when multiple reflections are included through the transfer matrix approach (Eq. (2), and Fig. 4).

Discussion

In this paper, we identify alternating FM layers as the origin of MOKE in an A-type antiferromagnet with $TS_{1/2}$ symmetry, therefore providing first experimental confirmation of the mechanism proposed by Dzyaloshinskii and Papamichail³¹. Within this theory, Θ_{AFM} is entirely determined by the MOKE response of the ferromagnetic layers that are the building blocks of the AFM, allowing us to test it directly by tuning MnBi_2Te_4 across the spin-flop transition, thus accessing Θ_{AFM} and Θ_{FM} in the same crystal. Based on the quantitative agreement between the measured RCD spectrum in the AFM phase and the theoretical prediction based solely on the FM spectrum, we conclude that MOKE observed at visible and near infrared wavelengths in MnBi_2Te_4 arises from alternating FM layers, rather than axion electrodynamics associated with band topology. Axion electrodynamics may dominate the MOKE response at terahertz frequencies below the bulk band gap^{25,27,39,40}, where there are no other optical transitions that could overwhelm their contribution, although results in even-layer flakes suggest that the axion contribution in this frequency range is weak^{27,39}.

The effect we observe is not limited to MnBi_2Te_4 , and is generically present in A-type antiferromagnets with spins out of plane. We believe that it has not been recognized experimentally in part because the signal vanishes when averaged over atomic steps, naturally present in as-grown bulk crystals. However, optical experiments in van der Waals materials regularly probe surfaces that are atomically flat across the length scale of a laser beam. We note that some previous sightings of MOKE in van der Waals AFMs with an even number of layers were conditionally attributed to extrinsic magnetization^{22,41,42}, given the widespread conviction that MOKE intrinsic to A-type AFMs was forbidden by symmetry. While this explanation is certainly plausible, our findings show that intrinsic MOKE in A-type AFMs is always allowed, and other mechanisms should be considered when θ_{AFM} cannot account for the magnitude, or the spectrum, of the observed signal.

Correctly estimating θ_{AFM} is therefore essential for interpretation of experimental results. Our work suggests a strategy to do so, both in bulk and thin flakes. In bulk, it is sufficient to combine measured θ_{FM} and optical conductivity with the analytical expression for θ_{AFM} (Eq. (2)). For thin flakes, it is important to consider the role of the substrate, which may suppress or enhance observed signals³⁵; we suggest the transfer matrix approach as a convenient way to do so. We note that $|\theta_{AFM}|$ is not generically small compared to the noise floor of modern experimental setups: it is suppressed with respect to $|\theta_{FM}|$ only by a factor of $|k_0nd| = |2\pi nd/\lambda|$, which is more than an order of magnitude larger than d/λ suggested by dimensional analysis.

Our findings show that MOKE is a powerful and general tool for investigating $TS_{1/2}$ symmetric AFMs. In this work we used it to image time-reversed domains, as shown for in Fig. 2b. Further, the nonzero θ_{AFM} enabled the discovery that a magnetic field can select antiferromagnetic domains (Fig. 2a) in such magnets, challenging the conventional view that antiferromagnets cannot be controlled by external magnetic fields. Uncovering the mechanism behind field control is beyond the scope of this study, but we note that the weakened exchange interaction at the surface is a plausible cause^{20,43}. This implies that details of the surface can affect the coercive field, as confirmed by measurements on two flakes exfoliated from the same batch (Fig. S1). However, the magnitude of the RCD at $H = 0$ is a bulk property, independent of local surface conditions. The coercivity and field-switching process will be the subject of future computational⁴⁴ and experimental investigations, enabled by the discovery of the AFM RCD signal. In summary, our results address fundamental questions concerning the origin of MOKE in AFMs, provide a strategy for studying and controlling their domains, and elucidate results on exfoliated van der Waals AFMs.

Methods

Complex MOKE: definitions

As discussed in the main text, MOKE is a manifestation of difference in reflectivity between the light of two circular polarizations. The Jones vectors corresponding to the circular polarizations are given by:

$$\hat{\mathbf{e}}_+ = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ i \end{pmatrix}, \text{ (LCP for } k_z > 0, \text{ RCP for } k_z < 0) \quad (\text{M1})$$

$$\hat{\mathbf{e}}_- = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -i \end{pmatrix}, \text{ (RCP for } k_z > 0, \text{ LCP for } k_z < 0), \quad (\text{M2})$$

capturing the fact that the LCP light becomes RCP upon reflection, and vice-versa. It is convenient to use the $\hat{\mathbf{e}}_{\pm}$ basis, rather than the LCP and RCP basis, so that reflection from an ideal isotropic mirror is captured by the identity matrix.

Vectors and matrices can be transformed between the $\hat{\mathbf{e}}_{\pm}$ basis and basis of linear ($\hat{\mathbf{e}}_{x,y}$) polarization using the following

transformation matrices:

$$\mathbf{A}_{C \rightarrow L} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ i & -i \end{pmatrix}, \mathbf{A}_{L \rightarrow C} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & -i \\ 1 & i \end{pmatrix}. \quad (\text{M3})$$

In the $\hat{\mathbf{e}}_{\pm}$ basis, the reflection matrix corresponding to circular dichroism is given by:

$$\mathbf{r}_C = \begin{pmatrix} r_0 + \delta r & 0 \\ 0 & r_0 - \delta r \end{pmatrix}, \quad (\text{M4})$$

In the $\hat{\mathbf{e}}_{x,y}$ basis the reflectivity matrix is then equal to:

$$\mathbf{r}_L = \begin{pmatrix} r_0 & r_{xy} \\ -r_{xy} & r_0 \end{pmatrix} = \begin{pmatrix} r_0 & -i\delta r \\ i\delta r & r_0 \end{pmatrix}. \quad (\text{M5})$$

The complex Kerr angle is defined as:

$$\Theta = \frac{r_{xy}}{r_0} = -i \frac{\delta r}{r_0}, \quad (\text{M6})$$

and RCD is the imaginary part of Θ .

RCD measurements

The experimental setup is shown in Fig. S4. The cryostat is Quantum Design Opticool, with a 7T magnet. Most measurements were done with a pulsed laser (output of Light Conversion Orpheus optical parametric amplifier, seeded by a Carbide laser, repetition rate 300 kHz, pulse duration ~ 250 fs), focused to a spot of lateral dimensions of ~ 4 μm . The position dependent measurements (Fig. 2b) were done with a continuous wave laser, with wavelength 532 nm, corresponding to the photon energy of 2.33 eV, which we found to offer good signal to noise throughout the studied field range (Fig. 3a). Spatial resolution is achieved by moving the sample underneath the focused laser spot using Attocube positioners. Regardless of the laser source, the average power of 1 μW reached the sample, the incident light was vertically polarized, and chopped using a mechanical chopper.

The incident vertical polarization is rotated by 45 deg using a half wave plate. The next element in the optical path is the photoelastic modulator (PEM) set to a 1/4 wave modulation, therefore modulating light polarization between linear and circular at 50 kHz. The light intensity was measured using a Si photo-diode, through the current input of the Zurich Instruments lock-in amplifier. The intensity was simultaneously demodulated at the chopper and at the PEM frequencies, yielding measured intensities I_c and I_p . $\text{Im}(\Theta)$ is found through their ratio as (see SI for a derivation):

$$\text{Im}(\Theta) = \frac{I_p}{I_c} \frac{1}{\pi J_1(\pi/2)} \approx \frac{I_p}{I_c} \frac{1}{1.78073}, \quad (\text{M7})$$

where J_1 is the Bessel function of first order. Extracting $\text{Im}(\Theta)$ through Eq. (M7) has the attractive feature that wavelength-dependent reflection and transmission properties of optical elements, as well as the responsivity of the photodiode, do not influence the measured spectrum, since they cancel out in the ratio $\frac{I_p}{I_c}$. Nonetheless, we took into account the wavelength dependence of the photodiode responsivity and the transmission through the beamsplitter to ensure that the power incident on the sample is ~ 1 μW across the spectral range.

Imperfections of optical elements, coupled with the Faraday rotation the cryostat windows and objective, result in a spurious field- and wavelength- dependent additive background in the RCD measurements. We measured the background on a Si/SiO₂ substrate, and subtracted it from measurements on MnBi_2Te_4 (Fig. S7). Since the

Table 1 | Parameters of the Lorentz model (Eq. (1)), used for the figures in the main text (Fig. 3b and Fig. 4)

γ/ω_0	$f/(\omega_0^2 \epsilon)$	$\omega_0[\text{eV}]$	$\delta\omega[\text{eV}]$	ϵ_∞/ϵ
0.424	4.2	2.05	-0.0708	$8.25 + 10.9i$

spectra in Fig. 3a were obtained through differential measurements, it was not necessary to measure the background contribution for each photon energy.

The error bars in Fig. 3a represent the statistical scatter of the RCD signal within the field range used to extract each value. For the AFM spectrum, the value at $H = 0$ is obtained by averaging the difference between down and up sweeps over the range ± 0.9 T, and the error bar is the standard deviation of the data points in that range. For the spin-flop spectrum, the value is taken from the difference between two field points (3.4 T and 3.2 T), so the standard deviation is correspondingly larger. Laser power fluctuations do not contribute, since the RCD is normalized by the simultaneously measured reflectivity (measurements were truly simultaneous, in that the same detector voltage is demodulated at two frequencies). The only relevant systematic uncertainty is from the PEM calibration, which here refers to the precision with which the modulation amplitude is known. We use a Hinds PEM-100, whose factory calibration guarantees retardation accuracy within 5% for a narrow monochromatic beam at normal incidence, which is sufficient for our purposes, as this level of uncertainty corresponds to < 0.1 mrad on the RCD scale in Fig. 3a.

Since our measurements are done with the sample in vacuum, and there are no electrical contacts on the sample, all of the thermalization is happening through the Si/SiO₂ substrate. This is very inefficient, leading to the known problem of large temperature gradients between the cryostat thermometer and the sample. Independently establishing the sample temperature is therefore difficult, but we use the bulk magnetization measurement as a ‘calibration’ - the agreement between the RCD measurement and the magnetization shows that the sample is at ≈ 18 K.

Transfer matrix calculations

The reflection and transmission coefficients for the AFM stack are found numerically through transfer matrix calculations, following the method detailed in ref. 35. This method offers a computationally convenient way to satisfy boundary conditions on the electric and magnetic fields at each interface, and captures the propagation through a uniform material by a phase factor of $\exp(ink_0d)$, where d is the thickness of the material, n the complex index of refraction, and $k_0 = \omega/c$ is the wave vector in vacuum.

We formulate the numerical transfer matrix calculation in the basis of linear polarization. If the dielectric tensor is diagonal in the basis of circular polarization,

$$\epsilon_C = \begin{pmatrix} \epsilon_+ & 0 \\ 0 & \epsilon_- \end{pmatrix} \quad (\text{M8})$$

in the basis of linear polarization it is given by:

$$\epsilon_L = \frac{1}{2} \begin{pmatrix} \epsilon_+ + \epsilon_- & i(\epsilon_- - \epsilon_+) \\ -i(\epsilon_- - \epsilon_+) & \epsilon_+ + \epsilon_- \end{pmatrix}. \quad (\text{M9})$$

This is the form of ϵ we use for transfer matrix calculations, with $\epsilon_\pm$ given by Eq. (1). The calculation will return the reflection matrix of the form given by Eq. (M5), with parameters given in Table 1, allowing us to calculate the complex Kerr angle through Eq. (M6), with its imaginary part corresponding to the reflection circular dichroism. A matrix of similar form is found for transmission.

We can use the same formalism to calculate the reflection and transmission from more complex structures. For instance, a calculation of reflection from a small N sample suspended in vacuum is unrealistic since samples are necessarily placed on substrates. In Fig. S9 we compare the reflection of a $N = 8$ and $N = 9$ layer sample suspended in vacuum to the same samples on sapphire and diamond substrates, as was done in experiments in ref. 23. We find that the $N = 9$ reflection is suppressed more than the $N = 8$ reflection, making the magnitude of the even and odd layer RCD very similar to each other.

Density functional theory

For our density functional calculations of the frequency-dependent dielectric function for MnBi₂Te₄, we employ the Vienna ab-initio software package (VASP)⁴⁵. We use the generalized gradient approximation (GGA) with the Perdew-Burke-Ernzerhof (PBE) functional⁴⁶. The Projector-augmented wave (PAW) method⁴⁷ with the standard VASP pseudopotentials is used, and we take Mn: 3d⁶4s¹; Bi: 5d¹⁰6s²6p³ and Te: 5s²5p⁴ electrons as valence. To approximately account for the localized nature of the unpaired d electrons in Mn, we use the DFT+U method⁴⁸ and adopt the rotationally invariant method by Dudarev et al.⁴⁹. We set $U = 4$ eV on the Mn atoms.

Given that MnBi₂Te₄ is a layered material, we implement van der Waals corrections, using the DFT-D3 method of Grimme et al.⁵⁰. We relax the bulk, primitive rhombohedral cell of MnBi₂Te₄ using a Gamma-centered mesh of $13 \times 13 \times 5$ to sample the Brillouin zone and a kinetic energy cutoff of 600 eV for our plane-wave basis set. For the structural relaxation, we neglect spin-orbit coupling (SOC), and enforce ferromagnetic order of the Mn ions using spin-polarized collinear calculations. We use a Gaussian smearing for the partial occupancies with a smearing width of 0.01 eV.

To calculate the frequency-dependent dielectric tensor within the independent particle approximation (that is, neglecting local field effects), we use the method developed by Gajdoš et al.⁵¹. For these calculations we include SOC self-consistently and enforce ferromagnetic ordering with the spin axis perpendicular to the Mn layers. Having first obtained the ground-state electronic density and corresponding Kohn-Sham states in a self-consistent DFT calculation, the imaginary part of ϵ is calculated with these wavefunctions using the following equation:

$$\epsilon_{\alpha\beta}^{(2)}(\omega) = \frac{4\pi^2 e^2}{\Omega} \lim_{q \rightarrow 0} \frac{1}{q^2} \sum_{c,v,\mathbf{k}} 2w_{\mathbf{k}} \delta(\epsilon_{c\mathbf{k}} - \epsilon_{v\mathbf{k}} - \omega) \times \langle u_{c\mathbf{k}+\mathbf{e}_\alpha q} | u_{v\mathbf{k}} \rangle \langle u_{c\mathbf{k}+\mathbf{e}_\beta q} | u_{v\mathbf{k}} \rangle^*, \quad (\text{M10})$$

Here, $w_{\mathbf{k}}$ is the weight of point $\mathbf{k}$ in the discrete summation over the Brillouin zone, Ω is the volume of the unit cell, and the indices c and v denote conduction and valence bands respectively, with ϵ_c and ϵ_v being their respective energies at the wavevector $\mathbf{k}$. $\mathbf{e}_\alpha$ is the unit vector in Cartesian direction α . To get the real part of the dielectric function we use the Kramers-Kronig transformation

$$\epsilon_{\alpha\beta}^{(1)}(\omega) = 1 + \frac{2}{\pi} \mathcal{P} \int_0^\infty \frac{\omega' \epsilon_{\alpha\beta}^{(2)}(\omega')}{\omega'^2 - \omega^2 + i\eta} d\omega', \quad (\text{M11})$$

Where $\mathcal{P}$ is the principal value and η is a Lorentzian broadening. For both the self-consistent DFT calculation to obtain converged wave functions and evaluation of the dielectric function, we use a $17 \times 17 \times 5$ Gamma-centered mesh, and we use 540 bands to ensure that we have sufficient unoccupied bands for convergence of the summation. We select a Lorentzian broadening of 0.1 eV.

Crystal growth, sample preparation, and thickness measurements

MnBi₂Te₄ bulk crystals were grown using a Bi-Te flux, following the previously reported recipe in ref. 32. The magnetization data in fields up to 12 T were collected using the AC option of a Quantum Design physical property measurement system.

In this work, we study thin bulk samples (infinite layer) with a thickness of 136 nm, corresponding to approximately 100 septuple layers. These samples are similar to bulk crystals and are not air-sensitive, in contrast to atomically thin flakes which can degrade in air over time^{19,21}. Nevertheless, care has been taken to minimize sample exposure to air before measurements.

To obtain thin bulk samples with atomically flat surfaces suitable for RCD studies, we used Scotch tape exfoliation of bulk crystals onto silicon wafers covered with 285 nm SiO₂ (we used 3M Magic Scotch Tape). The silicon wafers were pre-treated with RF O₂ plasma (duration: 10 min; power: 80 W; O₂ gas flow: 10 SCCM) before exfoliation to increase adhesion of crystals and overall yield. The exfoliation process was performed entirely inside a glovebox filled with inert argon gas, maintaining O₂ and H₂O levels below 0.1 ppm.

Once thin bulk samples of suitable dimensions were identified using an optical microscope, they were transported for loading into the low-temperature cryostat with optical access using a sealed container filled with argon. Care was taken to minimize air exposure during cryostat loading; we estimate that the sample was exposed to air for a maximum of 5 min before measurements. Based on the careful studies of oxidation on MnBi₂Te₄⁵², it is possible that the surface layer oxidized. However, the oxidation is self-limiting to the surface atomic layer⁵², and therefore cannot dominate our optical measurements with 30 nm penetration depth. The height of the studied thin bulk sample was measured after RCD measurements were completed using atomic force microscopy (Asylum Research Cypher S, tapping mode) in air.

Data availability

The datasets generated and analyzed during the study of “Magneto-optical Kerr effect in an A-type antiferromagnet” are available in the ISTA REX repository with <https://doi.org/10.15479/AT-ISTA-21422>.

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Author contributions

V.S. and S.K. performed the optical experiments. V.S. analyzed the optical data and performed the transfer matrix calculations. S.A., V.J., and D.O. fabricated and characterized samples. S.W. performed and analyzed the density functional theory calculations. J.-Q.Y. synthesized the single crystals and provided the magnetization measurement. V.S., J.O., and D.O. conceived and supervised the project and wrote the manuscript with input from all authors.

Competing interests

The authors declare no competing interests.

Additional information

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